

CS 6340

Software Analysis and Testing

Mary Jean Harrold

Aristotle Research Group
SPARC/CERCS
College of Computing
Georgia Tech

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Class 1

- Introductions; Student Information
- Details (syllabus, etc.)
 - Shown on T-Square (<https://t-square.gatech.edu>)
- Basic Analyses (1): intermediate representations, control-flow analysis,
- Assign
 - Basic Analyses (1): Be familiar with concepts
 - Representation and Analysis of Software (Sections 1-5) (Schedule has link)
 - Problem Set 1 (Schedule has link): due 8/25/09

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Course Overview, Syllabus

- Motivation for studying program analysis and testing
- Course objectives
 - Learn traditional, promising analyses
 - Learn traditional, new applications
 - Explore research areas in analysis, use of artifacts
 - Apply analyses and applications through homework, semester project
- Means for approaching course objectives
 - Class lectures, readings, homework, class presentations
 - Semester project (proposal, oral, written report)
 - Exams

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Course Overview, Syllabus

- Your responsibilities
 - Arrive on time, attend all classes
 - Prepare (read papers before class), participate in class
 - Submit homework, projects, etc. at the beginning of class on the due date
- Course evaluation
 - Homework: 30%
 - Semester project (proposal, written, oral): 30%
 - Exams: 30%
 - Class participation: 10%
- Prerequisites
 - CS 4240, graduate-level standing, permission of instructor

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Overview of Course

- Static analyses (computed without execution)
 - Intraprocedural (within a single procedure)
 - AST, control-flow, control-dependence, data-flow, etc.
 - Complicating factors
 - Interprocedural (across procedure boundaries), recursion
 - Pointers, references, polymorphism, dynamic binding, etc.
 - Slicing, analysis by reachability, demand analysis
 - Applications
- Dynamic analyses (computed by execution)
 - Instrumentation, profiling
 - Dynamic versions of control-flow, etc.
 - Applications such as testing, debugging,
- Combinations of static and dynamic analyses

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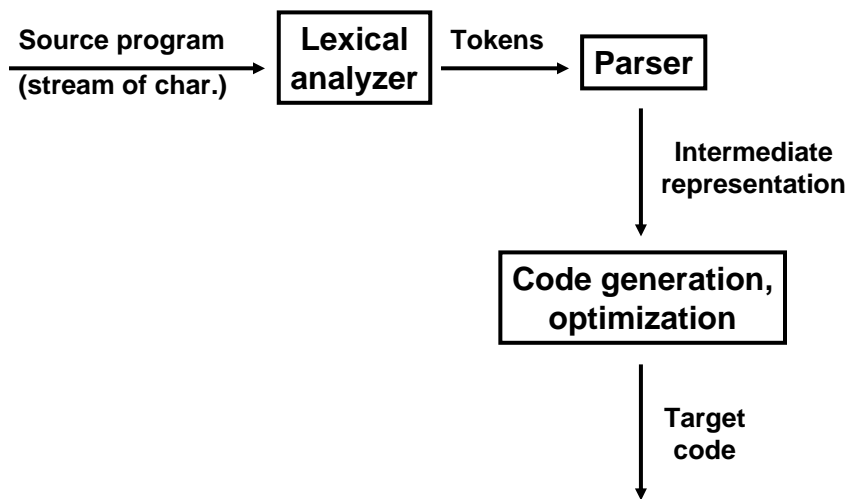
Overview of Course

