

# Lecture 2: Relational Model

CREATING THE NEXT®

# Today's Agenda

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## Relational Model

- 1.1 Recap
- 1.2 External Sorting
- 1.3 Relational Model: Motivation
- 1.4 Relational Model
- 1.5 Relational Algebra

# Recap

# Motivational Example

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Designing a robust, scalable algorithm is hard:

- must cope with very large instances
- hard even when the database fits in main memory
- billions of data items
- rules out the possibility of using  $O(n^2)$  algorithms
- external algorithms (*i.e.*, database does not fit in memory) are even harder

This is why a DBMS is a complex software system.

# Hardware Trends

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This affects the design of a DBMS

- CPU costs are now more important
- I/O operations are eliminated or greatly reduced
- the classical architecture (disk-oriented database systems) has become suboptimal

But this is more of an evolution as opposed to a revolution. Many of the old techniques are still relevant for scalability.

# Problem Statement

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- Sorting an arbitrary amount of data, stored on disk
- Accessing data on disk is slow – so we do not want to access each value individually
- Sorting in main memory is fast – but main memory size is limited

# Solution

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- Partition the list into a set of smaller-sized **chunks** that fit in main memory
- and sort all the **chunks**
- Use `std::sort` as the internal sorting algorithm.
- With **m** values fitting into main memory and **n** values that should be sorted:
- number of runs (**k**) =  $\lceil \frac{n}{m} \rceil$  runs

## Iterative 2-Way Merge

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- Iteratively merging the first run with the second, the third with the fourth, and so on.
- As number of runs ( $k$ ) is halved in each iteration, there are only  $\Theta(\log_2 k)$  iterations.
- In each iteration every element is moved exactly once.
- So in each iteration, we read and write out all the input data.
- The running time per iteration is therefore in  $\Theta(n)$ .
- The total I/O cost is therefore in  $\Theta(n \log_2 k)$ .



# External Sorting

# K-Way Merge (1)

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Memory 

|   |   |   |
|---|---|---|
| - | - | - |
|---|---|---|

Disk 

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | 5 | 8 | 3 | 4 | 7 | 2 | 6 | 9 |
|---|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| - | - | - | - | - | - | - | - | - |
|---|---|---|---|---|---|---|---|---|

## K-Way Merge (2)

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Memory 

|   |   |   |
|---|---|---|
| 1 | 3 | 2 |
|---|---|---|

Disk 

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | 5 | 8 | 3 | 4 | 7 | 2 | 6 | 9 |
|---|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| - | - | - | - | - | - | - | - | - |
|---|---|---|---|---|---|---|---|---|

# K-Way Merge (3)

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Memory 

|   |   |   |
|---|---|---|
| - | 3 | 2 |
|---|---|---|

Disk 

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | 5 | 8 | 3 | 4 | 7 | 2 | 6 | 9 |
|---|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | - | - | - | - | - | - | - | - |
|---|---|---|---|---|---|---|---|---|

# K-Way Merge (4)

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Memory 

|   |   |   |
|---|---|---|
| 5 | 3 | 2 |
|---|---|---|

Disk 

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | 5 | 8 | 3 | 4 | 7 | 2 | 6 | 9 |
|---|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | - | - | - | - | - | - | - | - |
|---|---|---|---|---|---|---|---|---|

# K-Way Merge (5)

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Memory 

|   |   |   |
|---|---|---|
| 5 | 3 | - |
|---|---|---|

Disk 

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | 5 | 8 | 3 | 4 | 7 | 2 | 6 | 9 |
|---|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | 2 | - | - | - | - | - | - | - |
|---|---|---|---|---|---|---|---|---|

# K-Way Merge (6)

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Memory 

|   |   |   |
|---|---|---|
| 5 | 3 | 6 |
|---|---|---|

Disk 

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | 5 | 8 | 3 | 4 | 7 | 2 | 6 | 9 |
|---|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | 2 | - | - | - | - | - | - | - |
|---|---|---|---|---|---|---|---|---|

# K-Way Merge (7)

---

Memory 

|   |   |   |
|---|---|---|
| - | - | - |
|---|---|---|

Disk 

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | 5 | 8 | 3 | 4 | 7 | 2 | 6 | 9 |
|---|---|---|---|---|---|---|---|---|

|   |   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|---|
| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 |
|---|---|---|---|---|---|---|---|---|



## K-Way Merge (8)

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Fewer disk reads

- A straightforward implementation would scan all  $k$  runs to determine the minimum.
- This implementation results in a running time of  $\Theta(kn)$ .
- Although it would work, it is not efficient.

We can improve upon this by computing the smallest element faster.

- By using a heap, the smallest element can be determined in  $O(\log k)$  time.
- Use `std::priority_queue` (implemented as a heap)
- The resulting running times are therefore in  $O(n \log k)$ .

