

DATA ANALYTICS USING DEEP LEARNING

GT 8803 // FALL 2019 // JOY ARULRAJ

LECTURE #15: RECURRENT NEURAL NETWORKS

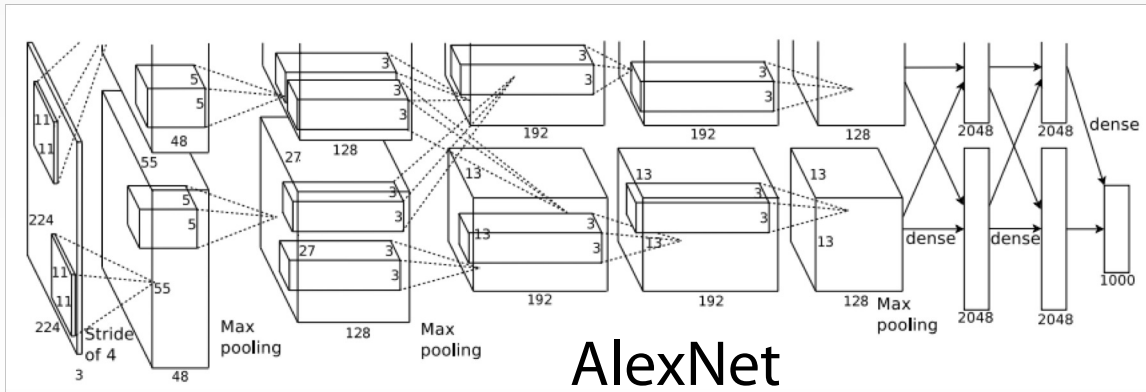
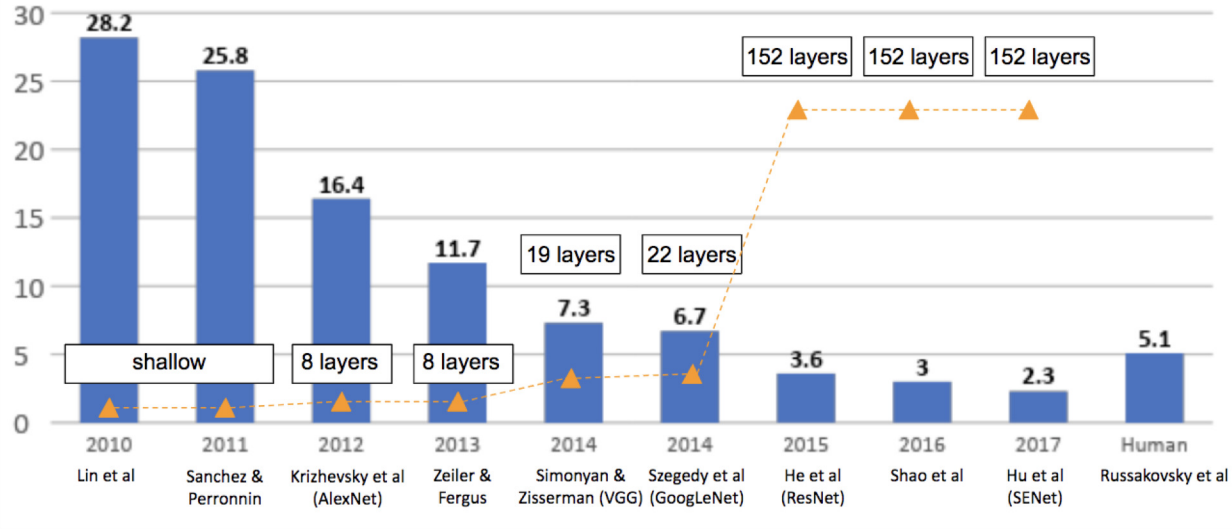
CREATING THE NEXT®

ADMINISTRIVIA

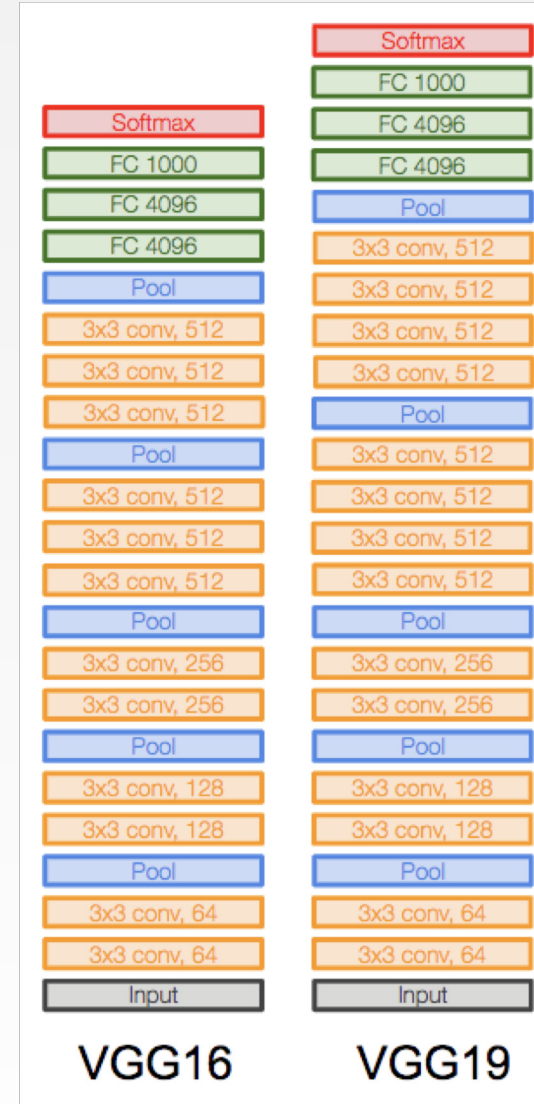
- Reminders
 - Signup for a weekly project discussion slot
 - Project progress updates due on next Monday
 - Assignment 2 due on next Wednesday

LAST TIME: CNN ARCHITECTURES

ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners

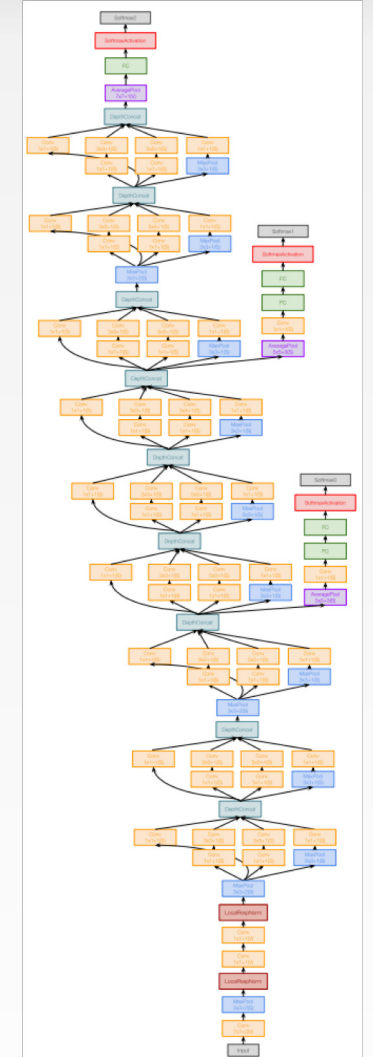


AlexNet



VGG16

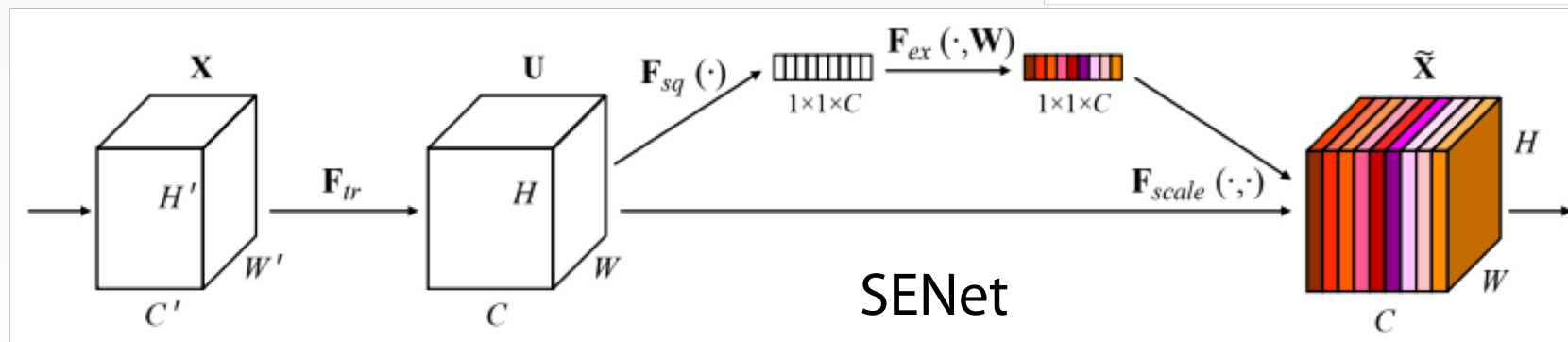
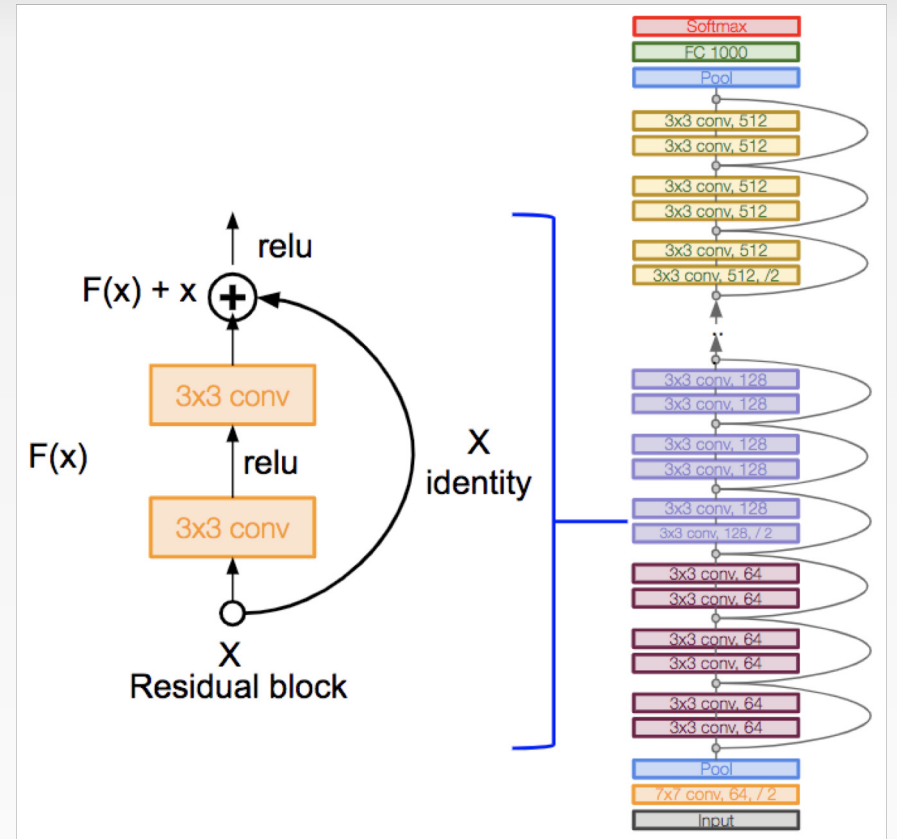
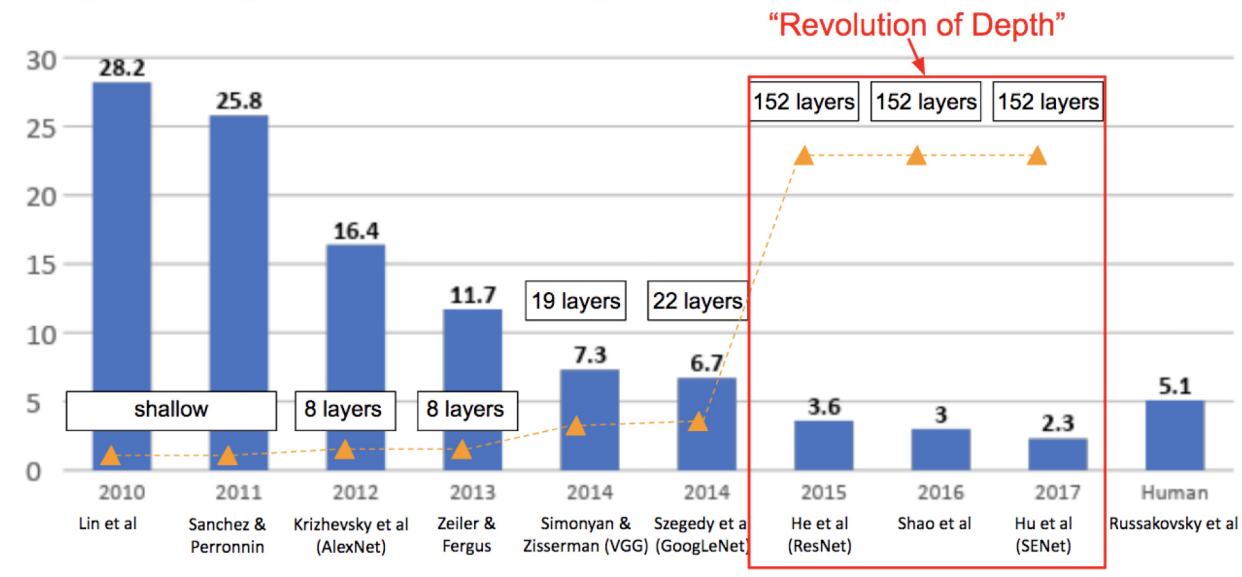
VGG19