- **Static analyses (computed without execution)**
 - Intraprocedural (within a single procedure)
 - AST, control-flow, control-dependence, data-flow, etc.
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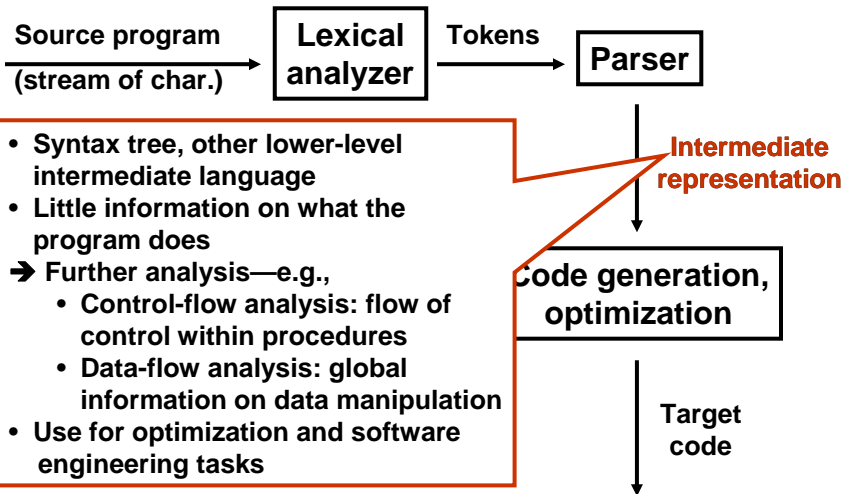
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Intermediate Representations

Intermediate Representations (traditional)

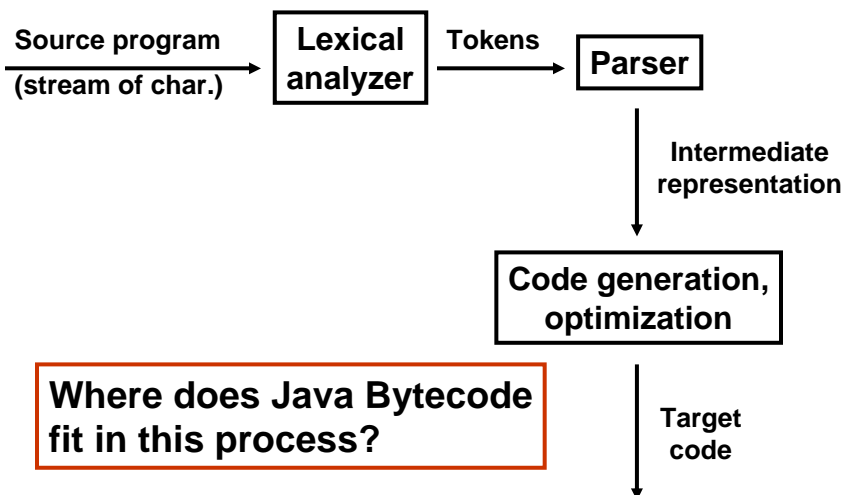


Intermediate Representations (traditional)



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Intermediate Representations (traditional)



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Abstract Syntax Tree (AST)

- **Concrete** versus **abstract** syntax
 - Concrete shows structure *and* is language-specific
 - Abstract shows structure
- Representations
 - **Parse tree** represents concrete syntax
 - **Abstract syntax tree** represents abstract syntax

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Example: Grammar

Examples

1. `a := b + c`
2. `a = b + c;`

Grammar for 1

- `stmtlist` \rightarrow `stmt` | `stmt stmtlist`
- `stmt` \rightarrow `assign` | `if-then` | ...
- `assign` \rightarrow `ident` `"="` `ident` `binop` `ident`
- `binop` \rightarrow `"+"` | `"-"` | ...

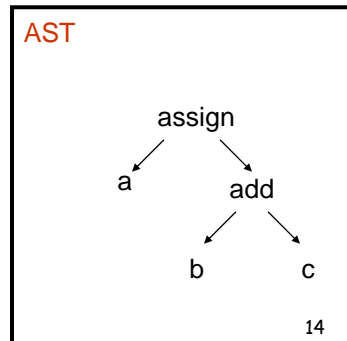
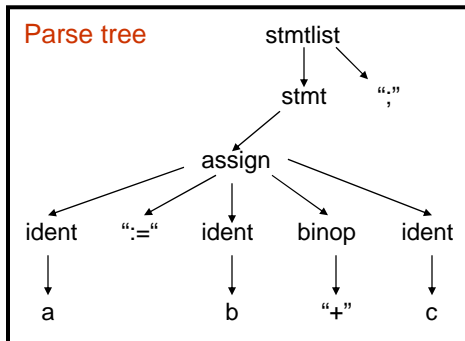
Grammar for 2

