# Multivariate Visual <br> Representations 2 

CS 7450 - Information Visualization
Sep. 15, 2011
John Stasko

## Recap

- We examined a number of techniques for projecting $>2$ variables (modest number of dimensions) down onto the 2D plane

Scatterplot matrix

- Table lens
- Parallel coordinates
etc.


## Varieties of Techniques



## Dust \& Magnet

- Altogether different metaphor
- Data cases represented as small bits of iron dust
- Different attributes given physical manifestation as magnets
- Interact with objects to explore data


## Interface



## Interaction

- Iron bits (data) are drawn toward magents (attributes) proportional to that data element's value in that attribute Higher values attracted more strongly
- All magnets present on display affect position of all dust
- Individual power of magnets can be changed
- Dust's color and size can connected to attributes as well


## Interaction

- Moving a magnet makes all the dust move

Also command for shaking dust

- Different strategies for how to position magnets in order to explore the data


## See It Live


ftp://ftp.cc.gatech.edu/pub/people/stasko/movies/dnm.mov
Video \&
Demo

## Set Operations

- Different type of problem
- Large set of items, each can be in one or more sets
- How do we visually represent the set membership?


## Standard Technique



Contains all possible zones of overlap

## Alternately

Euler
Diagram
Does not necessarily show all possible overlap zones

But what's the problem?

## Bubble Sets



Video

## ComED \& DupED



## Step Back

- Most of the techniques we've examined work for a modest number of data cases or variables

What happens when you have lots and lots of data cases and/or variables?

## Many Cases

## Recalll



Out5d dataset (5 dimensions, 16384 data items)

## Many Variables



## Strategies

- How are we going to deal with such big datasets with so many variables per case?
- Ideas?


## General Notion

- Data that is similar in most dimensions ought to be drawn together
- Cluster at high dimensions
- Need to project the data down into the plane and give it some ultra-simplified representation
- Or perhaps only look at certain aspects of the data at any one time


## Mathematical Assistance 1

- There exist many techniques for clustering high-dimensional data with respect to all those dimensions
Affinity propagation
k-means
- Expectation maximization
- Hierarchical clustering


## Mathematical Assistance 2

- There exist many techniques for projecting n-dimensions down to 2-D (dimensionality reduction)

Multi-dimensional scaling (MDS)

- Principal component analysis
- Linear discriminant analysis
- Factor analysis


## Other Techniques

- Other techniques exist to manage scale

Sampling - We only include every so many data cases or variables
Aggregation - We combine many data cases or variables

Interaction (later)

- Employ user interaction rather than special renderings to help manage scale


## Our Focus

- Visual techniques
- Many are simply graphic transformations from N-D down to 2-D



## Use?

- What kinds of questions/tasks would you want such techniques to address?
Clusters of similar data cases
- Useless dimensions
- Dimensions similar to each other
- Outlier data cases
- Think back to our "cognitive tasks" discussion


## Now

- We'll examine a number of other visual techniques intended for larger, higherdimensional data sets


## Can We Make a Taxonomy?

- D. Keim proposes a taxonomy of techniques

Standard 2D/3D display
Bar charts, scatterplots
Geometrically transformed display Parallel coordinates
Iconic display
Needle icons, Chernoff faces
Dense pixel display
What we're about to see...
Stacked display
Treemaps, dimensional stacking

## Minimum Possible?

- We have data cases with variables
- What's the smallest representation we can use?
How?


## Dense Pixel Display

- Represent data case or a variable as a pixel
- Million or more per display
- Seems to rely on use of color
- Can pack lots in
- Challenge: What's the layout?