GoogLeNet

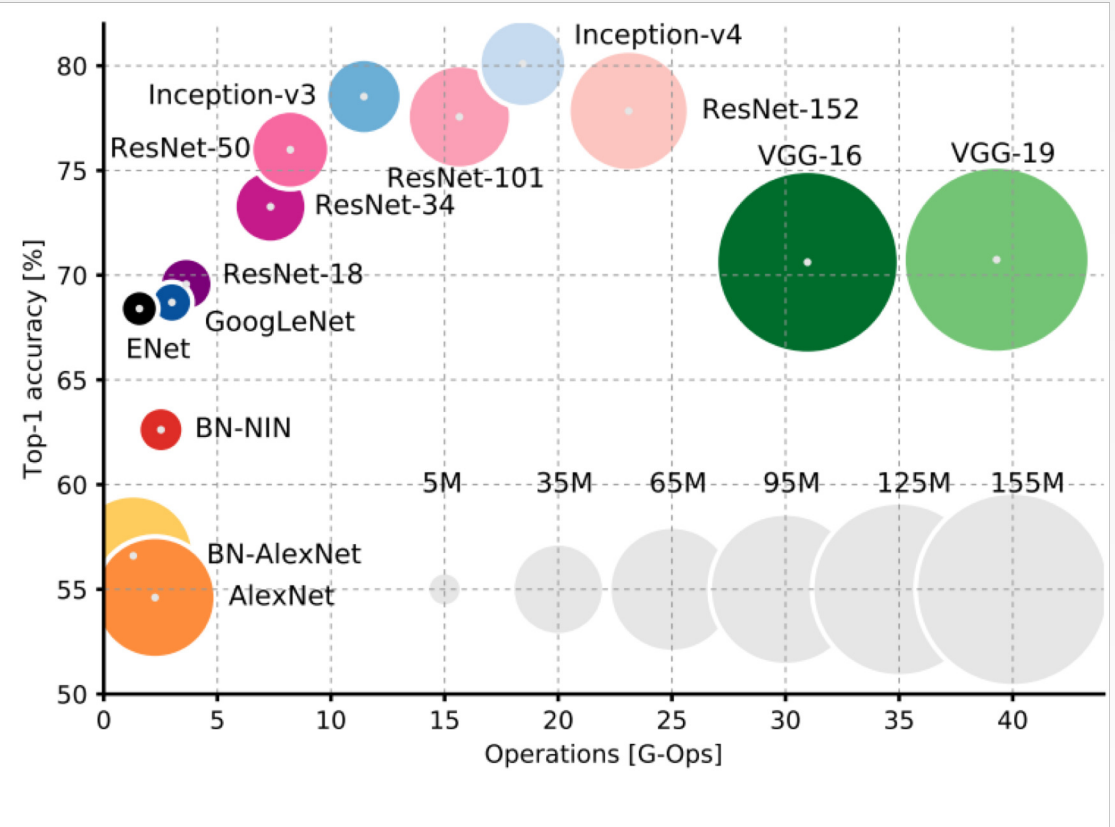
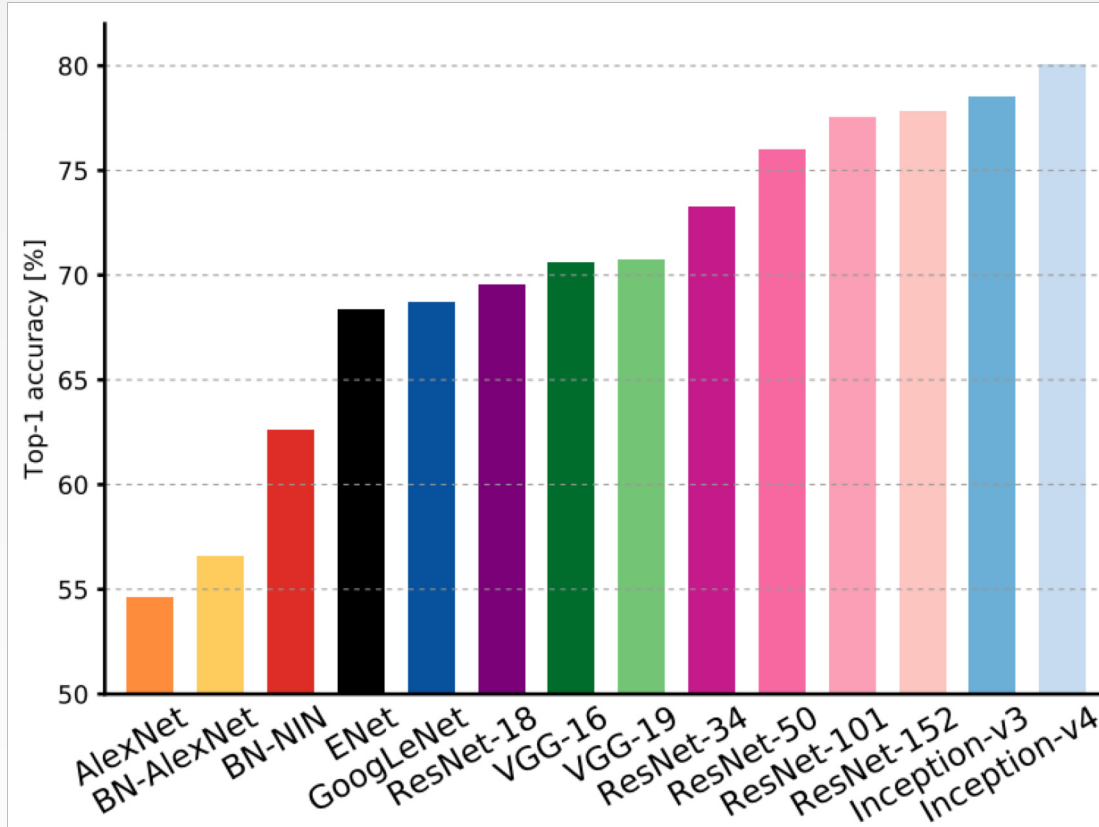
LAST TIME: CNN ARCHITECTURES

ImageNet Large Scale Visual Recognition Challenge (ILSVRC) winners



ResNet

LAST TIME: COMPARING COMPLEXITY



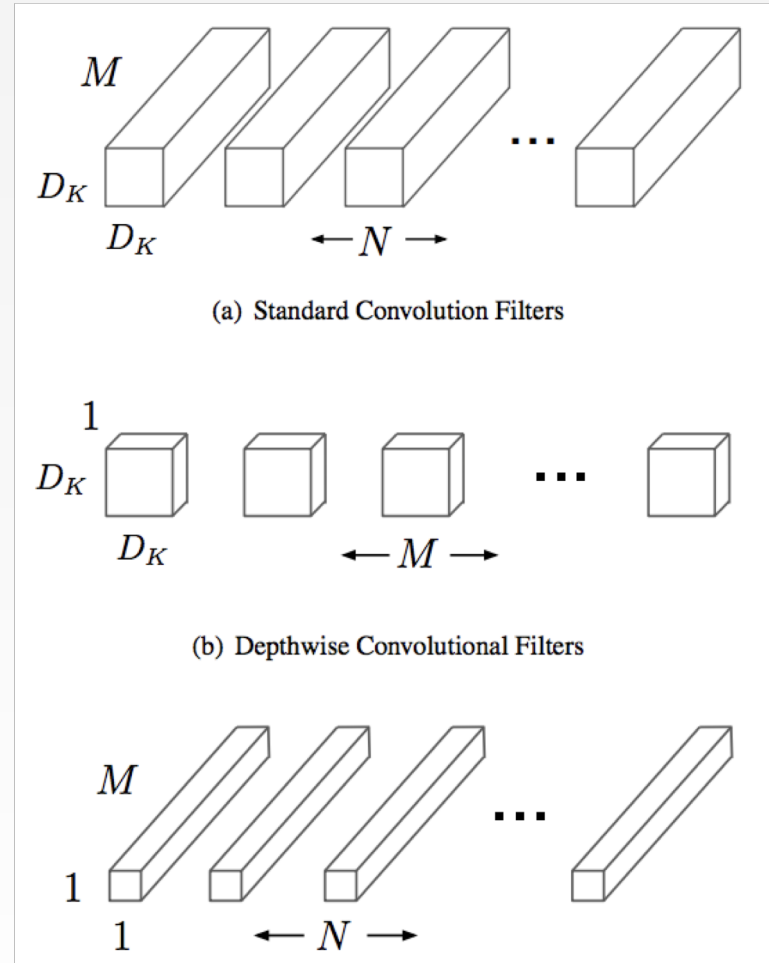
An Analysis of Deep Neural Network Models for Practical Applications, 2017.

EFFICIENT NETWORKS...

MOBILENETS: EFFICIENT CONVOLUTIONAL NEURAL NETWORKS FOR MOBILE APPLICATIONS

[Howard et al. 2017]

- Depthwise separable convolutions replace standard convolutions by factorizing them into a depthwise convolution and a 1x1 convolution that is much more efficient
- Much more efficient, with little loss in accuracy
- Follow-up MobileNetV2 work in 2018 (Sandler et al.)
- Other works in this space e.g. ShuffleNet (Zhang et al. 2017)

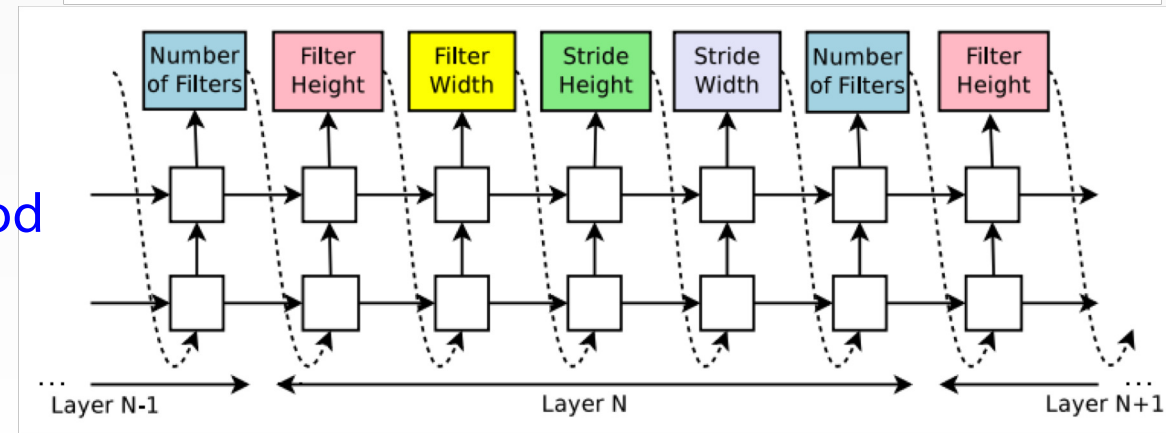
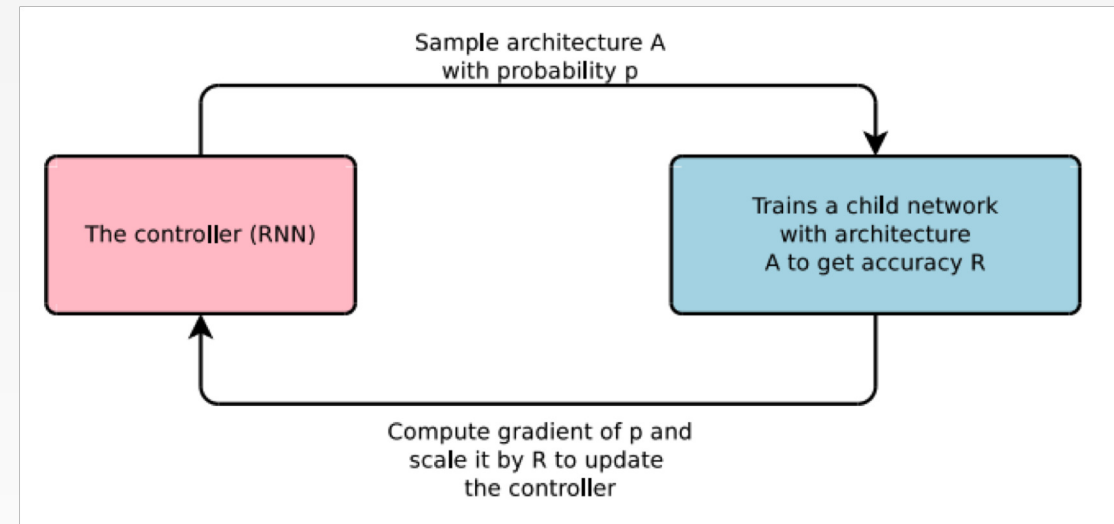


META-LEARNING: LEARNING TO LEARN NETWORK ARCHITECTURES...

NEURAL ARCHITECTURE SEARCH WITH REINFORCEMENT LEARNING (NAS)

[Zoph et al. 2016]

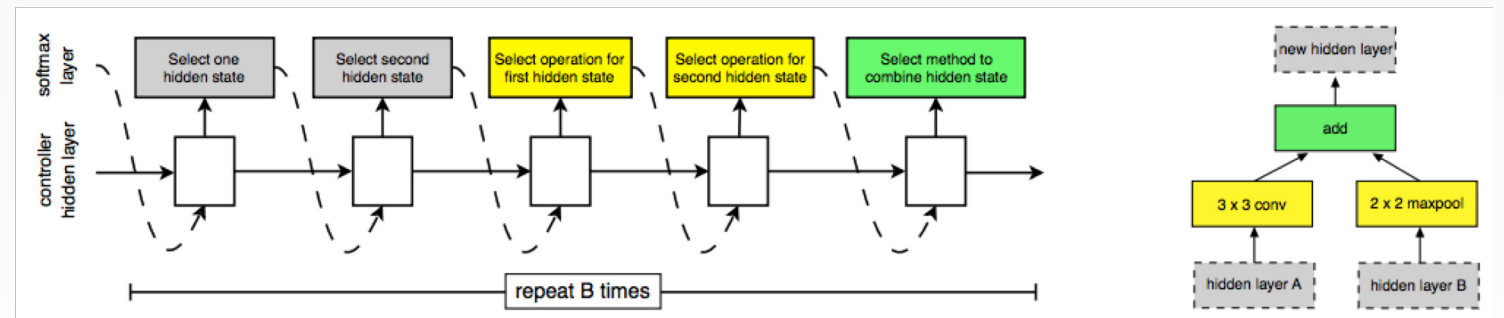
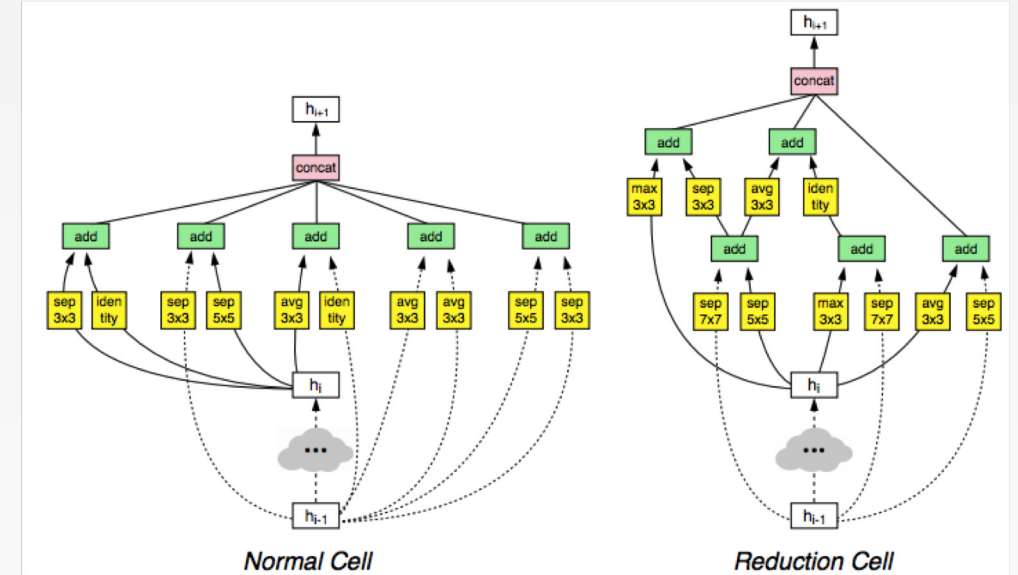
- “Controller” network that learns to design a good network architecture (output a string corresponding to network design)
- Iterate:
 - Sample an architecture from search space
 - Train the architecture to get a “reward” R corresponding to accuracy
 - Compute gradient of sample probability, and scale by R to **perform controller parameter update** (i.e. increase likelihood of good architecture being sampled, decrease likelihood of bad architecture)