- `stmtlist` \rightarrow `stmt` `";"` | `stmt` `";"` `stmtlist`
- `stmt` \rightarrow `assign` | `if-then` | ...
- `assign` \rightarrow `ident` `"="` `ident` `binop` `ident`
- `binop` \rightarrow `"+"` | `"-"` | ...

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Example: Parse tree and AST

- Example: `a := b + c;`
- Grammar
 - `stmtlist -> stmt ";" | stmt ";" stmtlist`
 - `stmt -> assign | if-then | ...`
 - `assign -> ident ":" "=" ident binop ident`
 - `binop -> "+" | "-"`
 - ...



Three Address Code

- General form: `x := y op z`
- May include temporary variables (intermediate values)
- Types (examples; rest in handout)
 - Assignment
 - Binary `x := y op z`
 - Unary `x := op y`
 - Copy `x := y`
 - Jumps
 - Unconditional `goto L`
 - Conditional `if x relop y goto L`
 - ...

Example: Three Address Code

Source code

```
if a > 10 then
  x = y + z
else
  x = y - z
...
```

Corresponding 3-address code

- if a > 10 goto 4
- x = y - z
- goto 5
- x = y + z
- ...

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Analysis Levels

- **Local**: within a single basic block or statement
- **Global, Intraprocedural**: within a single procedure, function, or method (sometimes, intramethod)
- **Interprocedural**: across procedure boundaries, procedure call, shared globals, etc.
- **Intraclass**: within a single class
- **Interclass**: across class boundaries
- **Intramodule**: within a single module
- ...

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Control-flow Analysis

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Computing Control Flow

Procedure AVG

```
S1 count = 0
S2 fread(fptr, n)
S3 while (not EOF) do
S4   if (n < 0)
S5     return (error)
    else
S6     nums[count] = n
S7     count ++
    endif
S8   fread(fptr, n)
endwhile
S9 avg = mean(nums, count)
S10 return(avg)
```

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Computing Control Flow

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Control flow is a relation (i.e., set of ordered pairs)

- that represents the possible flow of execution in a program
- (a, b) in the relation means that control can flow from node a to node b during execution.

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Computing Control Flow

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What is the control-flow relation for Procedure AVG?

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Computing Control Flow

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- that represents the possible flow of execution in a program
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{(entry, S1), (S1, S2), (S2, S3), (S3, S4), (S3, S9), (S4, S5), (S5, exit), (S4, S6), (S6, S7), (S7, S8), (S8, S3), (S9, S10), (S10, exit)}

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Computing Control Flow

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Control-flow Graph (CFG) is a way to represent the control-flow relation:

- *nodes* represent elements in pairs (A,B)
- *edges* represent the relation between A and B
- *labels* represent the conditions that cause that branch to be executed
- *entry* and *exit* nodes added

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Computing Control Flow

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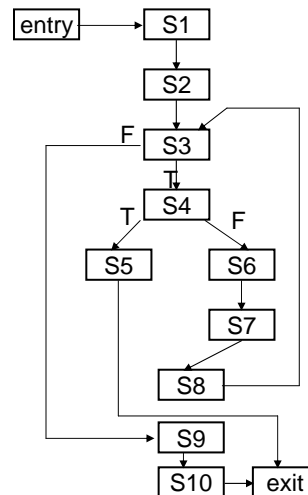
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Computing Control Flow

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Control Flow: Basic Blocks

- A **basic block** is a sequence of consecutive statements in which flow of control enters at the beginning and leaves at the end without halt or possibility of branch except at the end
- A basic block may or may not be maximal
- For compiler optimizations, maximal basic blocks are desirable
- For software engineering tasks, basic blocks that represent one source code statement are often used

