3-D Clipping and other things

Aside: Windows and Viewports

Window on Viewplane

Interface Window

Viewport
Window to Viewport Xform

Choose Window in World Coordinates

Xform window to Canonical View & Clip

Scale to size of Viewport

Translate to proper position on screen (Interface Window)

Notes on Window to Viewport

- Inverse relationship between window and viewport
  - As the window increases in size, the image in the viewport decreases in size and vice versa
- Beware of aspect ratio
### Example

1. Scale to correct size
2. Translate to proper coordinates

\[
\begin{bmatrix}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1 \\
\end{bmatrix}
\quad \begin{bmatrix}
0 & 0 & 0 \\
0 & 0 & 0 \\
0 & 0 & 1 \\
\end{bmatrix}
\]

### Culling Revisited

- **Trivial accept/reject of whole objects**
  - Fast, simple approach
    - Maintain bounding sphere
    - Fast, simple check against canonical volume
- **Only clip polygons of remaining objects**
  - Can't skip clipping of trivially accepted objects in practice
2D Clipping

A point is visible if

\[ x_l < X < x_r \]
and
\[ y_b < Y < y_t \]

- Line visible if both endpoints in window
- "Brute Force Method"
  - Solve simultaneous equations for intersections of lines and edges

Cohen-Sutherland Algorithm

- Region Checks: Trivially reject or accept lines and points
- Fast for large windows (everything is inside) and for small windows (everything is outside)
- 4-bit outcodes:
  - Bit 1 \( \leftarrow \) sign bit of \((y_t - Y)\) -- point is above window
  - Bit 2 \( \leftarrow \) sign bit of \((Y - y_b)\) -- point is below window
  - Bit 3 \( \leftarrow \) sign bit of \((x_r - X)\) -- point is to right of window
  - Bit 4 \( \leftarrow \) sign bit of \((X - x_l)\) -- point is to left of window
Cohen-Sutherland Clipping (cont.)

- Trivially accept a line if:
- Trivially reject a line if:

Clipping Lines Not Accepted or Rejected (“divide and conquer”)

Example:

Line AD: 1) Test outcodes of A and D → can’t accept or reject.
2) Calculate intersection point B, which is conceptually on the window side of the dividing line. Form new line segment AB and discard the rest of the line because it is above the window.
3) Test outcodes of A and B, Reject.
Sutherland-Hodgman Polygon Clipping

- Clip against each edge of the window one edge at a time
- New set of vertices after each clip
  - The number of vertices usually changes and will often increase.

Polygon Clipping Algorithm

- Window determines a visible and invisible region
- Edge from $i$ to $i+1$ one of four types:
  - Exit visible region - save the intersection
  - Wholly outside visible region - save nothing
  - Enter visible region - save intersection and endpoint
  - Wholly inside visible region - save endpoint
**Polygon clipping issues**

- Final output, if any, is always considered a single polygon
  - Might be multiple pieces
- Extra edge may not be a problem
  - Always occurs on a window boundary
  - Can be eliminated if necessary

**Pipelined Polygon Clipping**

- Clip against each edge independently

```
Clip Top → Clip Right → Clip Bottom → Clip Left
```

- Arrange clipping stages in a pipeline
  - Input polygon clipped against one edge
  - Retained points passed to next stage

- Can avoid intermediate storage
**3D Canonical Parallel View Volume**

Extension of 2-D algorithm, 6-bit outcode

- Bit 1 - above view volume \( y > 1 \)
- Bit 2 - below view volume \( y < -1 \)
- Bit 3 - right of view volume \( x > 1 \)
- Bit 4 - left of view volume \( x < -1 \)
- Bit 5 - behind view volume \( z < -1 \)
- Bit 6 - front of view volume \( z > 0 \)

**3D Canonical Perspective View Volume**

Extension of 2-D algorithm, 6-bit outcode

- Bit 1 - above view volume \( y > -z \)
- Bit 2 - below view volume \( y < z \)
- Bit 3 - right of view volume \( x > -z \)
- Bit 4 - left of view volume \( x < z \)
- Bit 5 - behind view volume \( z < -1 \)
- Bit 6 - front of view volume \( z > z_{\text{min}} \)
Canonical View Volume

- Trivially accept
  - Both endpoints have a code of all zeros
- Trivially rejected
  - Logical AND of the codes is not all zeros.
- Otherwise Calculate intersections.

Intersection Calculation (Perspective Volume)

On the $y = z$ plane
From parametric equation of the line:
$$y_0 + t(\ y_1 - y_0) = z_0 + t(\ z_1 + z_0)$$
Solve for $t$
$$t = (z_0 - y_0) / ((y_1 - y_0) - (z_1 - z_0))$$
Calculate $x$ and $y$
Already know $z = y$
Clipping in Homogeneous Coordinates

- Two reasons:
  - Efficiency
  - Correctness

Picking

- Goal: To use the mouse (2D) to select 3D objects
- Analytical method
  - gluUnproject
  - expensive
What are we trying to find?

- The objects that lie on the line that projects to the mouse position

Screen corresponds to Canonical View Volume

- What sliver lies under the mouse?
Scale Sliver to Screen:
gluPickMatrix

- After Viewing Transform
- Before Clipping

How to know what gets drawn?

- OpenGL Selection Modes (Picking and Feedback) (chapter 13)
  - glRenderMode, glSelectBuffer

- Add “names” to rendering stream
  - glInitNames, glLoadName, glPushName, glPopName