K-way merge might not fit in memory

- Fall back to regular 2-way merge for a few iterations

# Relational Model: Motivation

# Digital Music Store Application

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Consider an application that models a digital music store to keep track of artists and albums.

Things we need store:

- Information about Artists
- What Albums those Artists released

# Flat File Strawman (1)

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Store our database as comma-separated value (CSV) files that we manage in our own code.

- Use a separate file per entity
- The application has to parse the files each time they want to read/update records

## Flat File Strawman (2)

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|                    | <b>Artist</b> | <b>Year</b> | <b>City</b> |
|--------------------|---------------|-------------|-------------|
| <b>Artists.csv</b> | Mozart        | 1756        | Salzburg    |
|                    | Beethoven     | 1770        | Bonn        |
|                    | Chopin        | 1810        | Warsaw      |

|                   | <b>Album</b>            | <b>Artist</b> | <b>Year</b> |
|-------------------|-------------------------|---------------|-------------|
| <b>Albums.csv</b> | The Marriage of Figaro  | Mozart        | 1786        |
|                   | Requiem Mass In D minor | Mozart        | 1791        |
|                   | Für Elise               | Beethoven     | 1867        |

## Flat File Strawman (3)

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Example: Get the Albums composed by Beethoven.

```
for line in file:
    record = parse(line)
    if "Beethoven" == record[1]:
        print record[0]
```

|            | Album                   | Artist    | Year |
|------------|-------------------------|-----------|------|
| Albums.csv | The Marriage of Figaro  | Mozart    | 1786 |
|            | Requiem Mass In D minor | Mozart    | 1791 |
|            | Für Elise               | Beethoven | 1867 |

# Flat File Strawman (4)

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## Data Integrity

- How do we ensure that the artist is the same for each album entry?
- What if somebody overwrites the album year with an invalid string?
- How do we store that there are multiple artists on an album?

## Implementation

- How do you find a particular record?
- What if we now want to create a new application that uses the same database?
- What if two threads try to write to the same file at the same time?

## Durability

- What if the machine crashes while our program is updating a record?
- What if we want to replicate the database on multiple machines for high availability?

# Early DBMSs

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Limitations of early DBMSs (*e.g.*, IBM IMS FastPath in 1966)

- Database applications were difficult to build and maintain.
- Tight coupling between logical and physical layers.
- You have to (roughly) know what queries your app would execute before you deployed the database.



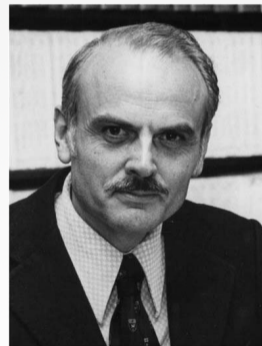
# Relational Model

# Relational Model

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Proposed in 1970 by Ted Codd (IBM Almaden).  
Data model to avoid this maintenance.

- Store database in simple data structures
- Access data through high-level language
- Physical storage left up to implementation



A handwritten signature in black ink, appearing to read "Ted Codd".

# Data Models

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A **data model** is collection of concepts for describing the data in a database.

A **schema** is a description of a particular collection of data, using a given data model.

## List of data models

- Relational (SQL-based, most DBMSs, focus of this course)
- Non-Relational (*a.k.a.*, NoSQL) models
  - ▶ Key/Value
  - ▶ Graph
  - ▶ Document
  - ▶ Column-family
- Array/Matrix (Machine learning)
- Obsolete models
  - ▶ Hierarchical/Tree

# Relation

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A relation is an unordered set of tuples. Each tuple represents an entity.

A tuple is a set of attribute values.

Values are (normally) atomic/scalar.

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| Artist    | Year | City     |
|-----------|------|----------|
| Mozart    | 1756 | Salzburg |
| Beethoven | 1770 | Bonn     |
| Chopin    | 1810 | Warsaw   |

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# Jargon

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- Relations are also referred to as **tables**.
- Tuples are also referred to as **records** or **rows**.
- Attributes are also referred to as **columns**.

# Relational Model: Definition

# Relational Model

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- **Structure:** The definition of relations and their contents.
- **Integrity:** Ensure the database's contents satisfy constraints.
- **Manipulation:** How to access and modify a database's contents.

## Structure: Primary Key

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- A relation's **primary key** uniquely identifies a single tuple.
- Some DBMSs automatically create an internal primary key if you don't define one.
- Auto-generation of unique integer primary keys (SEQUENCE in SQL:2003)

Schema: **Artists** (ID, Artist, Year, City)

| ID | Artist | Year     | City |
|----|--------|----------|------|
| 1  | 1756   | Salzburg |      |
| 2  | 1770   | Bonn     |      |
| 3  | 1810   | Warsaw   |      |



## Structure: Foreign Key (1)

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- A foreign key specifies that an tuple from one relation must map to a tuple in another relation.
- Mapping artists to albums?