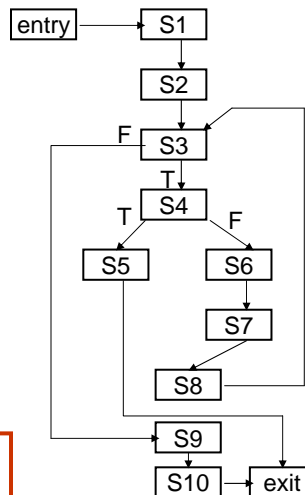
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CFG with Maximal Basic Blocks

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```

What are the maximal basic blocks for Procedure AVG?

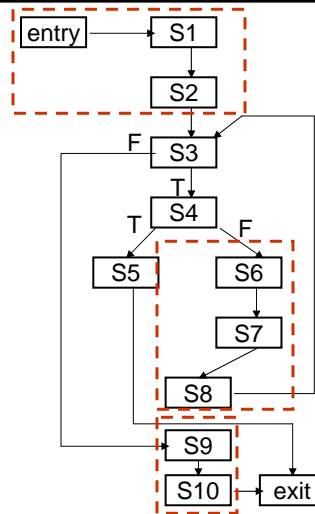


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CFG with Maximal Basic Blocks

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Computing Control Flow: Algorithm

- *Input:* a list of program statements in some form
- *Output:* A list of control-flow graph (CFG) nodes and edges
- *Method:*
 - Construct basic blocks **How?**
 - Create entry and exit nodes; create edge (entry, B1); create (Bk, exit) for each Bk that represents an exit from program
 - Add CFG edge from Bi to Bj if Bj can immediately follow Bi in some execution, i.e.,

How do we determine this?

- Label edges that represent conditional transfers of control

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Computing Control Flow: Algorithm

- *Input*: a list of program statements in some form
- *Output*: A list of control-flow graph (CFG) nodes and edges
- *Method*:
 - Construct basic blocks
 - Create entry and exit nodes; create edge (entry, B1); create (Bk, exit) for each Bk that represents an exit from program
 - Add CFG edge from Bi to Bj if Bj can immediately follow Bi in some execution, i.e.,
 - There is conditional or unconditional goto from last statement of Bi to first statement of Bj or
 - Bj immediately follows Bi in the order of the program and Bi does not end in an unconditional goto statement
 - Label edges that represent conditional transfers of control

What is the complexity of the algorithm, given n statements in the program?

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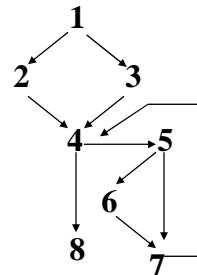
Control Flow Analysis: Terminology

- **CFG** = $\langle N, E \rangle$, rooted directed graph
 - N = set of nodes
 - $E \subseteq N \times N$ = set of edges, some labeled
 - *entry* $\in N$, *exit* $\in N$
- **Successors/predecessors** of a basic block
- **Branch node** is a node with two or more outgoing edges
- **Join node** is a node with two or more outgoing edges

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Applications of Control Flow

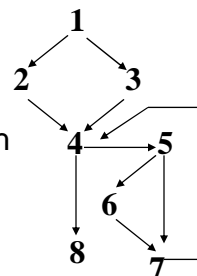
- **Program understanding**
 - program structure and flow is explicit
- **Complexity**
 - Cyclomatic (McCabe's)
 - Computed in several ways:
 - Edges – nodes + 2
 - Number of regions in CFG
 - Number of decision statements + 1 (if structured)
 - Indication of number of test case needed; indication of difficulty of maintaining



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Applications of Control Flow

- **Testing:** branch, path, basis path
 - Branch: must test 1→2, 1→3, 4→5, 4→8, 5→6, 5→7
 - Path: infinite number because of loop
 - Basis path: set of paths such that each path executes at least one more edge (cyclomatic complexity gives max necessary); example: 1,2,4,8; 1,3,4,5,6,7,4,8



