Composite schemes

- Fix a symmetric encryption scheme and a message authentication code
- There are several ways to use them together
 - 1. Encrypt-and-MAC
 - 2. MAC-then-Encrypt
 - 3. Encrypt-then-MAC
- If the components are secure, are the composite schemes secure (provide privacy and integrity)?

1



2



<u>Theorem1</u>. There exist an IND-CPA SE and SUF-CMA MAC s.t. EaM constructed as above is NOT IND-CPA secure.

3



Encrypt-then-MAC !

- Fix a symmetric encryption scheme $SE = (\mathcal{K}_{e}, \mathcal{E}, \mathcal{D})$ and a MAC $MAC = (\mathcal{K}_{u}, \mathcal{T}, \mathcal{V})$
- Consider a symmetric encryption scheme $\mathit{EtM} = (\overline{\mathcal{K}}, \overline{\mathcal{E}}, \overline{\mathcal{D}})$

$\begin{array}{l} \text{Algorithm } \overline{\mathcal{K}} \\ K_e \stackrel{\S}{\leftarrow} \mathcal{K}_e \\ K_m \stackrel{\S}{\leftarrow} \mathcal{K}_m \\ \text{Return } \langle K_e, K_m \rangle \end{array}$	$\begin{array}{l} \operatorname{Algorithm} \overline{\mathcal{E}}_{\langle Ke,Km \rangle}(M) \\ C' \leftarrow \mathcal{E}_{Ke}(M) \\ \tau' \leftarrow \mathcal{T}_{Km}(C') \\ C \leftarrow C' \tau' \\ \operatorname{Return} C \end{array}$	$\begin{array}{l} \text{Algorithm} \ \overline{\mathcal{D}}_{(Ke,Km)}(C) \\ \text{Parse } C \text{ as } C' \tau' \\ M \leftarrow \mathcal{D}_{Ke}(C') \\ v \leftarrow \mathcal{V}_{Km}(C',\tau') \\ \text{If } v = 1, \text{ return } M \\ \text{ else return } \bot. \end{array}$
--	--	---

<u>Theorem3</u>. For every IND-CPA SE and SUF-CMA MAC, EtM constructed as above is IND-CPA, INT-CTXT and IND-CCA secure.

5

<u>Proof</u>. We will show that for every adversary A attacking *ind-cpa* security of EtM there exists an adversary B attacking *ind-cpa* security of SE with the same resources, and for every adversary A attacking *int-ctxt* security of EtM there exists an adversary F attacking *suf-cma* security of MAC with the same resources s.t.

- 1) $Adv_{EtM}^{ind-cpa}(A) \le Adv_{SE}^{ind-cpa}(B)$
- 2) $Adv_{EtM}^{int-ctxt}(A) \le Adv_{MAC}^{suf-cma}(F)$

and the statement of the theorem will follow by using the theorem we proved before: [IND-CPA \wedge INT-CTXT \Rightarrow IND-CCA].

```
\begin{split} & \text{Adversary } B^{\mathcal{E}_{6}(\mathcal{L}_{n}^{(\cdot,b)})} \\ & K_{m} \stackrel{s}{\to} \mathcal{K}_{m} \\ & \text{For } i=1,\ldots,q \text{ do} \\ & \text{ When } A \text{ makes a query } (M_{i0},M_{i,1}) \text{ to its left-cr-right encryption oracle do} \\ & C_{i} \leftarrow \mathcal{E}_{K_{6}}(\mathcal{LR}(M_{i0},M_{isl},b)); \ \tau_{i} \leftarrow \mathcal{T}_{K_{m}}(C_{i}); \ A \leftarrow C_{i} || \tau_{i} \end{split}
```

 $A \Rightarrow b'$ Return b'

6