## Structure: Foreign Key (2)

Artists (ID, Artist, Year, City)

Albums (ID, Album, Artist\_ID, Year)

|         | <u>ID</u> | Artist    | Year | City     |
|---------|-----------|-----------|------|----------|
| Artists | 1         | Mozart    | 1756 | Salzburg |
|         | 2         | Beethoven | 1770 | Bonn     |
|         | 3         | Chopin    | 1810 | Warsaw   |

|        | <u>ID</u> | Album                   | Artist_ID | Year |
|--------|-----------|-------------------------|-----------|------|
| Albums | 1         | The Marriage of Figaro  | 1         | 1786 |
|        | 2         | Requiem Mass In D minor | 1         | 1791 |
|        | 3         | Für Elise               | 2         | 1867 |

## Structure: Foreign Key (3)

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What if an album is composed by two artists?

What if an artist composed two albums?

## Structure: Foreign Key (3)

---

What if an album is composed by two artists?

What if an artist composed two albums?

**Artists** (ID, Artist, Year, City)

**Albums** (ID, Album, Year)

**ArtistAlbum** (Artist\_ID, Album\_ID)

|                    | <u>Artist_ID</u> | <u>Album_ID</u> |
|--------------------|------------------|-----------------|
| <b>ArtistAlbum</b> | 1                | 1               |
|                    | 2                | 1               |
|                    | 2                | 2               |

# Data Manipulation Languages

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How to store and retrieve information from a database.

- **Relational Algebra**

- ▶ The query specifies the (high-level) strategy the DBMS should use to find the desired result.
- ▶ Procedural

- **Relational Calculus**

- ▶ The query specifies only what data is wanted and not how to find it.
- ▶ Non-Procedural

# Relational Algebra

# Core Operators

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- These operators take in relations (*i.e.*, tables) as input and return a relation as output.
- We can “chain” operators together to create more complex operations.
  
- Selection ( $\sigma$ )
- Projection ( $\Pi$ )
- Union ( $\cup$ )
- Intersection ( $\cap$ )
- Difference ( $-$ )
- Product ( $\times$ )
- Join ( $\bowtie$ )

# XKCD



Source: <https://xkcd.com/327/>



# Core Operators: Selection

- Choose a subset of the tuples from a relation that satisfies a selection predicate.
- Predicate acts as a filter to retain only tuples that fulfill its qualifying requirement.
- Can combine multiple predicates using conjunctions / disjunctions.
- Syntax:  $\sigma_{\text{predicate}}(\mathbf{R})$

```
SELECT * FROM R WHERE a_id = 'a2' AND b_id > 102;
```

**R**

| a_id | b_id |
|------|------|
| a1   | 101  |
| a2   | 102  |
| a2   | 103  |
| a3   | 104  |

$\sigma_{a\_id='a2' \wedge b\_id > 102}(\mathbf{R}) :$

| a_id | b_id |
|------|------|
| a2   | 103  |

# Core Operators: Projection

- Generate a relation with tuples that contains only the specified attributes.
- Can rearrange attributes' ordering.
- Can manipulate the values.
- Syntax:  $\Pi_{A_1, A_2, \dots, A_n}(\mathbf{R})$

`SELECT b_id - 100, a_id FROM R WHERE a_id = 'a2';`

**R**

| a_id | b_id |
|------|------|
| a1   | 101  |
| a2   | 102  |
| a2   | 103  |
| a3   | 104  |

$\Pi_{b\_id-100, a\_id}(\sigma_{a\_id='a2'}(\mathbf{R})) :$

| b_id - 100 | a_id |
|------------|------|
| 2          | 103  |
| 3          | 103  |

# Core Operators: Union

- Generate a relation that contains all tuples that appear in either only one or both input relations.
- Syntax:  $R \cup S$

```
(SELECT * FROM R)
  UNION ALL
(SELECT * FROM S)
```

| R    |      |
|------|------|
| a_id | b_id |
| a1   | 101  |
| a2   | 102  |
| a3   | 103  |

| S    |      |
|------|------|
| a_id | b_id |
| a3   | 103  |
| a4   | 104  |
| a5   | 105  |

$R \cup S$

| a_id | b_id |
|------|------|
| a1   | 101  |
| a2   | 102  |
| a3   | 103  |
| a3   | 103  |
| a4   | 104  |
| a5   | 105  |

# Semantics of Relational Operators

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Set semantics: Duplicates tuples are **not** allowed

Bag semantics: Duplicates tuples are allowed

We will assume **bag (a.k.a., multi-set)** semantics.