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Search and Ordering

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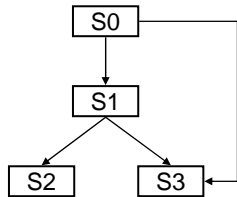
Some Useful Concepts

- **Depth-First Search (DFS):** Visits descendants before visiting siblings
- **Depth-first spanning tree:** All nodes, only edges traversed in the DFS
- **Depth-first presentation:** spanning tree + remaining edges (marked)
 - Forward edges: node \rightarrow direct descendant in the tree
 - Back edges: node \rightarrow ancestor in the tree
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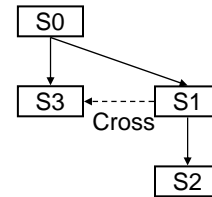
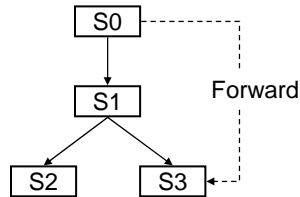
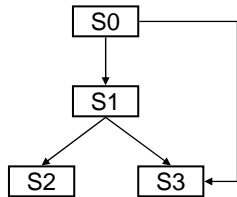


What are some depth-first spanning trees and presentations for this CFG?

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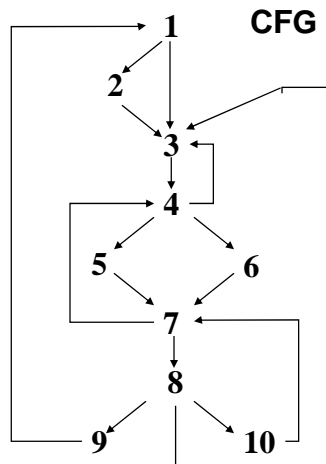
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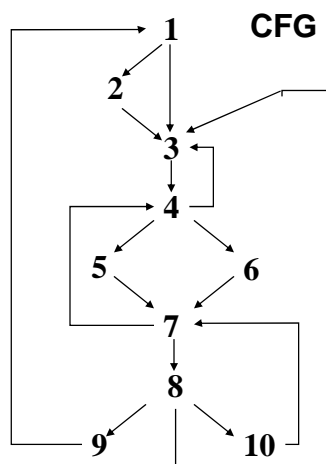
Search and Ordering (depth-first)



Show one depth-first presentation for the CFG?

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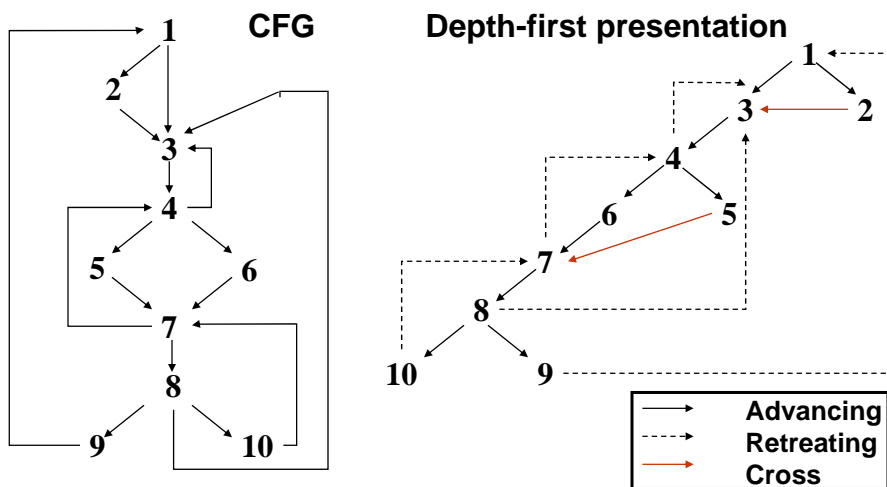
Search and Ordering (depth-first)