META-LEARNING: LEARNING TO LEARN NETWORK ARCHITECTURES... LEARNING TRANSFERABLE ARCHITECTURES FOR SCALABLE IMAGE RECOGNITION

[Zoph et al. 2017]

- Applying neural architecture search (NAS) to a large dataset like ImageNet is expensive
- Design a **search space of building blocks** (“cells”) that can be flexibly stacked
- NASNet: Use NAS to **find best cell structure on smaller CIFAR-10 dataset, then transfer architecture to ImageNet**
- Many follow-up works in this space e.g. AmoebaNet (Real et al. 2019) and ENAS (Pham, Guan et al. 2018)



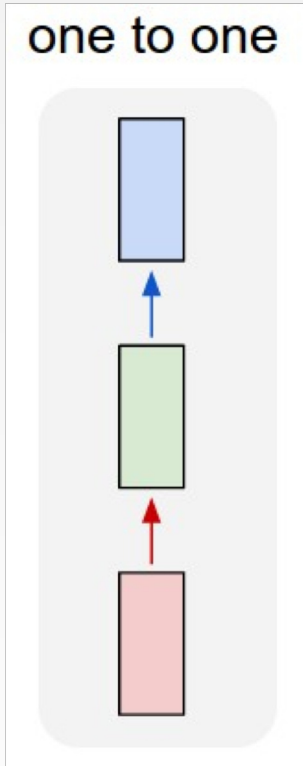
TODAY'S AGENDA

- Recurrent Neural Networks
- Case Studies
 - Language Modeling
 - Image Captioning
- Gradient Flow
- Long Short Term Memory (LSTM)



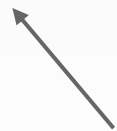
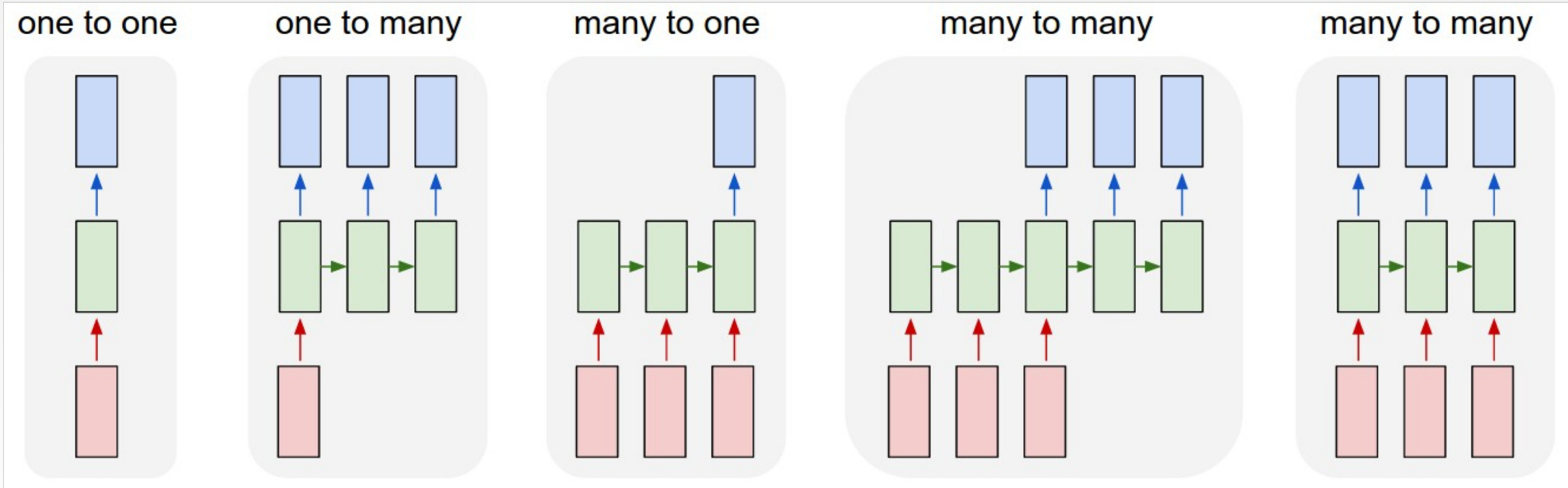
RNN

“VANILLA” NEURAL NETWORK



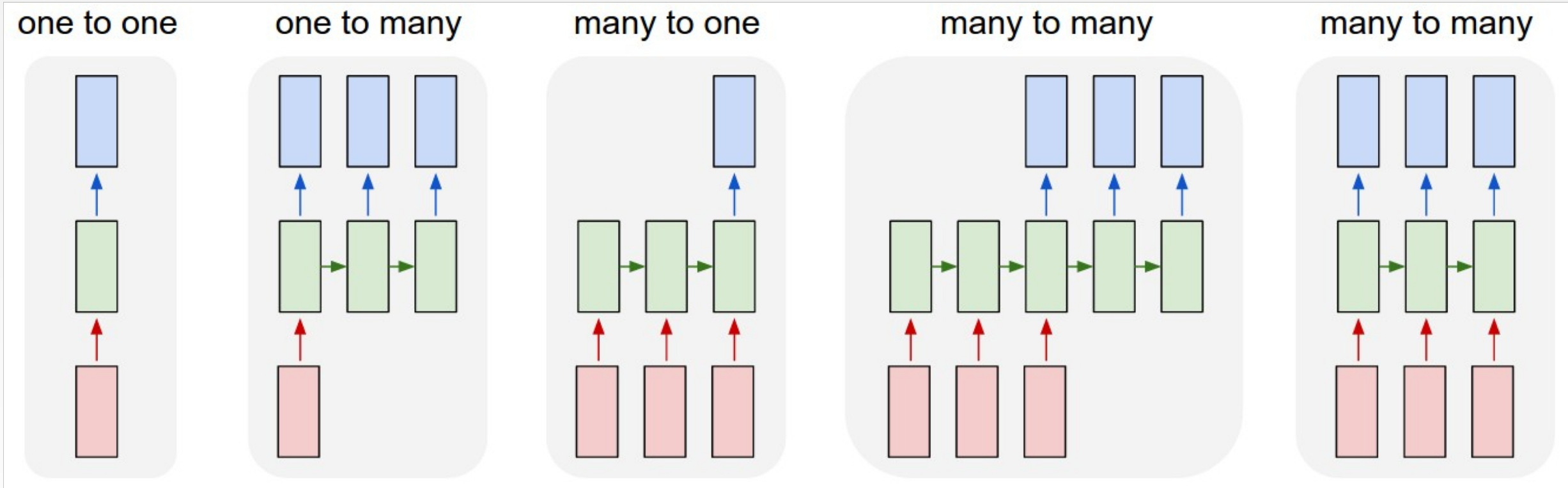
Vanilla Neural Networks

RECURRENT NEURAL NETWORKS: PROCESS SEQUENCES



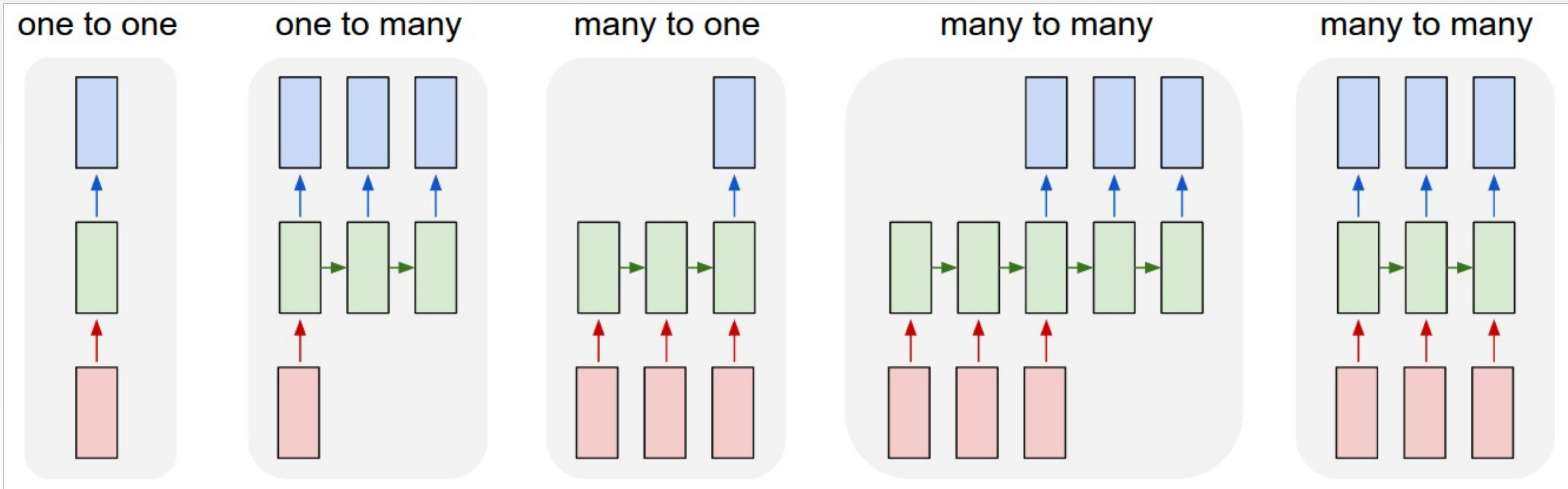
e.g. **Image Captioning**
image -> sequence of words

RECURRENT NEURAL NETWORKS: PROCESS SEQUENCES



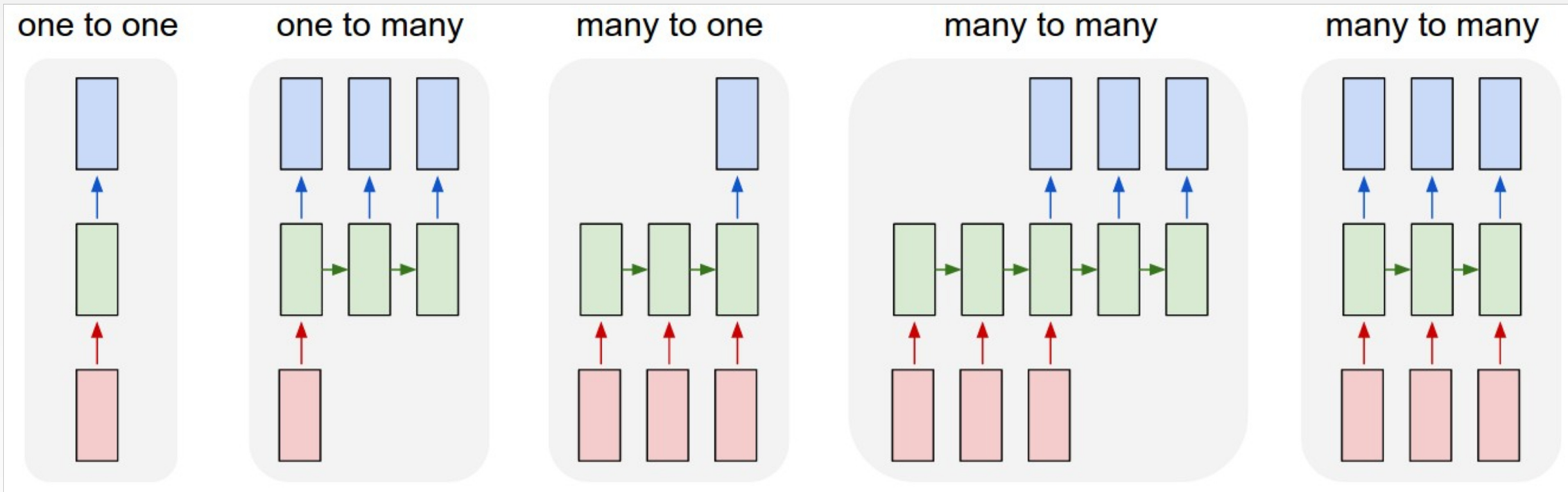
e.g. **Sentiment Classification**
sequence of words -> sentiment

