B+Tree In Practice

B+Tree Design Decisions

timizations

Conclusion 00



Lecture 14: Trees (Part I)

CREATING THE NEXT[®]

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- Assignment 3 due on Oct 24
- Exam Max Score: 175 for 6422, 120 for 4420



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Today's Agenda

Recap

B+Tree Overview

B+Tree In Practice

B+Tree Design Decisions

Optimizations

Conclusion







	Hash Tables				
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- Hash tables are fast data structures that support O(1) look-ups
- Used all throughout the DBMS internals.
 - Examples: Page Table (Buffer Manager), Lock Table (Lock Manager)
- Trade-off between speed and flexibility.



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Limitations of Hash Tables

- Hash tables are usually **not** what you want to use for a indexing tables
 - Lack of ordering in widely-used hashing schemes
 - ► Lack of locality of reference → more disk seeks
 - Persistent data structures are much more complex (logging and recovery)
 - Reference



т	able Indexes				
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- A **<u>table index</u>** is a replica of a subset of a table's attributes that are organized and/or sorted for efficient access based a subset of those attributes.
- Example: {**Employee Id**, **Dept Id**} \longrightarrow Employee Tuple Pointer
- The DBMS ensures that the contents of <u>the table</u> and <u>the indices</u> are in sync.



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Г	Table Indexes				

- It is the DBMS's job to figure out the best index(es) to use to execute each query.
- There is a trade-off on the number of indexes to create per database.
 - Storage Overhead
 - Maintenance Overhead



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То	day's Agenda				

- B+Tree Overview
- B+Tree in Practice
- Design Decisions
- Optimizations



B Tree Overview

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I	B-Tree Family				

- There is a specific data structure called a B-Tree.
- People also use the term to generally refer to a class of balanced tree data structures:
 - ► <u>**B-Tree**</u> (1971)
 - ► <u>**B**+Tree</u> (1973)
 - ► <u>**B*Tree**</u> (1977?)
 - Blink-Tree (1981)



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В	8+Tree				

- A <u>**B**+Tree</u> is a self-balancing tree data structure that keeps data sorted and allows searches, sequential access, insertions, and deletions in **O(log n)**.
 - Generalization of a **binary search tree** in that a node can have more than two children.
 - Optimized for disk storage (*i.e.*, read and write at page-granularity).



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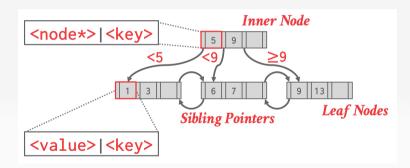
B+Tree Properties

- A B+Tree is an **M-way** search tree with the following properties:
 - It is perfectly balanced (*i.e.*, every leaf node is at the same depth).
 - ► Every node other than the root, is <u>at least half-full</u>: M/2-1 <= keys <= M-1
 - Every inner node with k keys has k+1 non-null children (**node pointers**)



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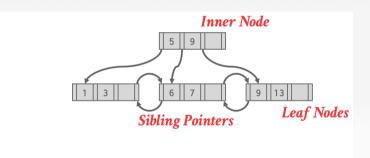
B+Tree Example







B+Tree Example



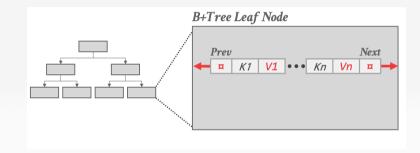


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ľ	Nodes				

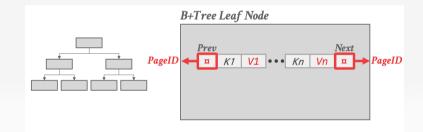
- Every B+Tree node is comprised of an **array** of key/value pairs.
 - ▶ The **keys** are derived from the attributes(s) that the index is based on.
 - The <u>values</u> will differ based on whether the node is classified as inner nodes or leaf nodes.
 - Inner nodes: Values are pointers to other nodes.
 - Leaf nodes: Values are pointers to tuples or actual tuple data.
- The arrays are (usually) kept in sorted key order.



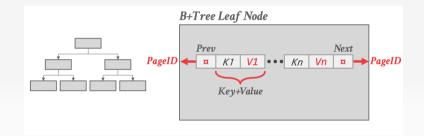
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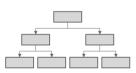








B+Tree Design Decisions









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N	lode				

```
struct Node {
    /// The level in the tree.
    uint16_t level;
    /// The number of children.
    uint16_t count;
    ~~I...
};
```

```
void print_node(Node *node);
```



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Ν	lode				



I	eaf Node Values				
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- Approach 1: Record Ids
 - A pointer to the location of the tuple that the index entry corresponds to.
- Approach 2: Tuple Data
 - The actual contents of the tuple is stored in the leaf node.
 - Secondary indexes typically store the record id as their values.



