Additional Index Magic

nverted Index

Conclusion 00



# Lecture 15: Trees (Part 2)

CREATING THE NEXT°

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- Project presentations in class next week
- Assignment 3 due on Oct 24



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Recap

More B+Trees

Additional Index Magic

Tries / Radix Trees

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Conclusion







- A <u>**B**+Tree</u> is a self-balancing tree data structure that keeps data sorted and allows searches, sequential access, insertions, and deletions in **O(log n)**.
  - Generalization of a **binary search tree** in that a node can have more than two children.
  - Optimized for disk storage (*i.e.*, read and write at page-granularity).



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#### **B+Tree Properties**

- A B+Tree is an **M-way** search tree with the following properties:
  - It is perfectly balanced (*i.e.*, every leaf node is at the same depth).
  - ► Every node other than the root, is <u>at least half-full</u>: M/2-1 <= keys <= M-1
  - Every inner node with k keys has k+1 non-null children (node pointers)



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- More B+Trees
- Additional Index Magic
- Tries / Radix Trees
- Inverted Indexes



# **More B Trees**

## **Duplicate Keys**

#### Approach 1: Append Record Id

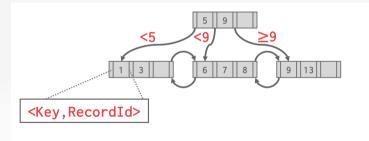
- Add the tuple's unique record id as part of the key to ensure that all keys are unique.
- The DBMS can still use partial keys to find tuples.

#### Approach 2: Overflow Leaf Nodes

- Allow leaf nodes to spill into overflow nodes that contain the duplicate keys.
- This is more complex to maintain and modify.



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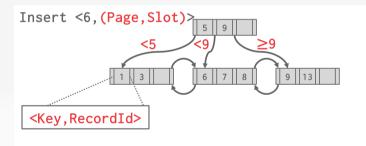


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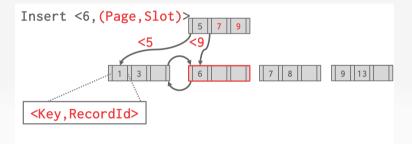
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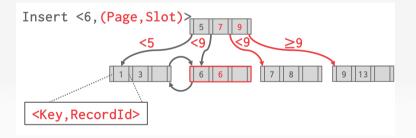


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## **Duplicate Keys**

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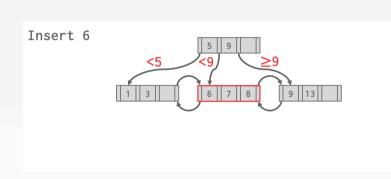
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#### **Overflow Leaf Nodes**

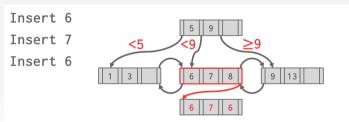




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#### **Overflow Leaf Nodes**





Bulk operations are fine if they are rare, but they are disruptive

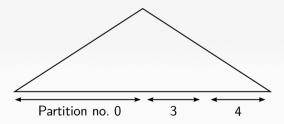
- usually the B-tree has to be take offline
- the new cannot be queries easily
- existing queries must be halted



#### **Partitioned B-Tree**

Basic idea: *partition* the B-tree

- add an artificial column in front
- creates separate partitions with the B-tree





### **Partitioned B-Tree**

Benefits:

- partitions are largely independent of each other
- one can append to the "rightmost" partition without disrupting the rest
- the index stays always online
- partitions can be merged lazily
- merge only when beneficial

Drawbacks:

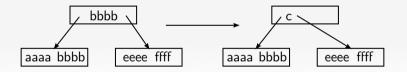
- no "global" order any more
- lookups have to access all partitions



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	Prefix B <sup>+</sup> -tree				

A B<sup>+</sup>-tree can contain separators that do not occur in the data

We can use this to save space:



- choose the smallest possible separator
- no change to the lookup logic is required



More B+Trees	Additional Index Magic 0000000	Tries / Radix Trees 00000000000000000000000000000000000	Inverted Index 0000000

#### Prefix B<sup>+</sup>-tree

We can do even better by factoring out a common prefix:



- only one prefix per page
- the change to the lookup logic is minor
- the lookup key itself is adjusted
- sometimes only inner nodes, to keep scans cheap



The lexicographic sort order makes prefix compression attractive:

- neighboring entries tend to differ only at the end
- a common prefix occurs very frequently
- not only for strings, also for compound keys etc.
- in particular important if partitioned B-trees
- with big-endian ordering any value might get compressed



# **Additional Index Magic**

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      Recap
      More B+Trees
      Additional Index Magic
      Tries / Radix Trees
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- Most DBMSs automatically create an index to enforce integrity constraints.
  - Primary Keys
  - Unique Constraints

```
CREATE TABLE foo (

id SERIAL PRIMARY KEY,

val1 INT NOT NULL,

val2 VARCHAR(32) UNIQUE

);

CREATE UNIQUE INDEX foo_pkey ON foo (id);

CREATE UNIQUE INDEX foo_val2_key ON foo (val2);
```



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But, this is <u>not</u> done for <u>referential</u> integrity constraints (i.e., foreign keys).
CREATE TABLE bar (
id INT REFERENCES foo (val1),
val VARCHAR(32)
);
CREATE INDEX foo val1 key ON foo (val1); -- Not automatically done
```



- Create an index on a subset of the entire table.
- This potentially reduces its size and the amount of overhead to maintain it.
- One common use case is to partition indexes by date ranges.
  - Create a separate index per month, year.