RECURRENT NEURAL NETWORKS: PROCESS SEQUENCES



↖ e.g. **Machine Translation**
seq of words -> seq of words

RECURRENT NEURAL NETWORKS: PROCESS SEQUENCES



e.g. **Video classification on frame level**

SEQUENTIAL PROCESSING OF NON-SEQUENCE DATA

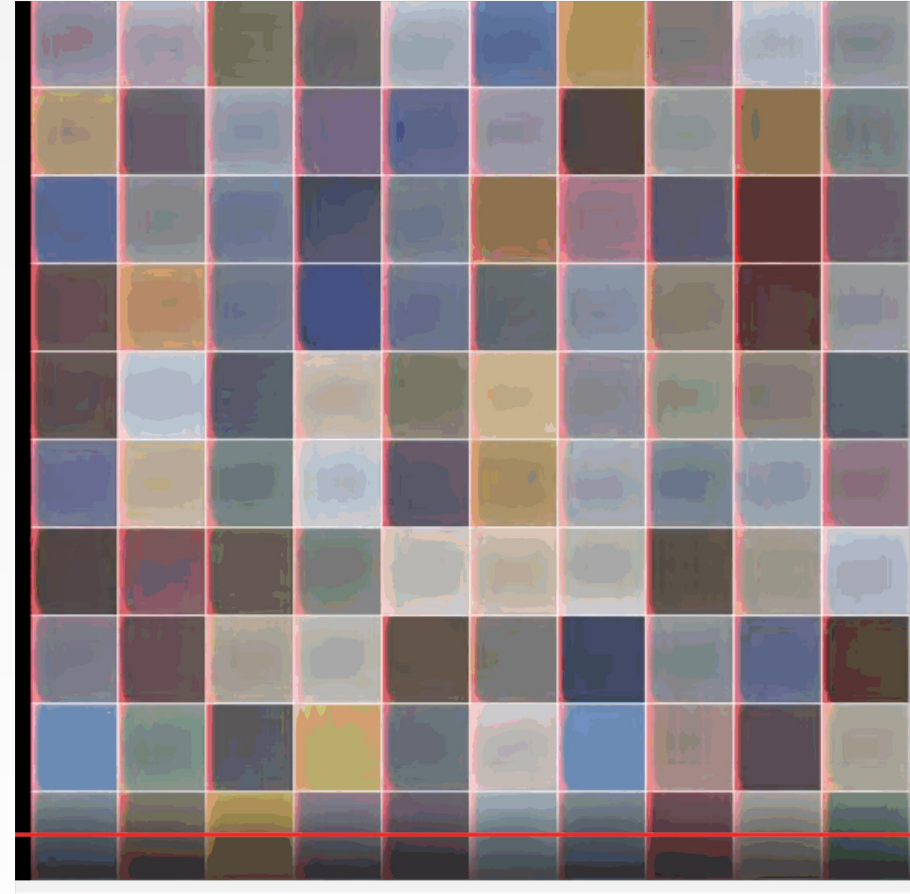
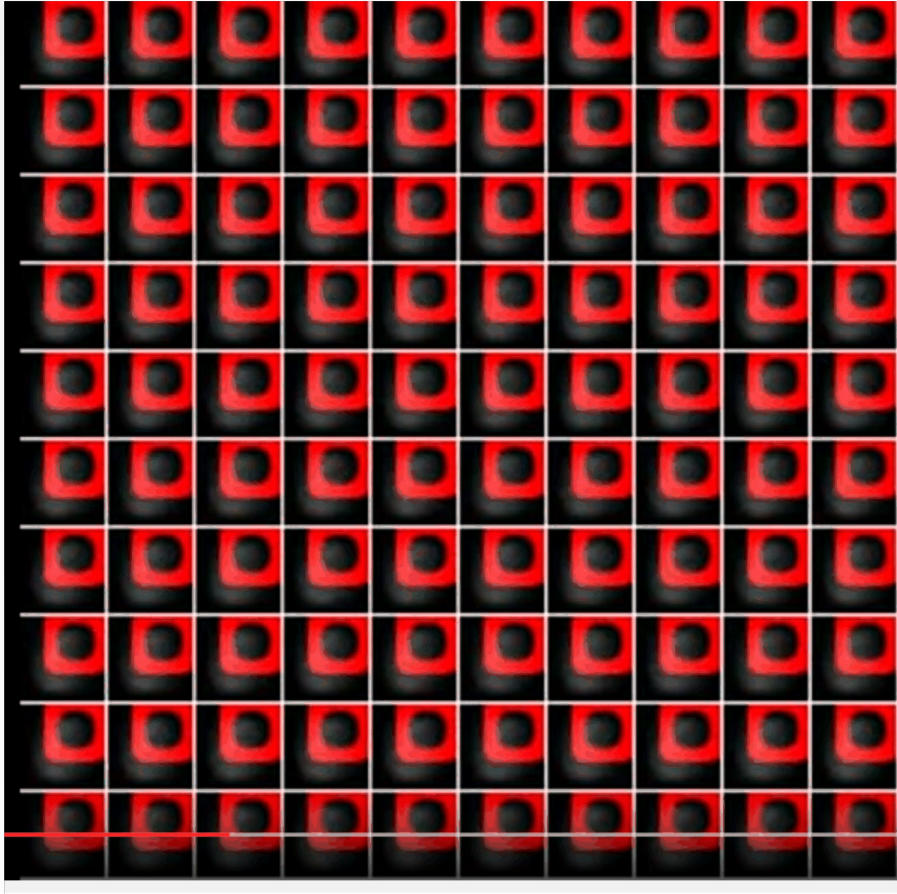
Classify images by taking a series of “glimpses”



Ba, Mnih, and Kavukcuoglu, “Multiple Object Recognition with Visual Attention”, ICLR 2015.
Gregor et al, “DRAW: A Recurrent Neural Network For Image Generation”, ICML 2015
Figure copyright Karol Gregor, Ivo Danihelka, Alex Graves, Danilo Jimenez Rezende, and Daan Wierstra, 2015.
Reproduced with permission.

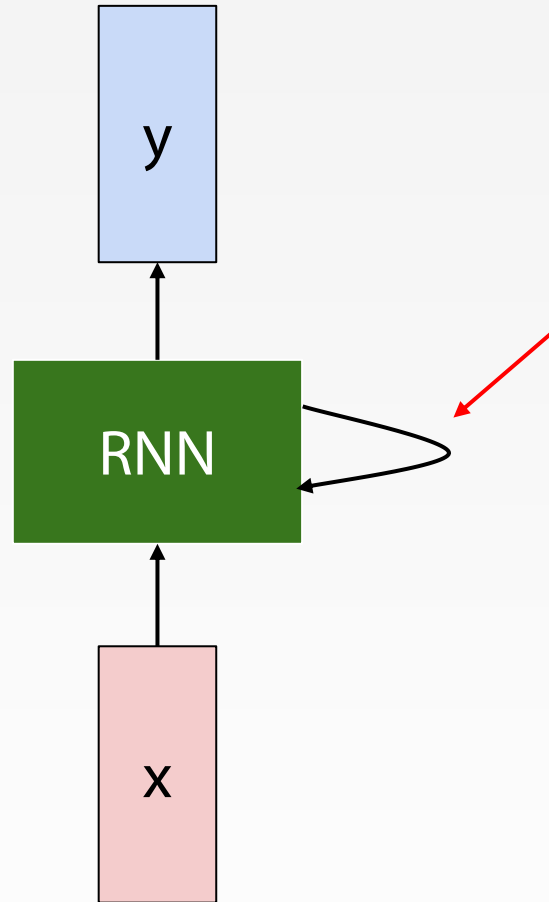
SEQUENTIAL PROCESSING OF NON-SEQUENCE DATA

Generate images one piece at a time!



Gregor et al, "DRAW: A Recurrent Neural Network For Image Generation", ICML 2015
Figure copyright Karol Gregor, Ivo Danihelka, Alex Graves, Danilo Jimenez Rezende, and Daan Wierstra, 2015. Reproduced with permission.

RECURRENT NEURAL NETWORK



Key idea: RNNs have an "internal state" that is updated as a sequence is processed

RECURRENT NEURAL NETWORK

We can process a sequence of vectors \mathbf{x} by applying a **recurrence formula** at every time step:

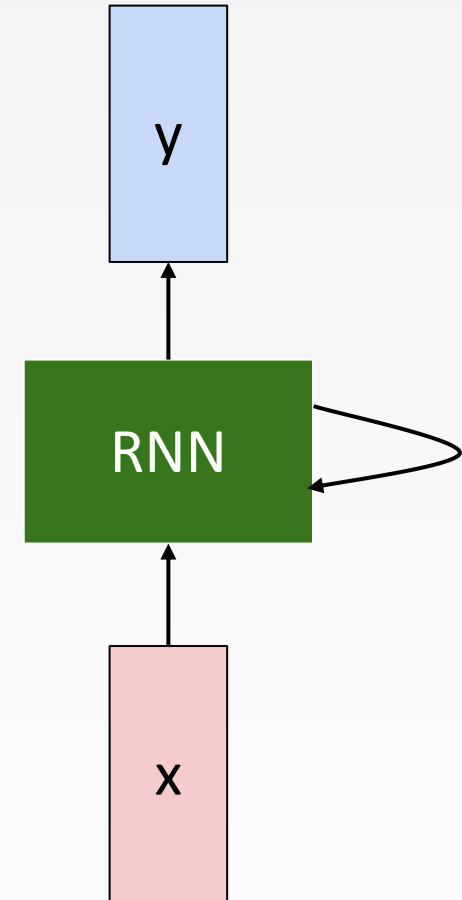
$$h_t = f_W(h_{t-1}, x_t)$$

new state

some function
with parameters W

old state

input vector at
some time step

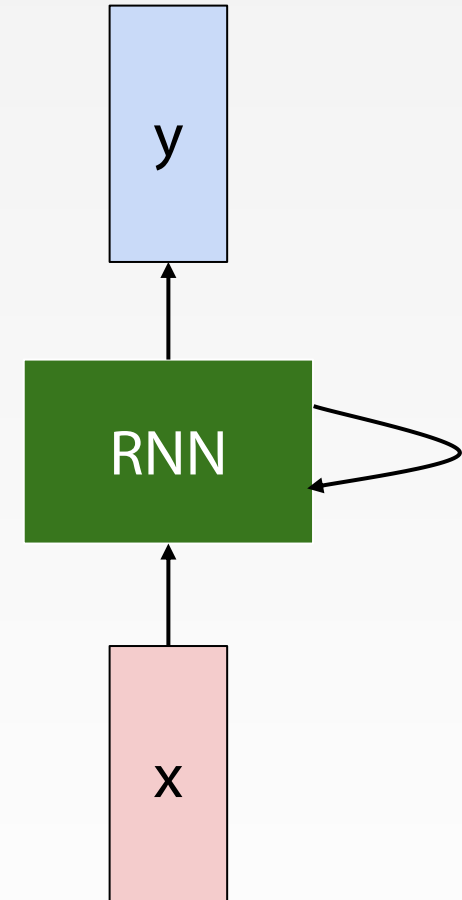


RECURRENT NEURAL NETWORK

We can process a sequence of vectors \mathbf{x} by applying a **recurrence formula** at every time step:

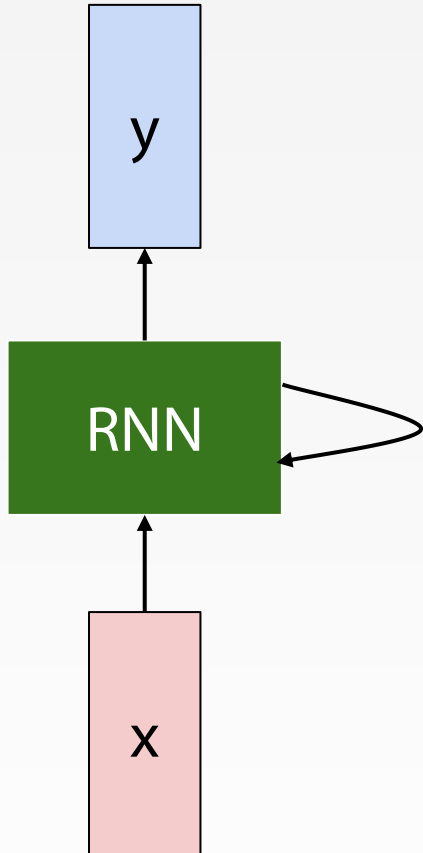
$$h_t = f_W(h_{t-1}, x_t)$$

Notice: the same function and the same set of parameters are used at every time step.



(SIMPLE) RECURRENT NEURAL NETWORK

The state consists of a single “hidden” vector \mathbf{h} :