## One Representation

- Grouping arrangement
- One pixel per variable
- Each data case has its own small rectangular icon
- Plot out variables for data point in that icon using a grid or spiral layout


## Illustration



## Spiral Technique

| 9 | 10 |  |
| :--- | :--- | :--- |
| 8 | 1 | 2 |
| 7 | 0 | 3 |
| 6 | 5 | 4 |

## Dimensions

## Related Idea

- Pixel Bar Chart
- Overload typical bar chart with more information about individual elements


## Idea 1



Height encodes quantity


Width encodes quantity

## Idea 2

- Make each pixel within a bar correspond to a data point in that group represented by the bar

Can do millions that way

- Color the pixel to represent the value of one of the data point's variables


## Idea 3



Each pixel is a customer
Color encodes amount spent by that person
High-bright, Low-dark
Ordered by that color attribute too
Right one shows more customers

## Idea 4



Product type is $x$-axis divider
Customers ordered by $y$-axis: dollar amount
$x$-axis: number of visits
Color is (a) dollar amount spent, (b) number of visits, (c) sales quantity

## Idea 5



Figure 7 Dividing attributes on $x$ - and $y$-axis (e.g., $D_{x}=$ Product Type, $D_{\gamma}=$ Region .

Can divide on two different attributes on $x$ and $y$


Figure 9 Multiple coloring attributes (e.g., $C_{1}=$ dollar amount,
$C_{2}=$ no. of visits, $C_{3}=$ quantity, $C_{4}=$ rocion)
 Amount, $O_{y}=$ Quantity).

Order items on both x and y

CS 7450

## Idea 6

Mapping specified by 5 tuple $<D_{x}, D_{y}, O_{x}, O_{y}, C>$

$D_{x}$ - Attribute partitions $x$ axis
$D_{y}$ - Attribute partitions y axis
$\mathrm{O}_{\mathrm{x}}$ - Attribute specifies x ordering
$\mathrm{O}_{\mathrm{y}}$ - Attribute specifies y ordering
C - Attribute specifies color mapping

Figure 13 Multi-pixel bar chart for mining 405,000 sales transaction records. ( $D_{x}=$ Product Type, $D_{y}=\perp, O_{x}=$ no. of visits, $O_{y}=$ dollar amount, C). (a) Color: dollar amount. (b) Color: no. of visits. (c) Color: quantity.

1. Product type 7 and product type 10 have the top dollar amount customers (dark colors of bar 7 and 10 in Figure

13a)
2. The dollar amount spent and the number of visits are clearly correlated, especially for product type 4 (linear
increase of dark colors at the top of bar 4 in Figure 13b)
3. Product types 4 and 11 have the highest quantities sold (dark colors of bar 4 and 11 in Figure 13c)
4. Clicking on pixel A shows details for that customer

## Thoughts?

- Do you think that would be a helpful exploratory tool?


## High Dimensions

- Those techniques could show lots of data, but not so many dimensions at once
Have to pick and choose


## Another Idea

- Use the dense pixel display for showing data and dimensions, but then project into 2D plane to encode more information
- VaR - Value and relation display


## Algorithm

- Find a correlation function for comparing dimensions
- Calculate distances between dimensions (similarities)
- Make each dimension into a dense pixel glyph
- Assign position for each glyph in 2D plane using multi-dimensional scaling



## Questions

- What order are the data cases in each dimension-glyph?
- Maybe there is a predefined order

Choose one dimension as "important" then order data cases by their values in that dimension
"Important" one may be the one in which many cases are similar

## Alternative

- Instead of each glyph being a dimension, it can be a data case


## Follow-on Work

- Use alternate positioning strategies other than MDS
- Use Jigsaw map idea (Wattenberg, InfoVis '05) to lay out the dimensions into a grid
Removes overlap
- Limits number that can be plotted


## New Layout

Plot the glyphs into the grid positions


## HCE

- Hierarchical Clustering Explorer
- Implements "rank by feature" framework
- Help guide user to choose 1D distributions and 2D scatterplots from various dimensions of a data set
- Combine statistical analysis with userdirected exploration


## Idea

- Choose a feature detection criterion to rank 1D and 2D projections of a data set
- Use person's perceptual abilities to pick out interesting items from view

HCE UI


## Operation

- When you choose the histogram ordering or scatterplot ordering tabs at the bottom left, these give results based on various statistical measures
- You can then choose some of them to visualize

Demo


## Recap

- We've seen many general techniques for multivariate data these past two days
Know strengths and limitations of each
Know which ones are good for which circumstances

We still haven't explored interaction much

## HW 3

- Visualization design
- Due Tuesday
- Bring two copies
- Questions?


## Upcoming

- Tufte's Design Principles

Reading:
Envisioning Information (if you have it)

- Few's Design Guidance

Reading
Now You See It chapters 5-12