# Core Operators: Intersection

- Generate a relation that contains only the tuples that appear in both of the input relations.
- Syntax:  $R \cap S$

```
(SELECT * FROM R)
INTERSECT
(SELECT * FROM S)
```

| R    |      | S    |      |
|------|------|------|------|
| a_id | b_id | a_id | b_id |
| a1   | 101  | a3   | 103  |
| a2   | 102  | a4   | 104  |
| a3   | 103  | a5   | 105  |

$R \cap S$

| a_id | b_id |
|------|------|
| a3   | 103  |

# Core Operators: Difference

- Generate a relation that contains only the tuples that appear in the first and not the second of the input relations.
- Syntax:  $R - S$

```
(SELECT * FROM R)
EXCEPT
(SELECT * FROM S)
```

| <b>R</b>                | <b>S</b>                |  | <b>R - S</b>            |
|-------------------------|-------------------------|--|-------------------------|
| <u>a_id</u> <u>b_id</u> | <u>a_id</u> <u>b_id</u> |  | <u>a_id</u> <u>b_id</u> |
| a1   101                | a3   103                |  | a1   101                |
| a2   102                | a4   104                |  | a2   102                |
| a3   103                | a5   105                |  |                         |

# Core Operators: Product

- Generate a relation that contains all possible combinations of tuples from the input relations.
- Syntax:  $\mathbf{R} \times \mathbf{S}$

`SELECT * FROM R CROSS JOIN S`

| <b>R</b> |      |
|----------|------|
| a_id     | b_id |
| a1       | 101  |
| a2       | 102  |
| a3       | 103  |

| <b>S</b> |      |
|----------|------|
| a_id     | b_id |
| a3       | 103  |
| a4       | 104  |
| a5       | 105  |

$\mathbf{R} \times \mathbf{S}$

| R.a_id | R.b_id | S.a_id | S.b_id |
|--------|--------|--------|--------|
| a1     | 101    | a3     | 103    |
| a1     | 101    | a4     | 104    |
| a1     | 101    | a5     | 105    |
| a2     | 102    | a3     | 103    |
| a2     | 102    | a4     | 104    |
| a2     | 102    | a5     | 105    |
| a3     | 103    | a3     | 103    |
| a3     | 103    | a4     | 104    |
| a3     | 103    | a5     | 105    |

# Core Operators: Join

- Generate a relation that contains all tuples that are a combination of two tuples (one from each input relation) with a common value(s) for one or more attributes.
- Syntax:  $R \bowtie S$

`SELECT * FROM R NATURAL JOIN S`

| R    |      |
|------|------|
| a_id | b_id |
| a1   | 101  |
| a2   | 102  |
| a3   | 103  |

| S    |      |
|------|------|
| a_id | b_id |
| a3   | 103  |
| a4   | 104  |
| a5   | 105  |

$R \bowtie S$

| $R \bowtie S$ |      |
|---------------|------|
| a_id          | b_id |
| a3            | 103  |



# Derived Operators

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Additional (derived) operators are often useful:

- Rename ( $\rho$ )
- Assignment ( $R \leftarrow S$ )
- Duplicate Elimination ( $\delta$ )
- Aggregation ( $\gamma$ )
- Sorting ( $\tau$ )
- Division ( $R \div S$ )

# Observation

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Relational algebra still defines the high-level steps of how to execute a query.

- $\sigma_{b\_id=102}(\mathbf{R} \bowtie \mathbf{S})$  versus
- $(\mathbf{R} \bowtie \sigma_{b\_id=102}(\mathbf{S}))$

A better approach is to state the high-level answer that you want the DBMS to compute.

- Retrieve the joined tuples from  $\mathbf{R}$  and  $\mathbf{S}$  where  $b\_id$  equals 102.

# Relational Model

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The relational model is independent of any query language implementation. However, SQL is the **de facto** standard.

Example: Get the Albums composed by Beethoven.

```
for line in file:
    record = parse(line)
    if "Beethoven" == record[1]:
        print record[0]
```

```
SELECT Year
FROM Artists
WHERE Artist = "Beethoven"
```

# Set-Oriented Processing

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Small applications often loop over their data

- one for loop accesses all item  $x$ ,
- for each item, another loop access item  $y$ ,
- then both items are combined.

This kind of code of code feels “natural”, but is bad

- $\Omega(n^2)$  runtime
- does not scale

Instead: **set oriented** processing. Perform operations for large batches of data.

## Set-Oriented Processing (2)

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Processing whole batches of tuples is more efficient:

- can prepare index structures
- or re-organize the data
- sorting/hashing
- runtime ideally  $O(n \log n)$

Many different algorithms, we will look at them later.

# Conclusion

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- External sorting allows us to sort larger-than-memory datasets
- Relational algebra defines the primitives for processing queries on a relational database.
- We will see relational algebra again when we talk about query execution.
- In the next lecture, we will learn about advanced SQL.