$$h_t = f_W(h_{t-1}, x_t)$$

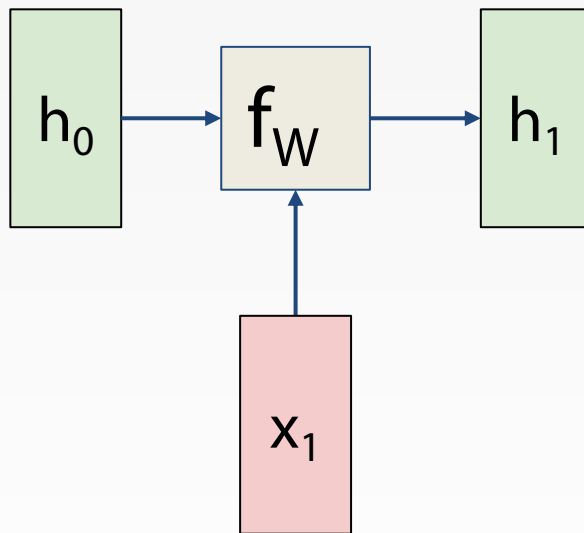


$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)$$

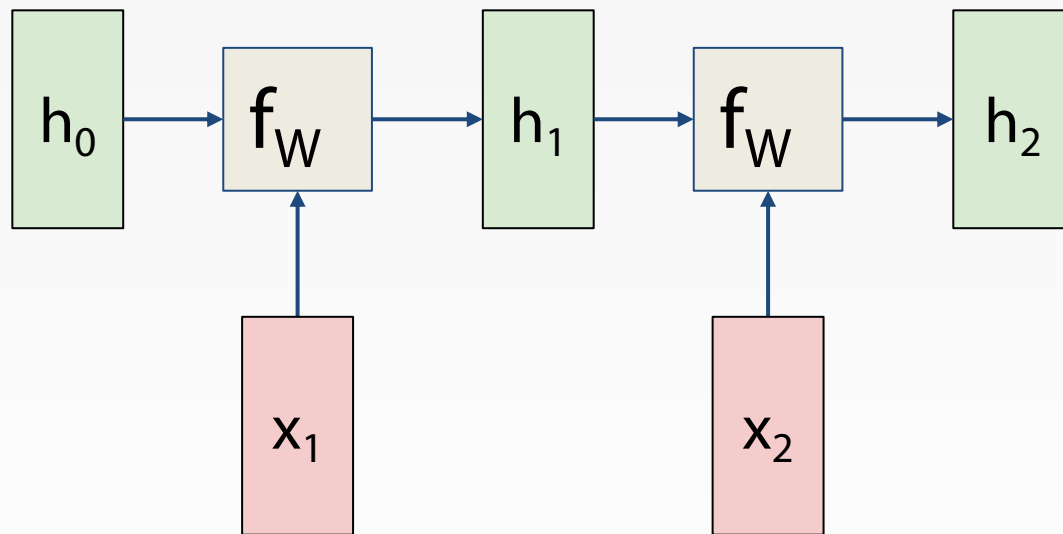
$$y_t = W_{hy}h_t$$

Sometimes called a “Vanilla RNN”
or an “Elman RNN” after Prof. Jeffrey Elman

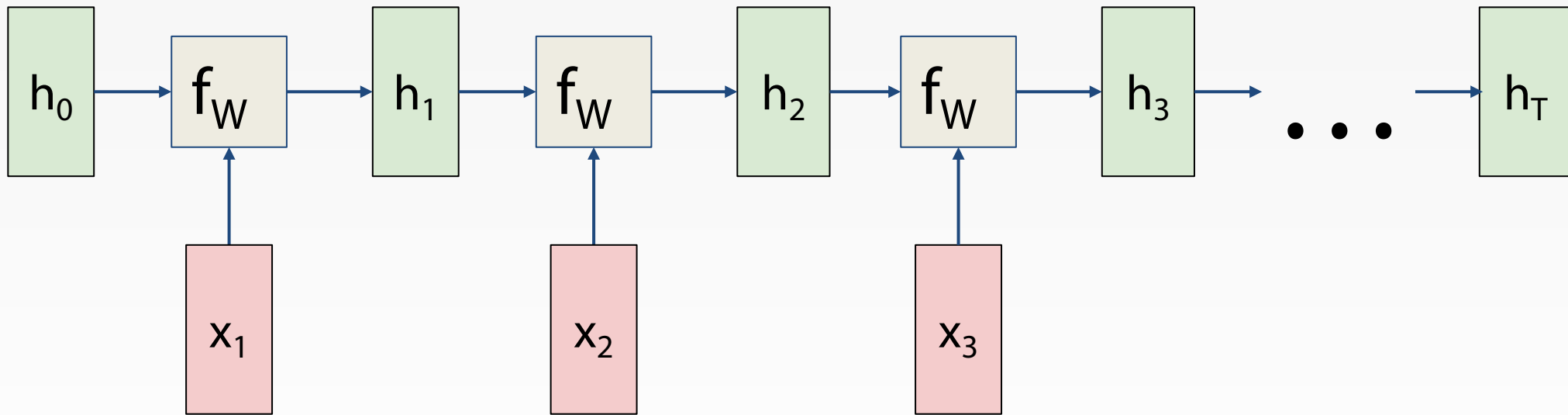
RNN: COMPUTATIONAL GRAPH



RNN: COMPUTATIONAL GRAPH

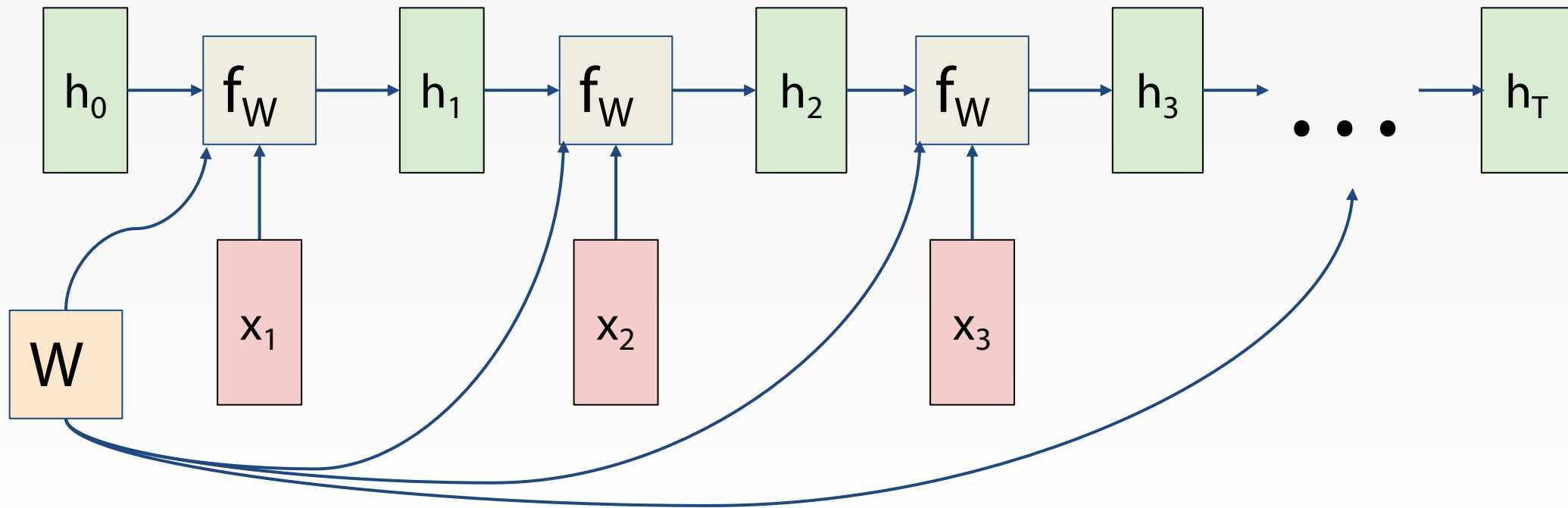


RNN: COMPUTATIONAL GRAPH

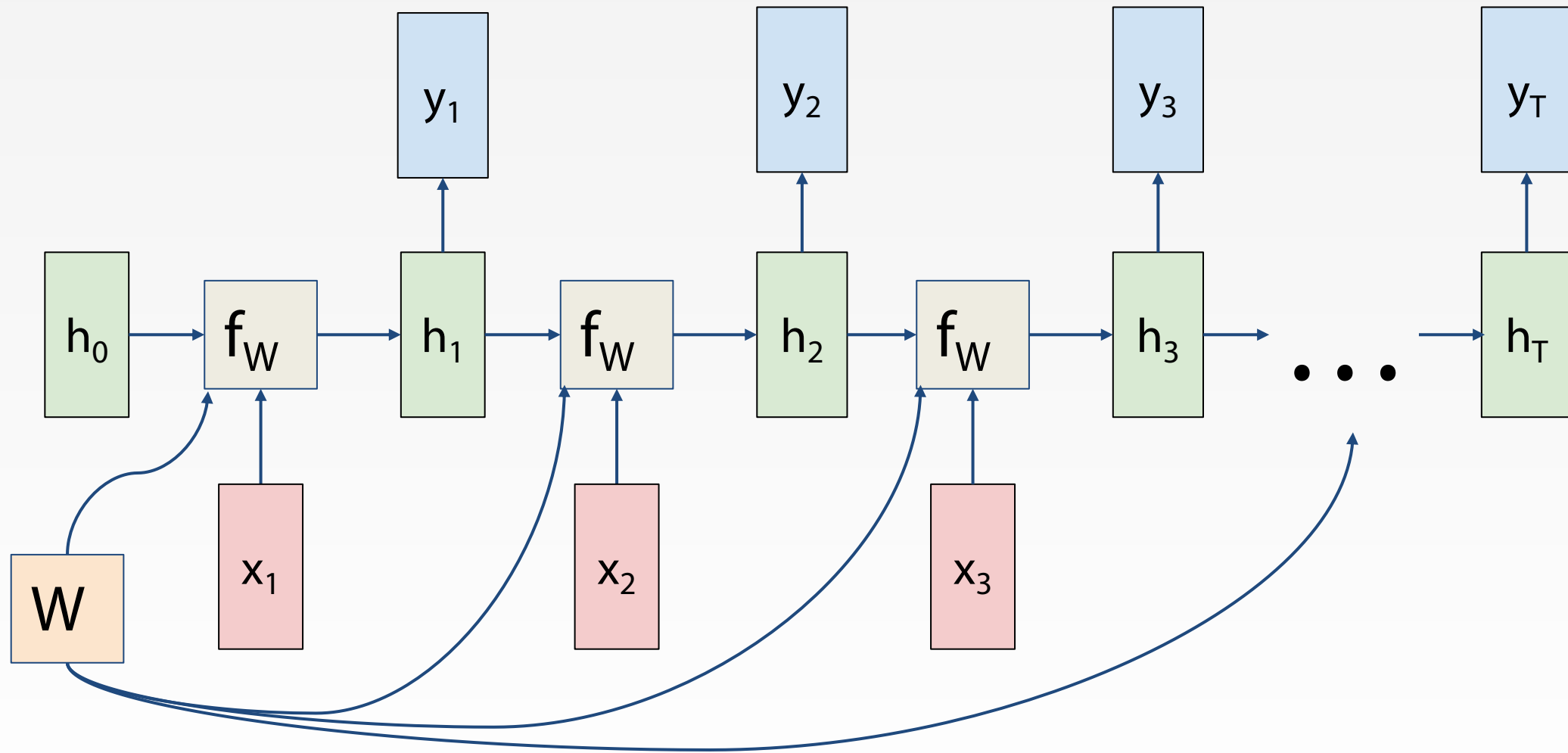


RNN: COMPUTATIONAL GRAPH

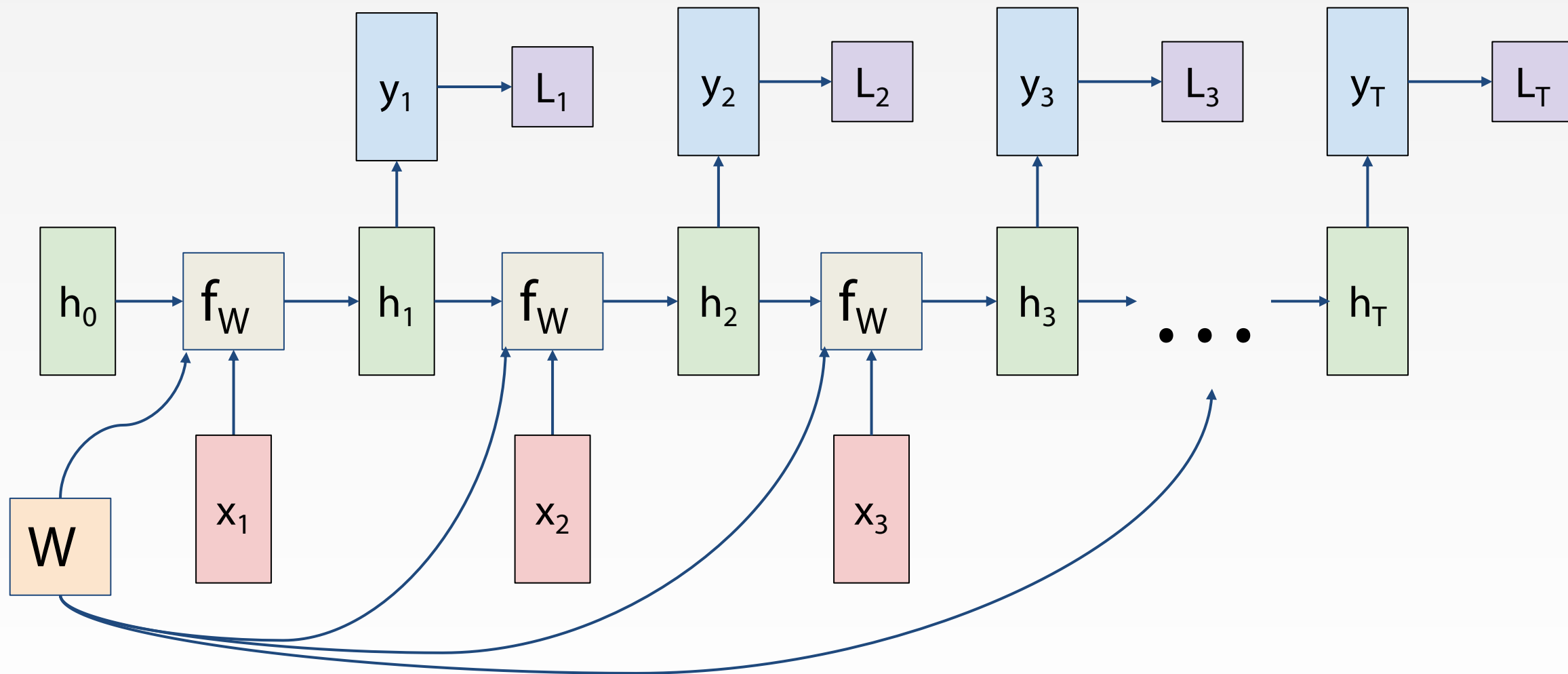
Re-use the same weight matrix at every time-step