- One DFS of CFG is $1 \rightarrow 3 \rightarrow 4 \rightarrow 6 \rightarrow 7 \rightarrow 8 \rightarrow 10$, back to 8, $\rightarrow 9$, back to 8, 7, 6, 4, $\rightarrow 5$, back to 4, 1, 3, $\rightarrow 2$, back to 1
- **Depth-first ordering** of nodes is the reverse of the order in which nodes are visited in the DFS
- For the DFS, nodes are visited $1, 3, 4, 6, 7, 8, 10, 8, 9, 8, 7, 6, 4, 5, 4, 1, 3, 2, 1$
- Depth-first ordering is $1, 2, 3, 4, 5, 6, 7, 8, 9, 10$

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Search and Ordering (depth-first)

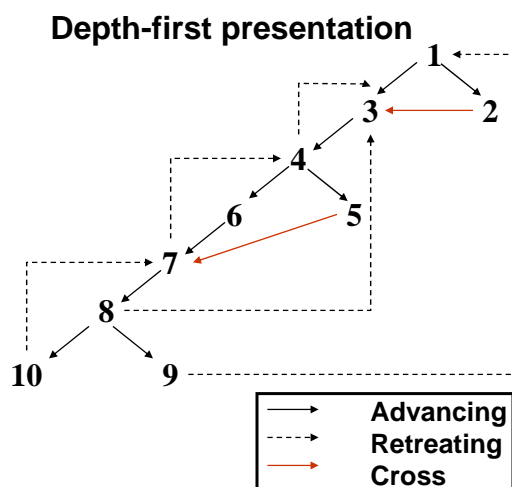


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Search and Ordering (depth-first)

Given a depth-first presentation of a CFG, the **depth of the CFG** is the greatest number of retreating edges on any cycle-free path

What is the depth of this CFG, given this presentation?

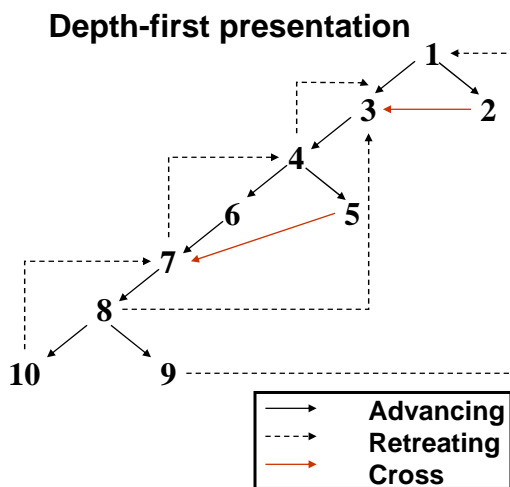


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Search and Ordering (depth-first)

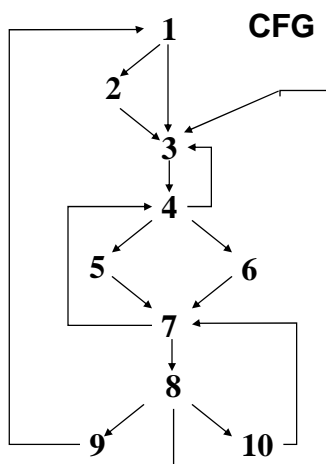
Given a depth-first presentation of a CFG, the **depth of the CFG** is the greatest number of retreating edges on any cycle-free path

There is a path $10 \rightarrow 7 \rightarrow 4 \rightarrow 3$ with three retreating edges; thus the depth of the CFG is 3



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Search and Ordering (depth-first)



For Thursday:

Is there a depth-first presentation with depth greater than 3?

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Some Useful Concepts

- **Preorder traversal (reverse postorder):** Traversal of the depth-first spanning tree in which each node is processed before its descendants
- **Postorder traversal:** Traversal of the depth-first spanning tree in which each node is processed after its descendants
- **Breadth-First Search (BFS):** All of a node's immediate descendants are processed before any of their unprocessed descendants
- **Breadth-first order:** Order imposed by a BFS

Search and ordering algorithms are review, and you are expected to know them.

