

Randomized FDH-RSA (PSS0)

PSS0 is a randomized variant of the FDH-RSA scheme. It has the same key generation algorithm.

PSS0 also uses $H: \{0,1\}^* \rightarrow Z_N^*$, a random function to which all parties have oracle access to, and it has a parameter s

<p>Algorithm $\text{Sign}_{N,p,q,d}^{H(\cdot)}(M)$</p> <p>$r \xleftarrow{\\$} \{0,1\}^s$ $y \leftarrow H(r \parallel M)$ $x \leftarrow y^d \bmod N$ Return (r, x)</p>	<p>Algorithm $\text{VF}_{N,e}^{H(\cdot)}(M, \sigma)$</p> <p>Parse σ as (r, x) where $r = s$ $y \leftarrow H(r \parallel M)$ If $x^e \bmod N = y$ Then return 1 else return 0</p>
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Security of PSS0

- Theorem.** [Under the RSA assumption the PSS0 signature scheme is uf-cma secure in the random oracle (RO) model.] Let K_{rsa} be an RSA generator and let DS be the PSS0 signature scheme. Let F be an adversary making at most q_{hash} queries to its hash oracle and at most q_{sign} queries to its signing oracle where $q_{\text{hash}} \geq q_{\text{sign}} + 1$. Then there exists an adversary I with comparable resources s.t.

$$\text{Adv}_{DS}^{\text{uf-cma}}(F) \leq \text{Adv}_{K_{\text{rsa}}}^{\text{ov-koa}}(I) + \frac{(q_{\text{hash}} - 1) \cdot q_{\text{sig}}}{2^s}$$

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Other signature schemes

- Let's consider several signature schemes whose security relies on the hardness of the DL problem.
- Schnorr signature scheme

<p>Algorithm $K(k)$</p> <p>pick a k-bit prime p s.t. $p=2q+1$ pick $g \in Z_p^*$ of order q $x \xleftarrow{\\$} Z_q$ $X \leftarrow g^x$ Pick a hash function $H: \{0,1\}^* \rightarrow Z_q$ Return $((H, g, p, q, X), (H, g, p, q, x))$</p>	<p>Algorithm $\text{Sign}_{\text{sk}}(M)$</p> <p>$y \xleftarrow{\\$} Z_q$ $Y \leftarrow g^y \bmod p$ $c \leftarrow H(M \parallel Y)$ $s \leftarrow y + cx \bmod q$ Return (Y, s)</p>
<p>Algorithm $\text{VF}_{\text{pk}}(M, (Y, s))$</p> <p>$c \leftarrow H(M \parallel Y)$ If $g^s = YX^c \pmod{p}$ then return 1 else return 0</p>	

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Other signature schemes

- ElGamal signature scheme

<p>Algorithm $K(k)$</p> <p>pick a k-bit prime p pick a generator g of Z_p^* $x \xleftarrow{\\$} Z_{p-1}$ $X \leftarrow g^x$ Pick a hash function $H: \{0,1\}^* \rightarrow Z_{p-1}$ Return $((H, g, p, q, X), (H, g, p, q, x))$</p>	<p>Algorithm $\text{Sign}_{\text{sk}}(M)$</p> <p>$y \xleftarrow{\\$} Z_{p-1}$ $Y \leftarrow g^y \bmod p$ $s \leftarrow y^{-1} (H(M \parallel Y) - xY) \pmod{p-1}$ Return (Y, s)</p>
<p>Algorithm $\text{VF}_{\text{pk}}(M, (Y, s))$</p> <p>If $X^Y Y^s = g^{H(M \parallel Y)} \pmod{p}$ then return 1 else return 0</p>	

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Security of Schnorr and ElGamal signatures

- The Schnorr and ElGamal signature schemes are uf-cma secure in the random oracle (RO) model in groups where the discrete logarithm (DL) problem is hard.