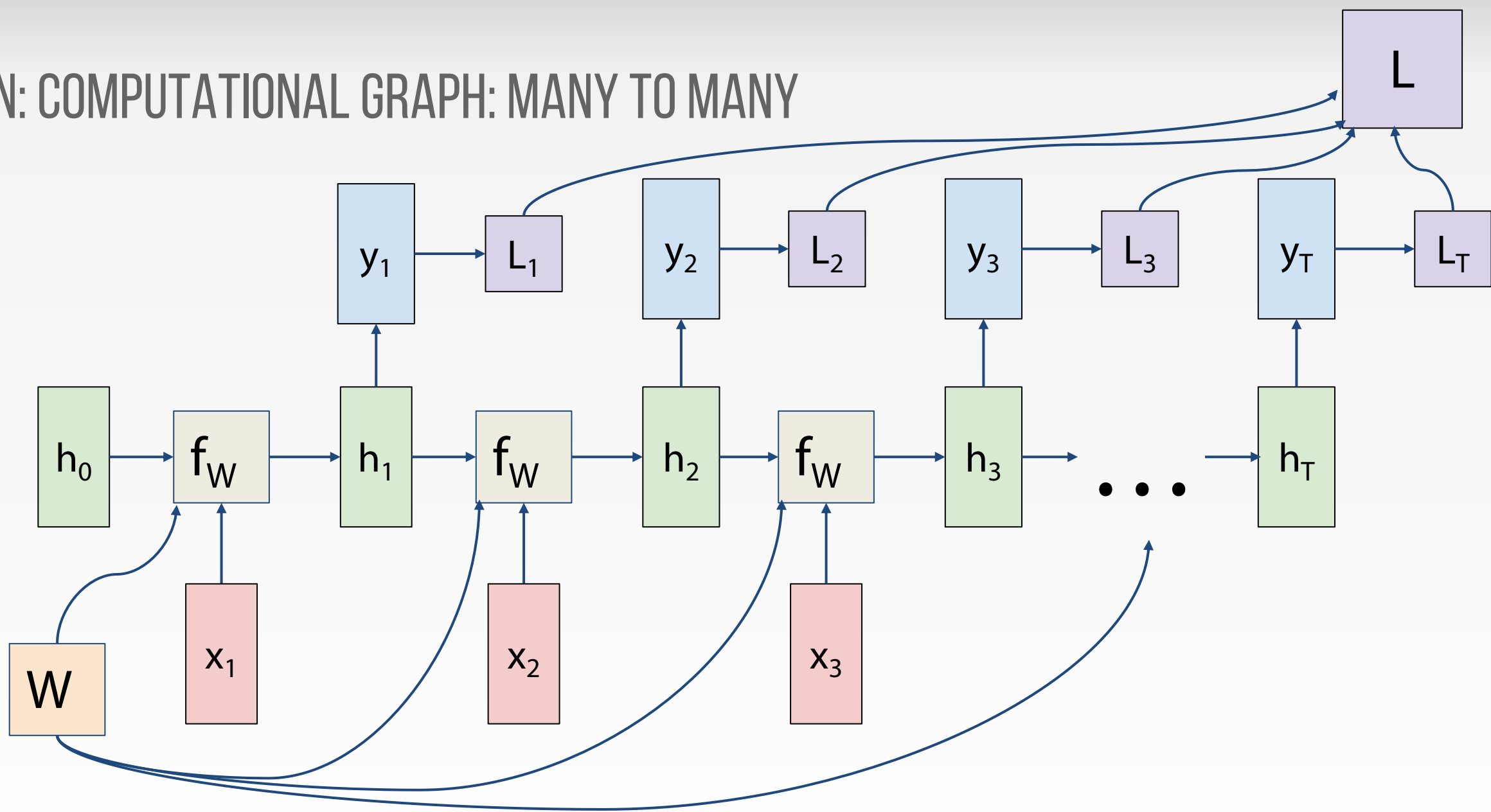
RNN: COMPUTATIONAL GRAPH: MANY TO MANY



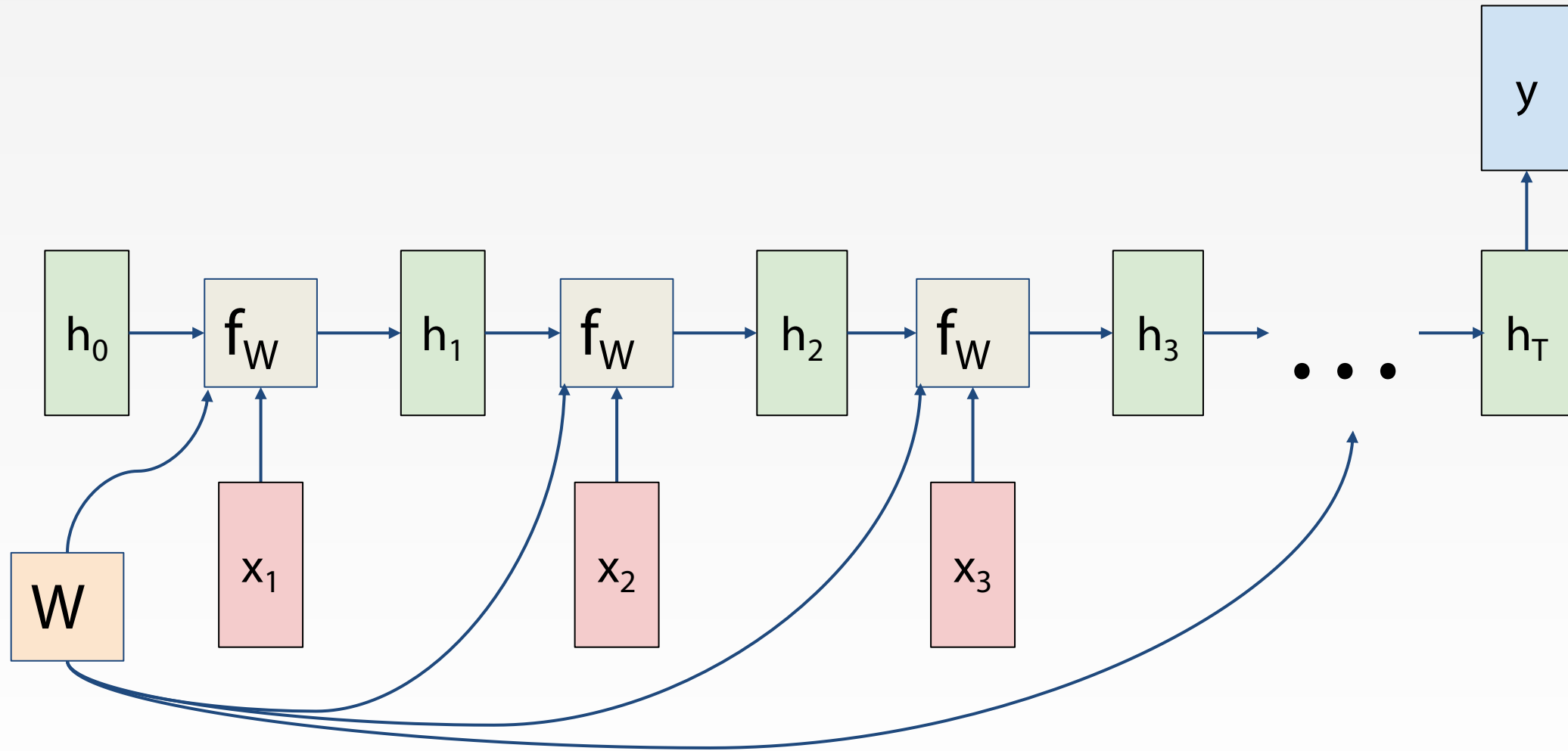
RNN: COMPUTATIONAL GRAPH: MANY TO MANY



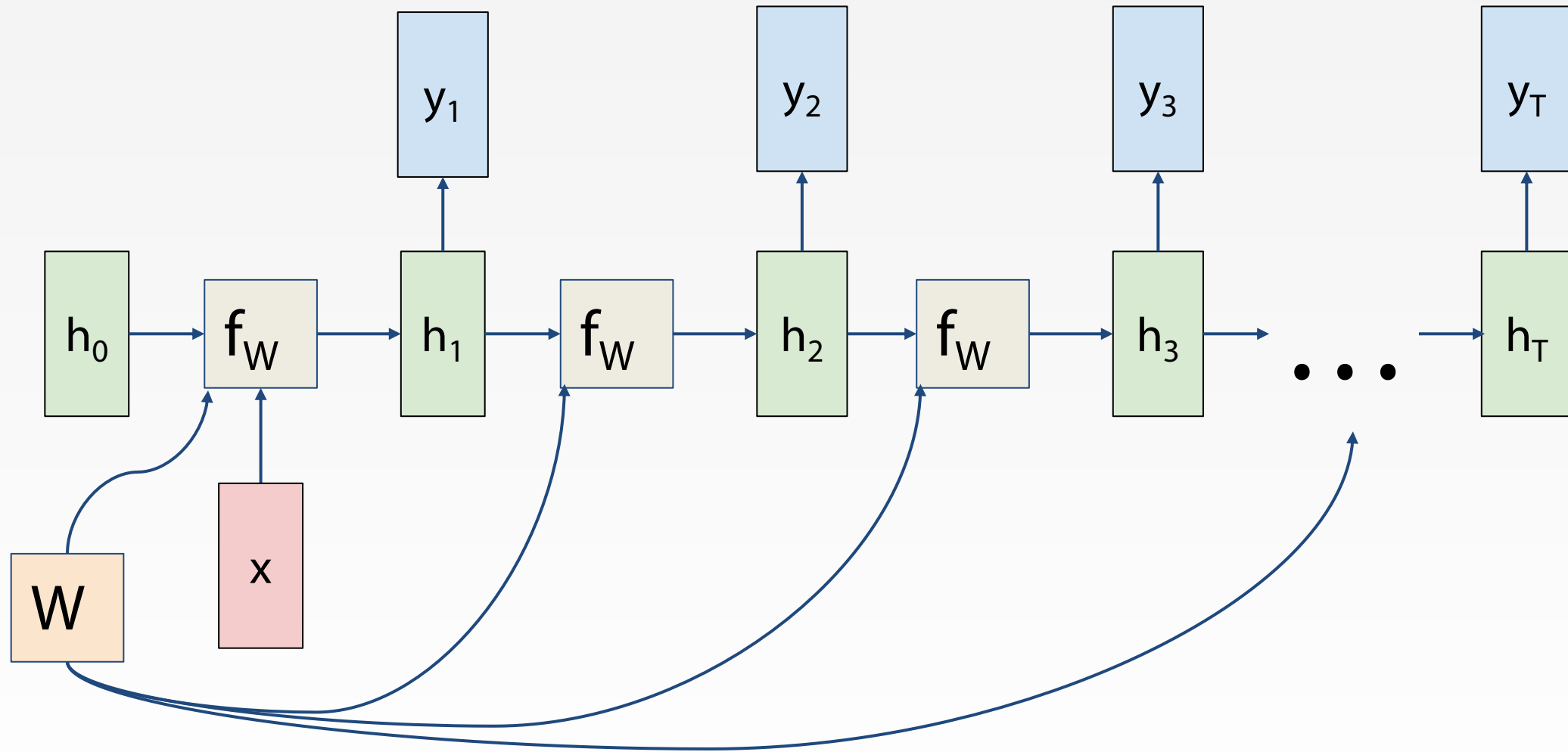
RNN: COMPUTATIONAL GRAPH: MANY TO MANY



RNN: COMPUTATIONAL GRAPH: MANY TO ONE

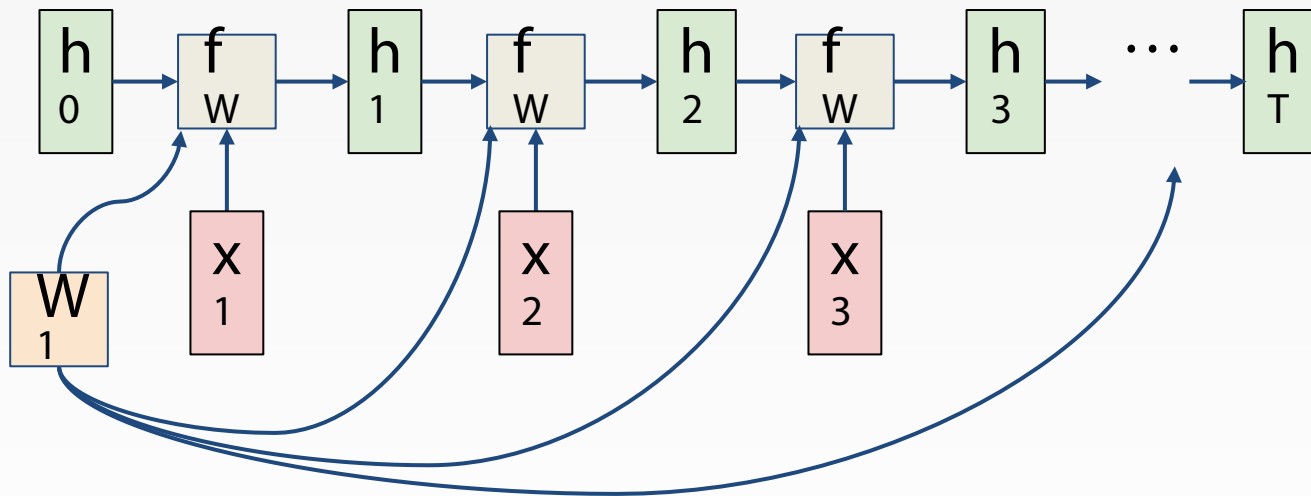


RNN: COMPUTATIONAL GRAPH: ONE TO MANY



SEQUENCE TO SEQUENCE: MANY-TO-ONE + ONE-TO-MANY

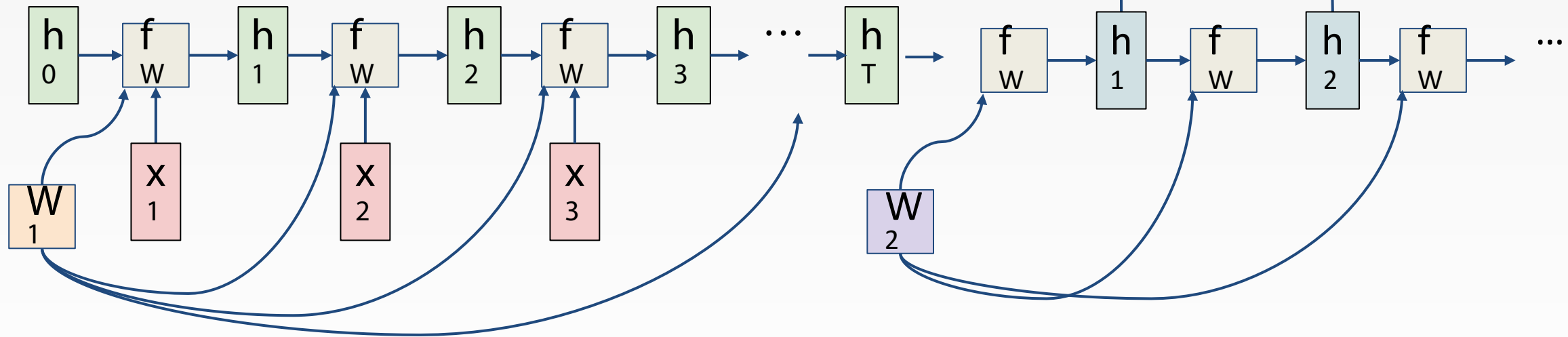
Many to one: Encode input sequence in a single vector