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Dominance and Postdominance

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Dominators, Postdominators

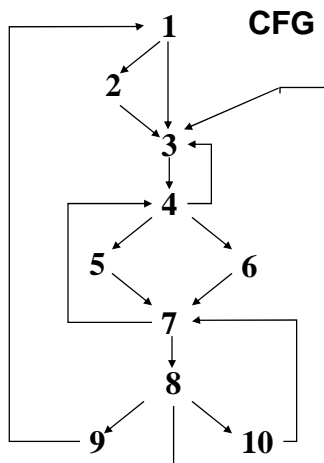
Given a CFG with nodes D and N, D **dominates** N if every path from the initial node to N goes through D

Properties of dominance

1. Every node dominates itself
2. Initial node dominates all others

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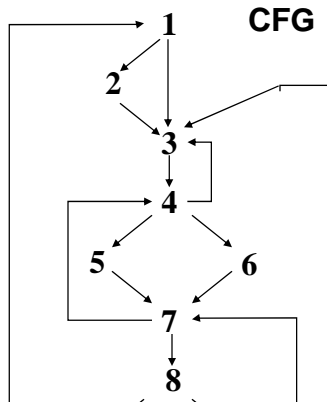
Dominators, Postdominators (example)



Node	Dominates
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	

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Dominators, Postdominators (example)

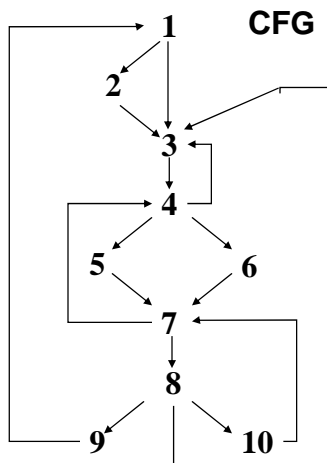


What are the dominators for nodes in the CFG?

Node	Dominates
1	
2	
3	
4	
5	
6	
7	
8	
9	
10	

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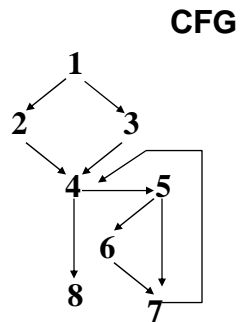
Dominators, Postdominators (example)



Node	Dominates
1	1,2,...,10
2	2
3	3,4,...,10
4	4,5,...,10
5	5
6	6
7	7,8,9,10
8	8,9,10
9	9
10	10

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Dominators, Postdominators (dominator properties)



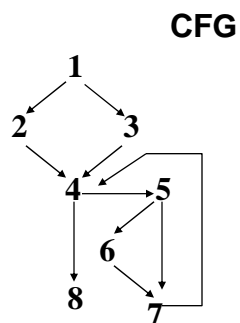
$a \text{ dom } b$ iff

- $a = b$ or
- a is the unique immediate predecessor of b or
- b has more than one predecessor and for all immediate predecessors c of b , a dominates c

dom is reflexive, transitive, and antisymmetric

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Dominators, Postdominators (dominator properties)



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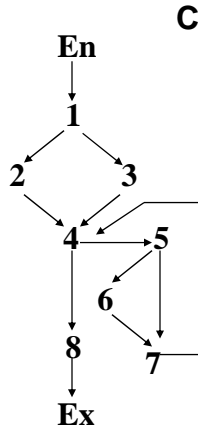
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What these properties mean for the dom relation?