```
CREATE INDEX idx_foo ON foo (a, b)
```

WHERE c = 'October';

SELECT b FROM foo WHERE a = 123 AND c = 'October';



• If all the fields needed to process the query are available in an index, then the DBMS does **not** need to retrieve the tuple from the heap.

• This reduces contention on the DBMS's buffer pool resources. CREATE INDEX idx\_foo ON foo (a, b); SELECT b FROM foo WHERE a = 123;



#### **Index Include Columns**

- Embed additional columns in indexes to support index-only queries.
- These extra columns are only stored in the leaf nodes and are <u>**not**</u> part of the search key.

CREATE INDEX idx\_foo ON foo (a, b) INCLUDE (c);

SELECT b FROM foo WHERE a = 123 AND c = 'October';



### **Functional/Expression Indexes**

- An index does not need to store keys in the same way that they appear in their base table.
- You can use functions/expressions when declaring an index.

SELECT \* FROM users WHERE EXTRACT(dow FROM login) = 2; CREATE INDEX idx\_user\_login ON users (login);



### **Functional/Expression Indexes**

• An index does not need to store keys in the same way that they appear in their base table.

• You can use functions/expressions when declaring an index. CREATE INDEX idx\_user\_login ON users (EXTRACT(dow FROM login)); CREATE INDEX idx\_user\_login ON foo (login) WHERE EXTRACT(dow FROM login) = 2;



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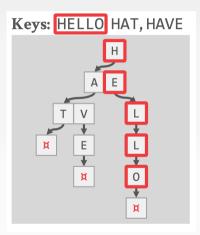
# **Tries / Radix Trees**

- The inner node keys in a B+Tree cannot tell you whether a key exists in the index.
- You must always traverse to the leaf node.
- This means that you could have (at least) one buffer pool page miss per level in the tree just to find out a key does not exist.



### Trie Index

- Use a **digital representation** of keys to examine prefixes one-by-one instead of comparing entire key.
  - *a.k.a.*, Digital Search Tree, Prefix Tree.





## Properties

- Shape only depends on key space and lengths.
  - Does not depend on existing keys or insertion order.
  - Does not require rebalancing operations.
- All operations have O(k) complexity where  $\underline{k}$  is the length of the key.
  - The path to a leaf node represents the key of the leaf
  - Keys are stored implicitly and can be reconstructed from paths.



## Key Span

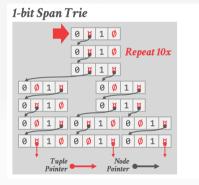
- The **span** of a trie level is the number of bits that each partial key / digit represents.
  - If the digit exists in the corpus, then store a pointer to the next level in the trie branch.
  - Otherwise, store null.
- This determines the <u>fan-out</u> of each node and the **physical height** of the tree.



## Key Span

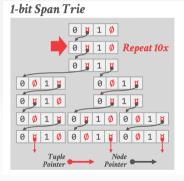
<b>K10</b> → 00000000 0000101
<b>K25</b> → 00000000 0001100
<b>K31</b> → 00000000 0001111







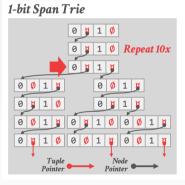




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K10→	00000000	00001010
K25→	00000000	00011001
K31→	00000000	00011111

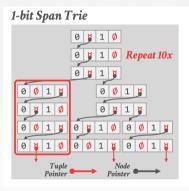


## Key Span



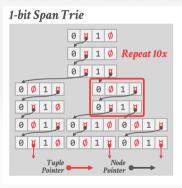
**K10**→ 00000000 00001010 **K25**→ 00000000 00011001 **K31**→ 0000000 00011111





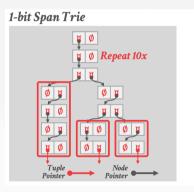
K10→	00000000	0000 <mark>1010</mark>
K25→	00000000	00011001
K31→	00000000	00011111





<b>K10</b> → 00000000	00001010
K25→ 00000000 K31→ 00000000	0001 <mark>10</mark> 01
<b>K31</b> → 00000000	0001 <mark>11</mark> 11



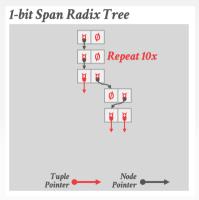


K10→	00000000	00001010
K25→	00000000	00011001
K31→	00000000	00011111



## **Radix** Tree

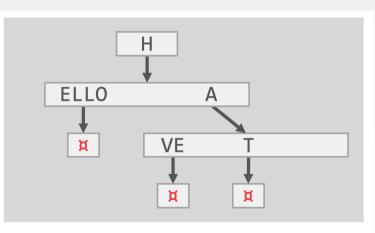
- Omit all nodes with **only** a single child.
  - ▶ a.k.a., Patricia Tree.
- Can produce false positives
- So the DBMS always checks the original tuple to see whether a key matches.





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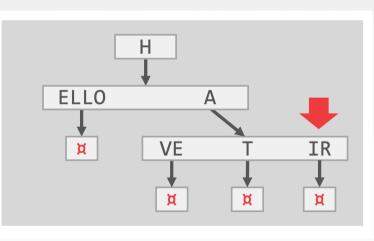




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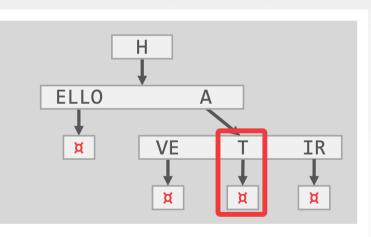
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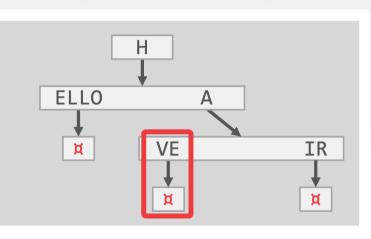
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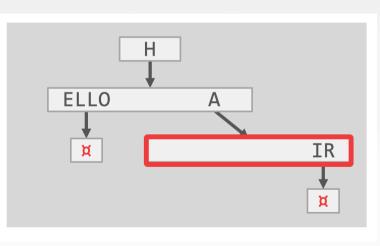
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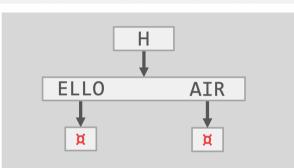
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More B+Trees

## Radix Tree: Binary Comparable Keys

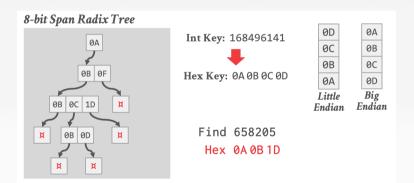
- Not all attribute types can be decomposed into binary comparable digits for a radix tree.
  - **Unsigned Integers:** Byte order must be flipped for little endian machines.
  - Signed Integers: Flip two's-complement so that negative numbers are smaller than positive.
  - Floats: Classify into group (neg vs. pos, normalized vs. denormalized), then store as unsigned integer.
  - **Compound:** Transform each attribute separately.



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### Radix Tree: Binary Comparable Keys

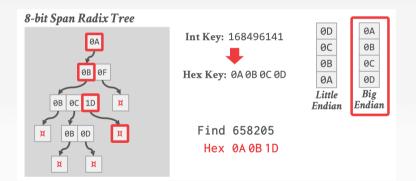




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## Radix Tree: Binary Comparable Keys





# **Inverted Index**

- The tree indexes that we've discussed so far are useful for "point" and "range" queries:
  - Find all customers in the 30308 zip code.
  - Find all orders between June 2020 and September 2020.
- They are not good at keyword searches:
  - Find all Wikipedia articles that contain the word "Trie"



Tries / Radix Trees

## Wikipedia Example