Sutskever et al, "Sequence to Sequence Learning with Neural Networks", NIPS 2014

SEQUENCE TO SEQUENCE: MANY-TO-ONE + ONE-TO-MANY

Many to one: Encode input sequence in a single vector



One to many: Produce output sequence from single input vector

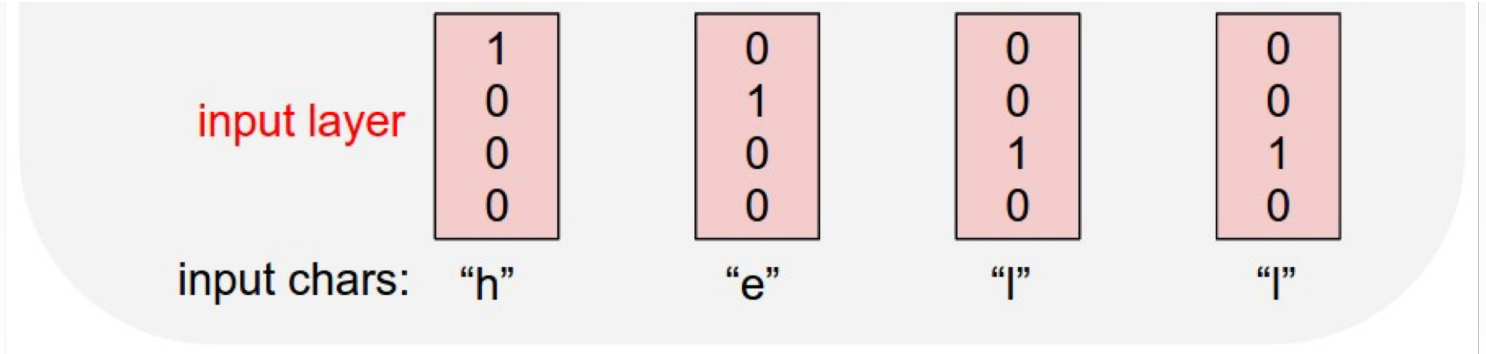


LANGUAGE MODELING

EXAMPLE: CHARACTER- LEVEL LANGUAGE MODEL

Vocabulary:
[h,e,l,o]

Example training
sequence:
“hello”

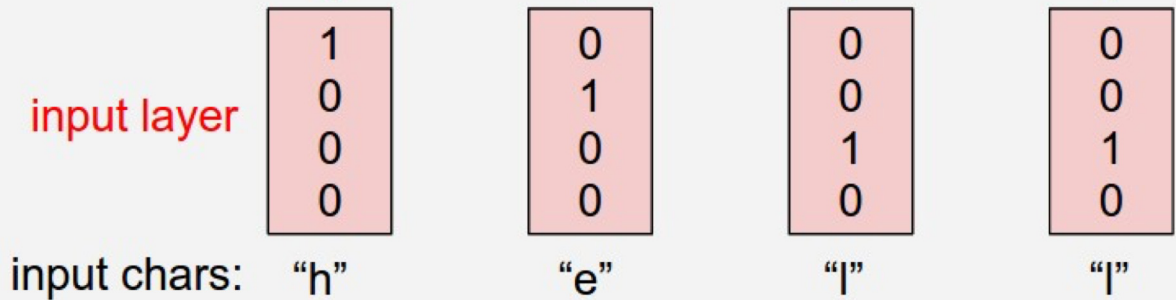


EXAMPLE: CHARACTER-
LEVEL
LANGUAGE MODEL

Vocabulary:
[h,e,l,o]

Example training
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“hello”

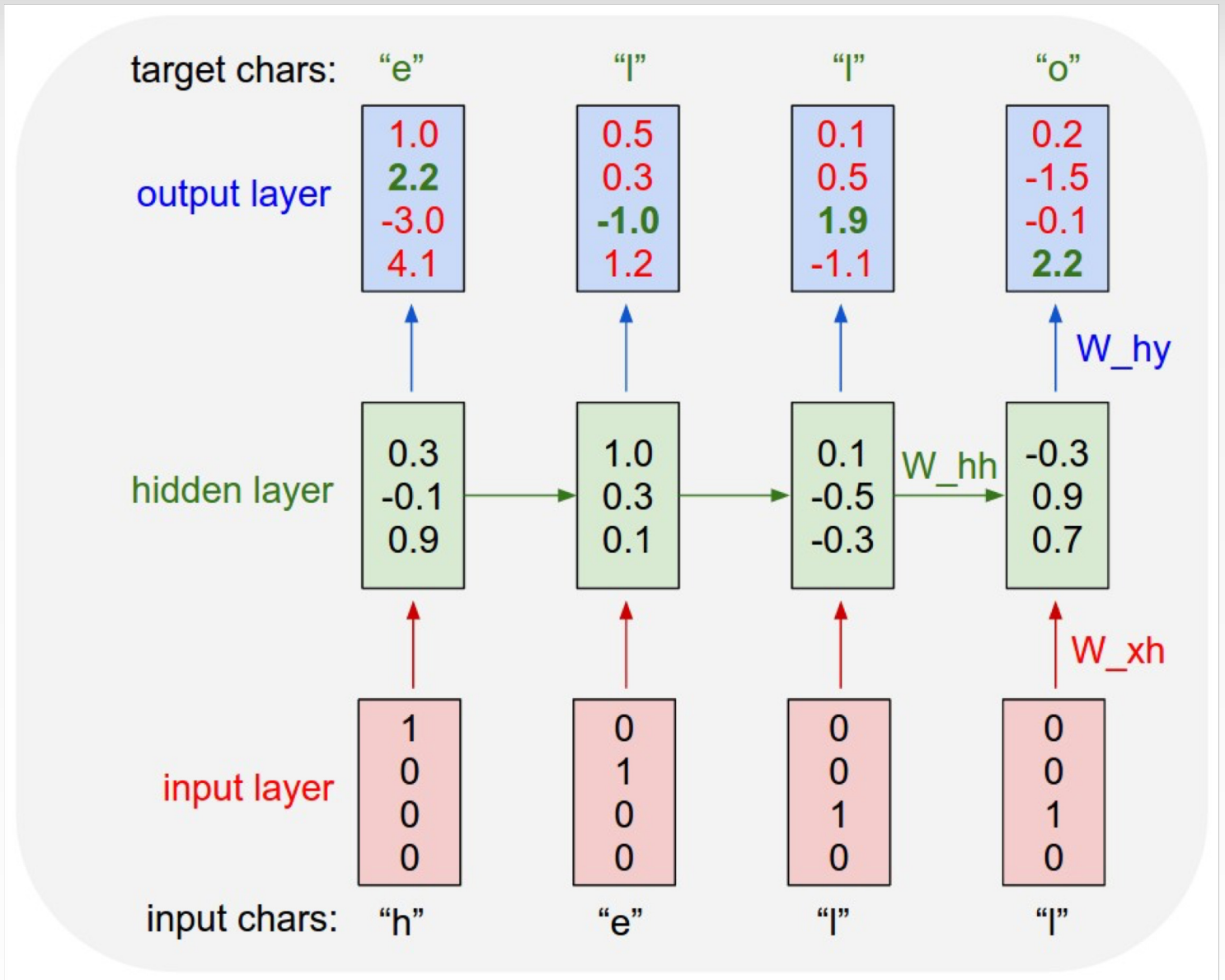
$$h_t = \tanh(W_{hh}h_{t-1} + W_{xh}x_t)$$



EXAMPLE: CHARACTER-LEVEL LANGUAGE MODEL

Vocabulary:
[h,e,l,o]

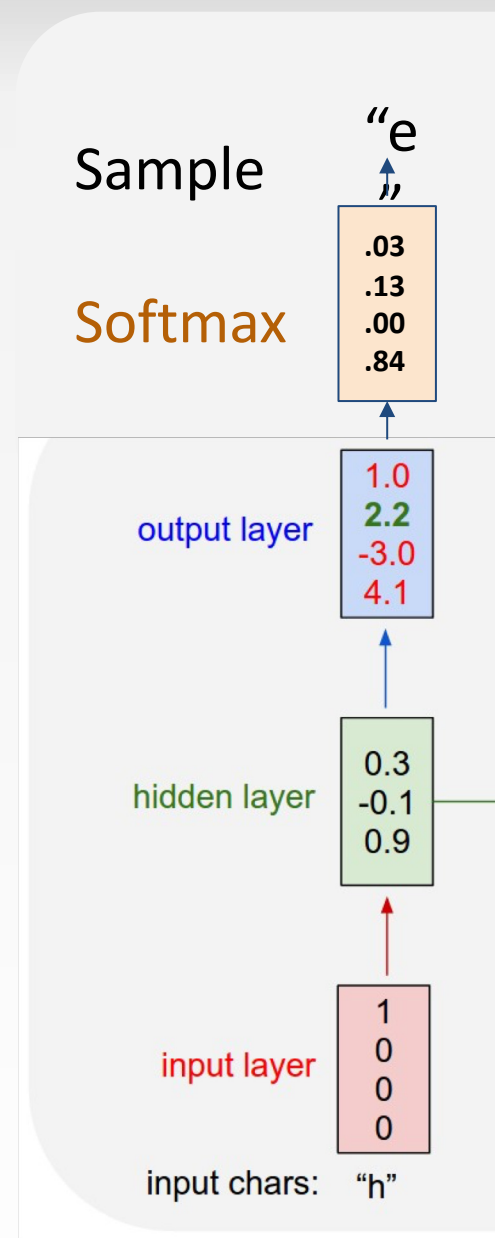
Example training sequence:
"hello"



EXAMPLE: CHARACTER-LEVEL LANGUAGE MODEL

Vocabulary:
[h,e,l,o]

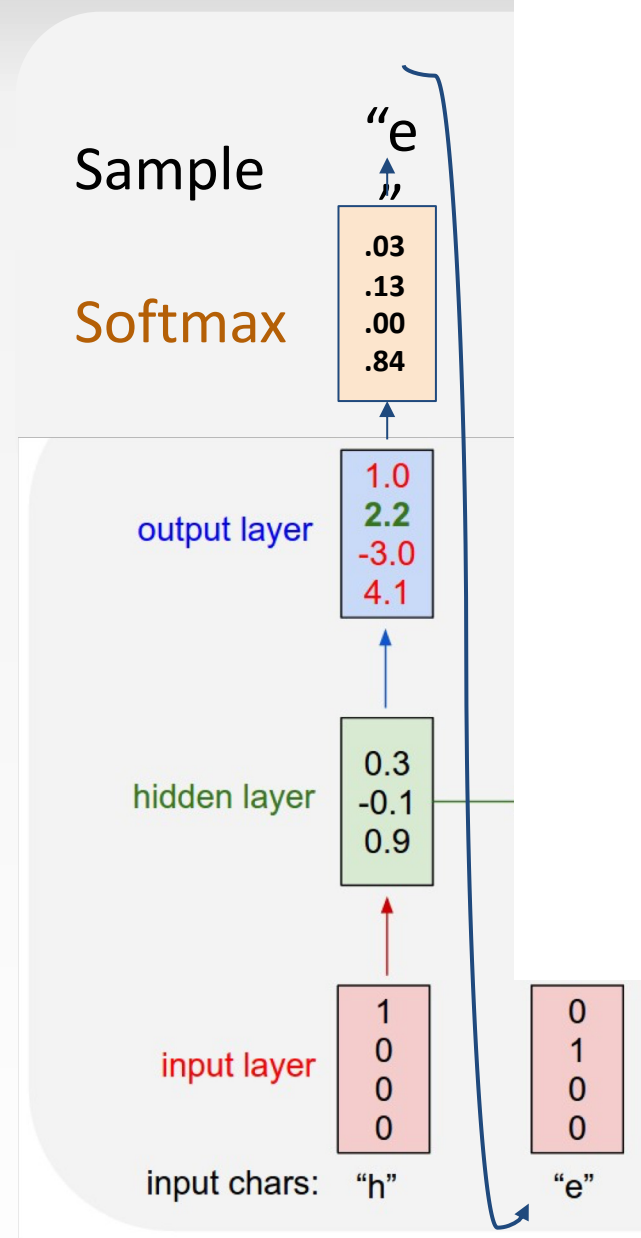
At test-time sample characters one at a time, feed back to model



EXAMPLE: CHARACTER-LEVEL LANGUAGE MODEL

Vocabulary:
[h,e,l,o]

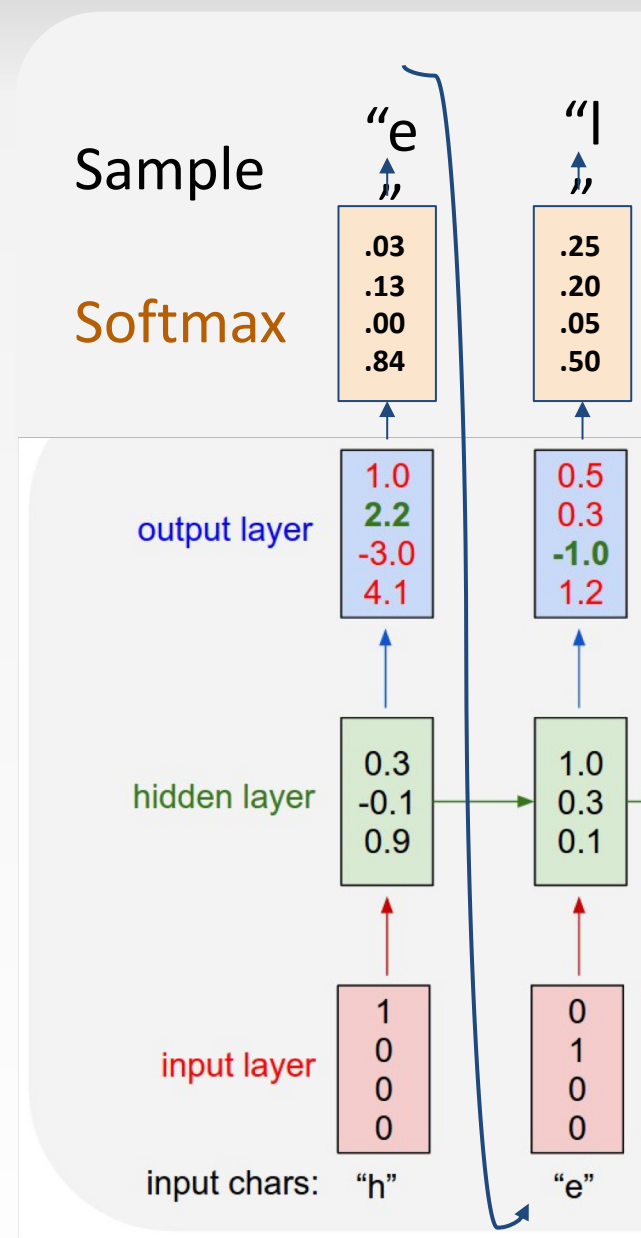
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EXAMPLE: CHARACTER-LEVEL LANGUAGE MODEL

Vocabulary:
[h,e,l,o]