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В	-Tree vs. B+Tree				

- The original B-Tree from 1972 stored keys + values in all nodes in the tree.
 - More space efficient since each key only appears once in the tree.
- A B+Tree only stores values in leaf nodes.
- Inner nodes only guide the search process.
- Easier to support concurrent index access when only values are stored in leaf nodes



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B+Tree: Insert

- Find correct leaf node L.Put data entry into L in sorted order. ٠
- If L has enough space, done!
- Otherwise, split L keys into L and a new node L2
 - Redistribute entries evenly, copy up middle key.
 - Insert index entry pointing to L2 into parent of L.
- To split inner node, redistribute entries evenly, but push up middle key.
- Splits help grow the tree by one level





B+Tree Design Decisions

- Demo
- Source: David Gales (Univ. of San Francisco)



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I	B+Tree: Delete				

- Start at root, find leaf L where entry belongs.
- Remove the entry.
- If L is at least half-full, done! If L has only M/2-1 entries,
 - > Try to re-distribute, borrowing from sibling (adjacent node with same parent as L).
 - ► If re-distribution fails, merge L and sibling.
- If merge occurred, must delete entry (pointing to L or sibling) from parent of L.



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B Tree In Practice

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B+Tree Statistics

- Typical Fill-Factor: 67
- Pages per level:
 - ► Level 1 = 1 page = 8 KB
 - ► Level 2 = 134 pages = 1 MB
 - ► Level 3 = 17,956 pages = 140 MB



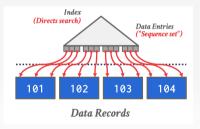
Data Organization

- A table can be stored in two ways:
 - Heap-organized storage: Organizing rows in no particular order.
 - Index-organized storage: Organizing rows in primary key order.
- Types of indexes:
 - **<u>Clustered index</u>**: Organizing rows in a **primary key order**.
 - Unclustered index: Organizing rows in a secondary key order.



Clustered Index

- Tuples are kept sorted on disk using the order specified by **primary key**.
- If the query accesses tuples using the clustering index's attributes, then the DBMS can jump directly to the pages that it needs.
- Traverse to the left-most leaf page, and then retrieve tuples from all leaf pages.

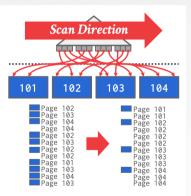




B+Tree Design Decisions

Unclustered Index

- Retrieving tuples in the order that appear in an unclustered index is inefficient.
- The DBMS can first figure out all the tuples that it needs and then sort them based on their page id.





Clustered vs. Unclustered Index

- Clustered index
 - Only one clustered index per table
 - ► Example: {**Employee Id**} → **Employee Tuple Pointer**
- Unclustered index
 - Multiple unclustered indices per table
 - ► Example: {Employee City} → Clustered Index Pointer or Employee Tuple Pointer
 - Accessing data through a non-clustered index may need to go through an extra layer of indirection



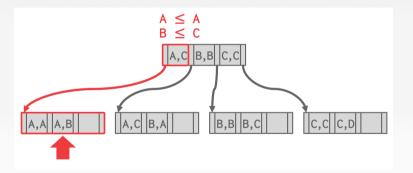
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- The DBMS can use a B+Tree index if the filter uses any of the attributes of the key.
- Example: Index on **<a,b,c>**
 - Supported: (a=5 AND b=3)
 - ► Supported: (b=3).
- For hash index, we must have **<u>all attributes</u>** in search key.



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Filtering Tuples

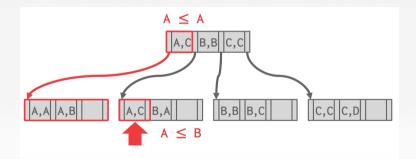


Find Key=(A,B)



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Filtering Tuples



Find Key=(A,*)



B+Tree Design Decisions

- Node Size
- Merge Threshold
- Variable Length Keys
- Non-Unique Indexes
- Intra-Node Search
- Modern B-Tree Techniques



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N	lode Size				

- The slower the storage device, the larger the optimal node size for a B+Tree.
 - ► HDD ~ 1 MB
 - ► SSD: ~10 KB
 - ► In-Memory: ~512 B
- · Optimal sizes varies depending on the workload
 - Leaf Node Scans (OLAP) vs. Root-to-Leaf Traversals (OLTP)



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N	Jerge Threshold				

Merge Threshold

- Some DBMSs do not always merge nodes when it is half full.
- Delaying a merge operation may reduce the amount of reorganization.
- It may also be better to just let **<u>underflows</u>** to exist and then periodically <u>**rebuild**</u> entire tree.