```
CREATE TABLE pages (
userID INT PRIMARY KEY,
userName VARCHAR UNIQUE,
);
CREATE TABLE pages (
pageID INT PRIMARY KEY,
title VARCHAR UNIQUE,
latest INT REFERENCES revisions (revID),
);
CREATE TABLE revisions (
revID INT PRIMARY KEY.
userID INT REFERENCES useracct (userID),
pageID INT REFERENCES pages (pageID),
content TEXT.
                                 -- Text Search
updated DATETIME
);
```



## Wikipedia Example

- If we create an index on the content attribute, what does that do?
- This doesn't help our query.
- Our query is also not correct since it will return any occurrence (not only exact matches)

CREATE INDEX idx\_rev\_content ON revisions (content);

SELECT pageID FROM revisions WHERE content LIKE '%Trie%';



- An inverted index stores a mapping of words to records that contain those words in the target attribute.
  - Sometimes called a <u>full-text search index</u>.
  - Also called a concordance in old (like really old) times.
- Major DBMSs support these natively (*e.g.*, PostgreSQL Generalized Inverted Index (GIN))
- There are also specialized DBMSs (e.g., Lucene, Elasticsearch)



# **Query Types**

More B+Trees

- Phrase Searches
  - ► Find records that contain a list of words in the given order.
- Proximity Searches
  - ► Find records where two words occur **<u>within n words</u>** of each other.
- Wildcard Searches
  - ▶ Find records that contain words that match some pattern (*e.g.*, regular expression).



## **Design Decisions**

#### • Decision 1: What To Store

- The index needs to store at least the words contained in each record (separated by punctuation characters).
- Can also store frequency, position, and other meta-data.

#### • Decision 2: When To Update

 Maintain auxiliary data structures to "stage" updates and then update the index in batches.





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- B+Trees are still the way to go for tree indexes.
- Next Class
  - How to make indexes thread-safe!



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