

1. Consider the following language  $B = \{ \langle X, Y \rangle \mid X \text{ and } Y \text{ are regular languages and } X \subseteq Y \}$ . Show that  $B$  is decidable.
2. Using the fact that  $E_{DFA}$  is a decidable language prove that  $C$  is decidable, where  $C = \{ \langle R \rangle \mid R \text{ is a regular expression describing a language containing at least one string } w \text{ that has } 010 \text{ as a substring} \}$ .
3. Rank the following functions:  $\lg \lg n, (\sqrt{2})^{\lg n}, n^3, 2^{2^n}, n2^n, n \lg n, n, (\frac{3}{2})^n$  by order of growth; that is find an arrangement  $g_1, g_2, \dots, g_8$  of the functions satisfying  $g_1 = O(g_2), g_2 = O(g_3), \dots, g_7 = O(g_8)$ .