Variable Length Keys

Approach 1: Pointers

Store the keys as pointers to the tuple's attribute.

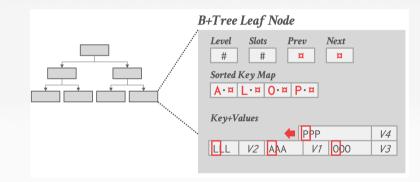
• Approach 2: Variable Length Nodes

- The size of each node in the index can vary.
- Requires careful memory management.
- Approach 3: Padding
 - Always pad the key to be max length of the key type.
- Approach 4: Key Map / Indirection
 - Embed an array of pointers that map to the key + value list within the node.



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Variable Length Keys: Key Map





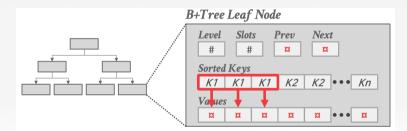
Non-Unique Indexes

- Approach 1: Duplicate Keys
 - Use the same leaf node layout but store duplicate keys multiple times.
- Approach 2: Value Lists
 - Store each key only once and maintain a linked list of unique values.



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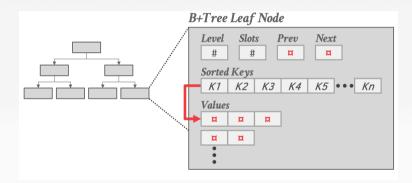
Non-Unique Indexes: Duplicate Keys





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Non-Unique Indexes: Value Lists



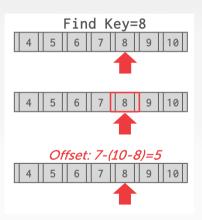


Intra-Node Search

- Approach 1: Linear Search
 - Scan node keys from beginning to end.
- Approach 2: Binary Search
 - Jump to middle key, pivot left/right depending on comparison.

Approach 3: Interpolation Search

 Approximate location of desired key based on known distribution of keys.





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Intra-Node Search

```
struct InnerNode: public Node {
   std::pair<uint32_t, bool> lower_bound(const KeyT &key) {
      /// Set lower and upper bounds for binary search
      uint16_t l = 0;
      uint16_t h = this->count - 2;
   }
~I...
};
```



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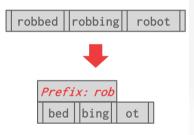
Optimizations

- Prefix Compression
- Suffix Truncation
- Bulk Insert
- Pointer Swizzling



Prefix Compression

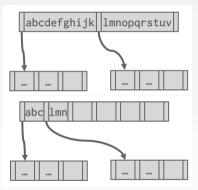
- Sorted keys in the same leaf node are likely to have the same prefix.
- Instead of storing the entire key each time, extract common prefix and store only unique suffix for each key.
 - Many variations.





Suffix Truncation

- The keys in the inner nodes are only used to "direct traffic".
 - We don't need the entire key.
- Store a minimum prefix that is needed to correctly route probes into the index.





Bulk Insert

• The fastest/best way to build a B+Tree is to first sort the keys and then build the index from the bottom up.

Keys: 3, 7, 9, 13, 6, 1 Sorted Keys: 1, 3, 6, 7, 9, 13

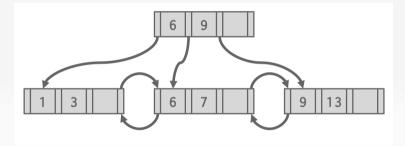


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E	Bulk Insert				





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Bu	lk Insert				





Pointer Swizzling

- Nodes use **page ids** to reference other nodes in the index.
- The DBMS must get the memory location from the page table during traversal.
- If a page is pinned in the buffer pool, then we can store **raw pointers** instead of page ids.
- This avoids address lookups from the page table.

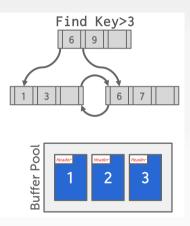


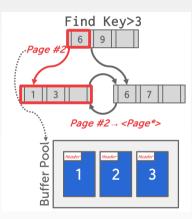
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Pointer Swizzling







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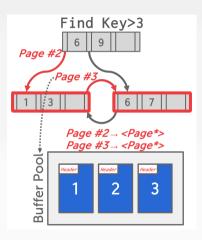
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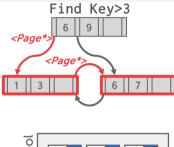
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Pointer Swizzling









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С	onclusion				

- The venerable B+Tree is always a good choice for your DBMS.
- Next Class
 - More B+Trees
 - Tries / Radix Trees
 - Inverted Indexes