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Dominators, Postdominators (dominator algorithm)

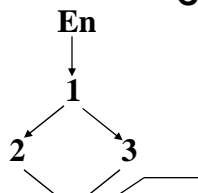


CFG Intuition for algorithm

- N is set of nodes in CFG with En , Ex
- initialize $domin(En)$ to $\{En\}$, $change$ to false
- Initialize $domin(n)$ to N for all $n \neq En$
- iterate over all n (except En) until no change in $domin$ sets
 - assign N to T
 - compute $domin(n)$ by first taking the intersection of T and $domin(p)$, for all p , a predecessor of n
 - then add n to T (this is new $domin(n)$)
- If $T \neq domin(n)$, a change has occurred
 - assign T to $domin(n)$
 - $change$ is true

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Dominators, Postdominators (dominator algorithm)



CFG Intuition for algorithm

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 - $change$ is true

For Thursday:

Show iterations of the algorithm over the nodes in the CFG until the result converges?

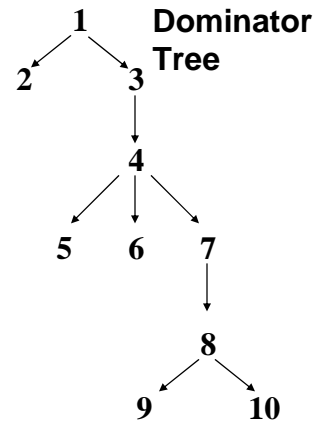
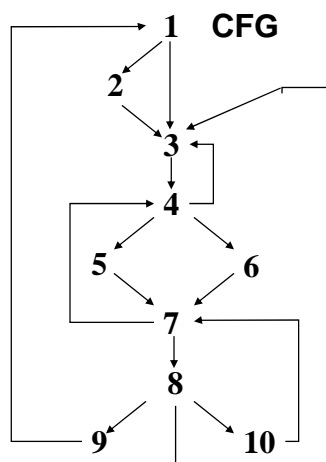
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Dominators, Postdominators (dominator tree)

- In a **dominator tree**
 - The initial node n is the root of the CFG
 - The parent of a node n is its *immediate dominator* (i.e., the last dominator of n on any path); the immediate dominator for n is unique

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Dominators, Postdominators (dominator tree)



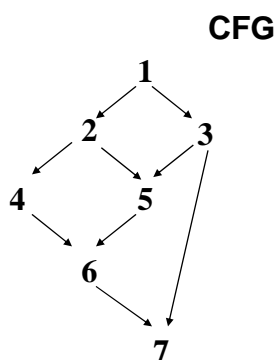
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Dominators, Postdominators

Given a CFG with nodes PD and N, PD **postdominates** N if every path from N to the final nodes goes through PD

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Dominators, Postdominators (example)



Node	Postdominates
1	--
2	--
3	--
4	--
5	--
6	2,4,5
7	1,2,...,6

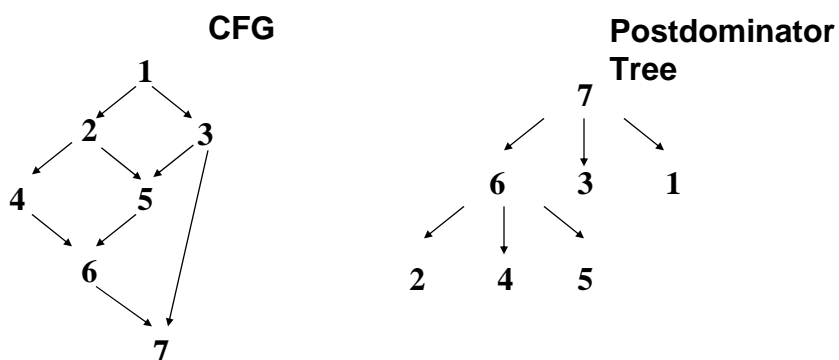
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Dominators, Postdominators (dominator tree)

- In a **postdominator tree**
 - The initial node n is the exit node of the CFG
 - The parent of a node n is its *immediate postdominator* (i.e., the first postdominator of n on any path); the immediate postdominator for n is unique

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Dominators, Postdominators (dominator tree)



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