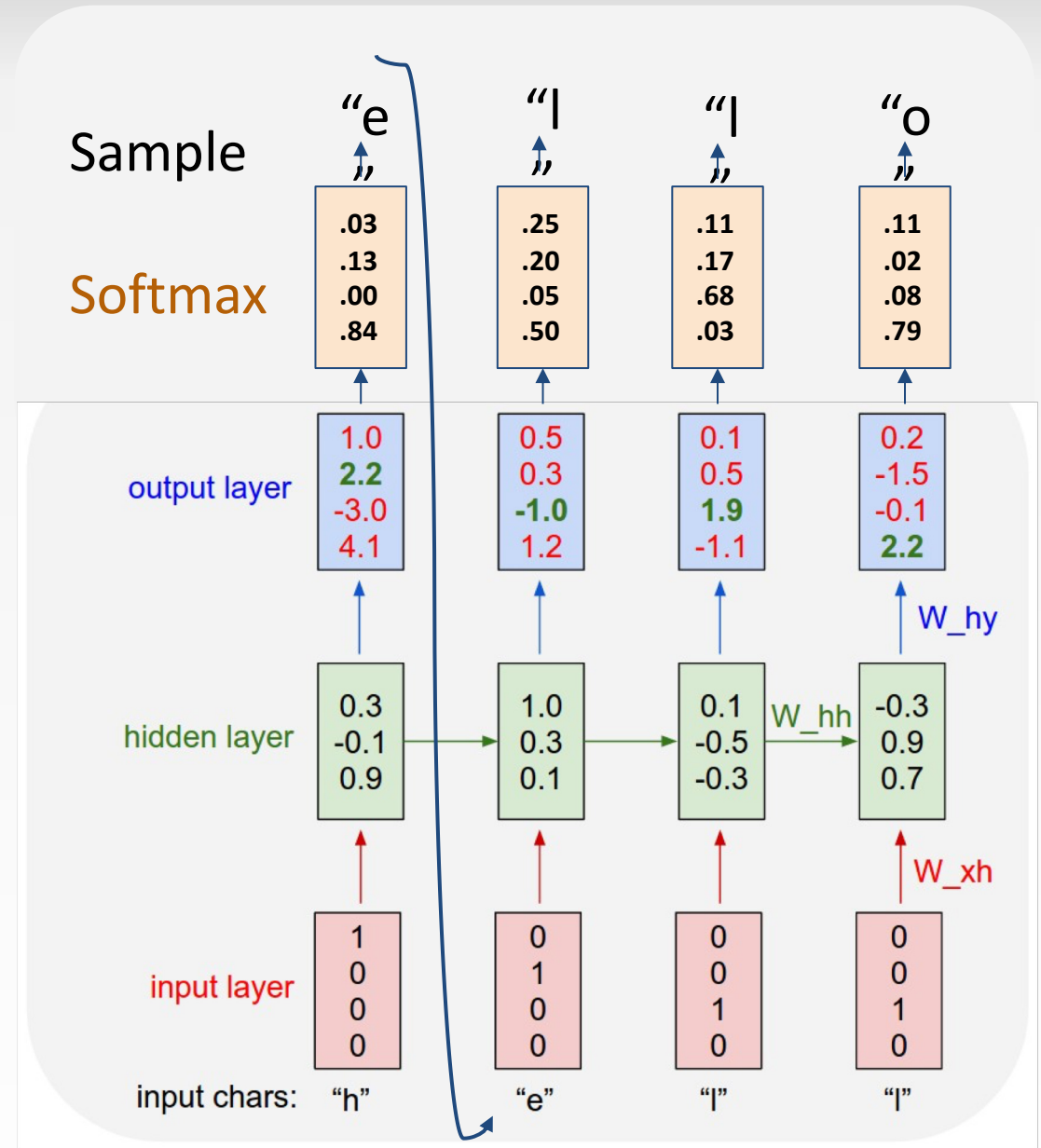
At test-time sample characters one at a time, feed back to model



EXAMPLE: CHARACTER-LEVEL LANGUAGE MODEL

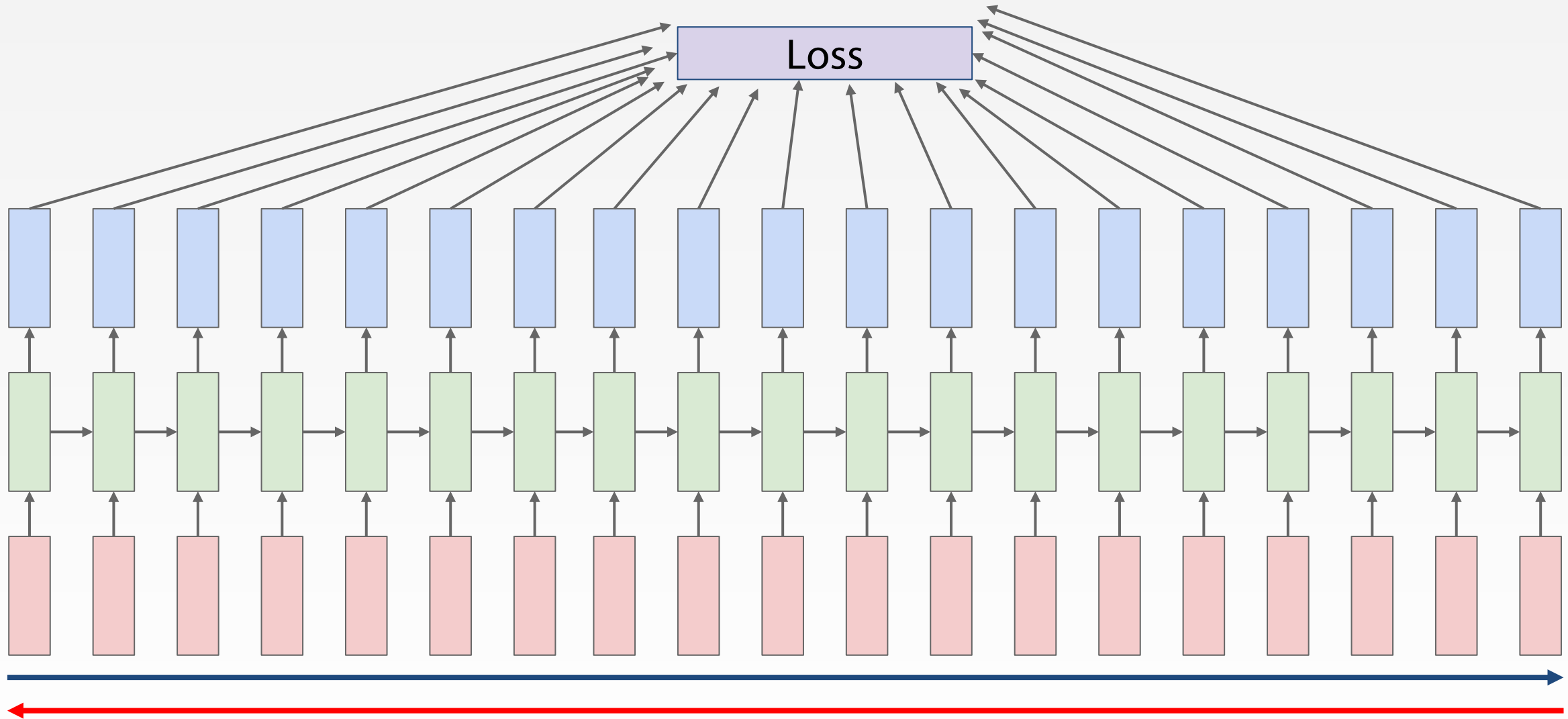
Vocabulary:
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At test-time sample characters one at a time, feed back to model

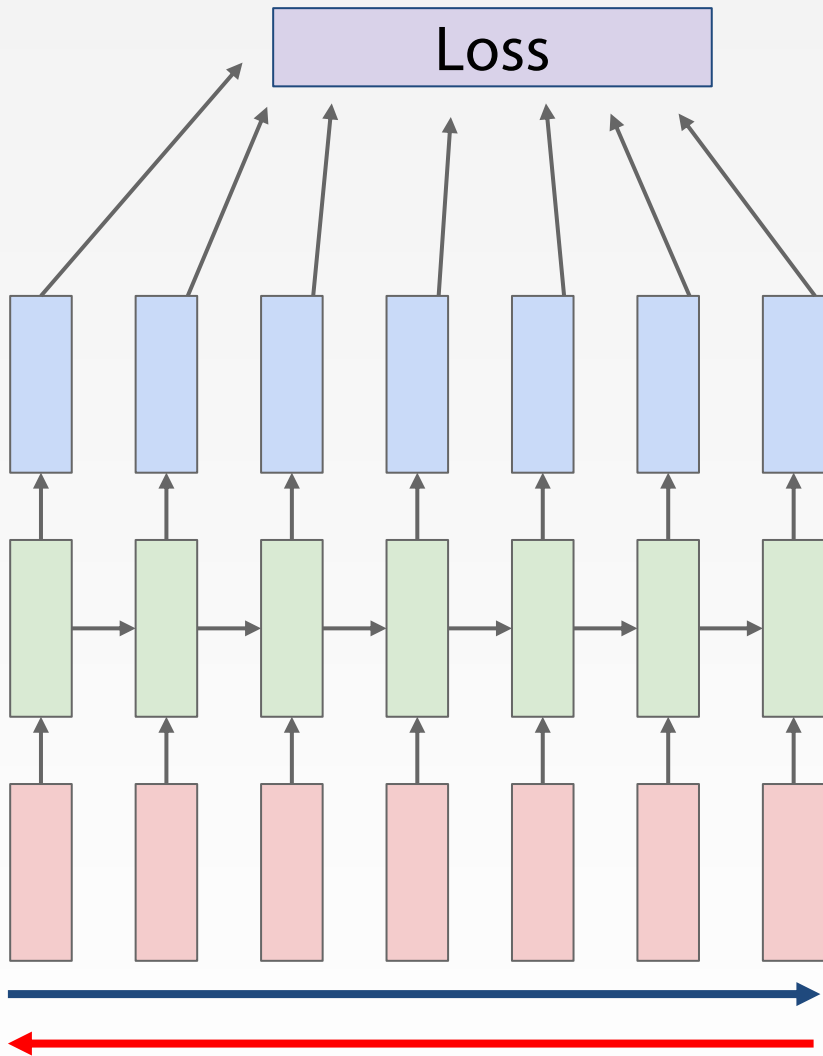


BACKPROPAGATION THROUGH TIME (BPTT)

Forward through entire sequence to compute loss, then backward through entire sequence to compute gradient

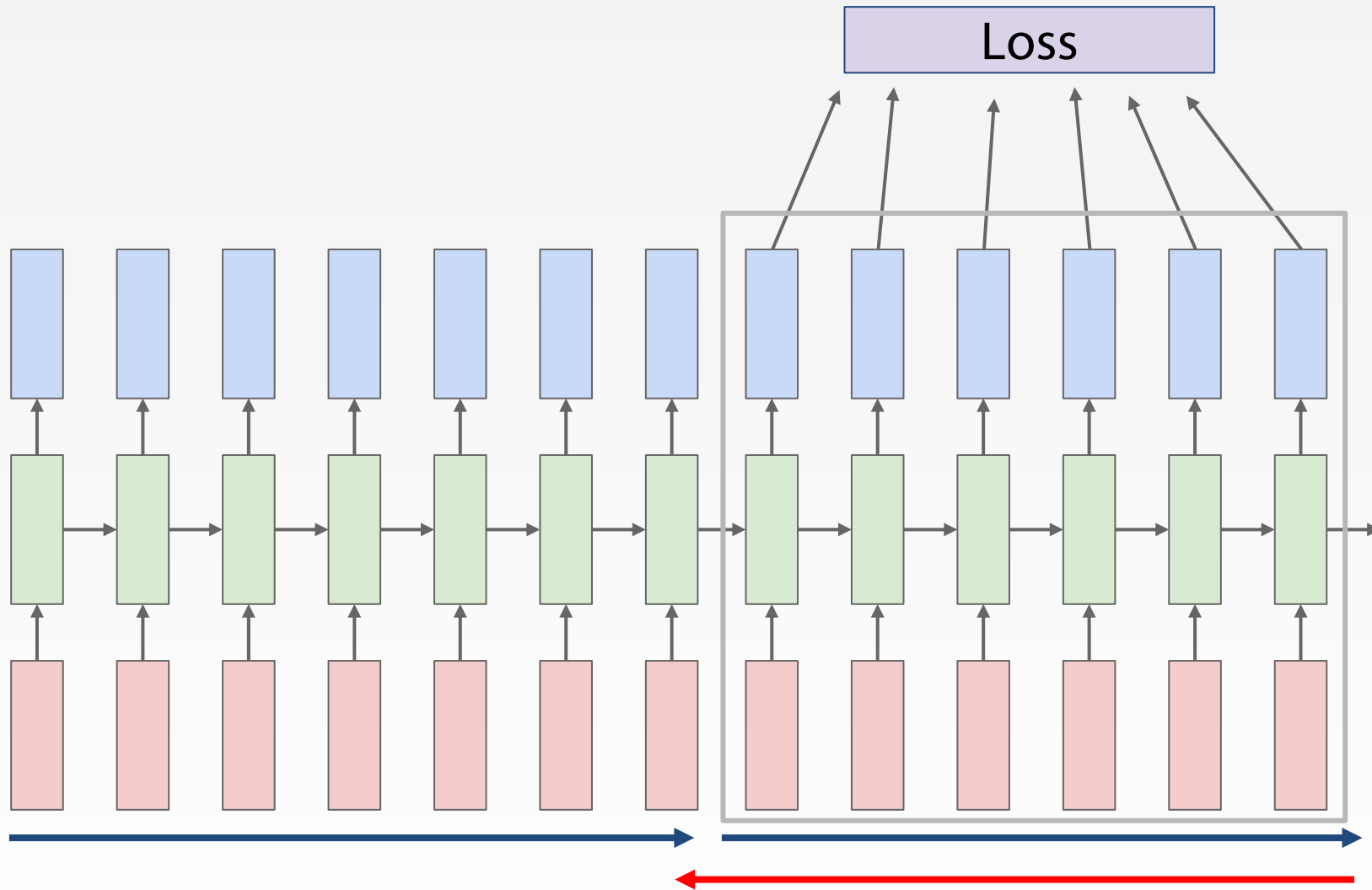


TRUNCATED BACKPROPAGATION THROUGH TIME



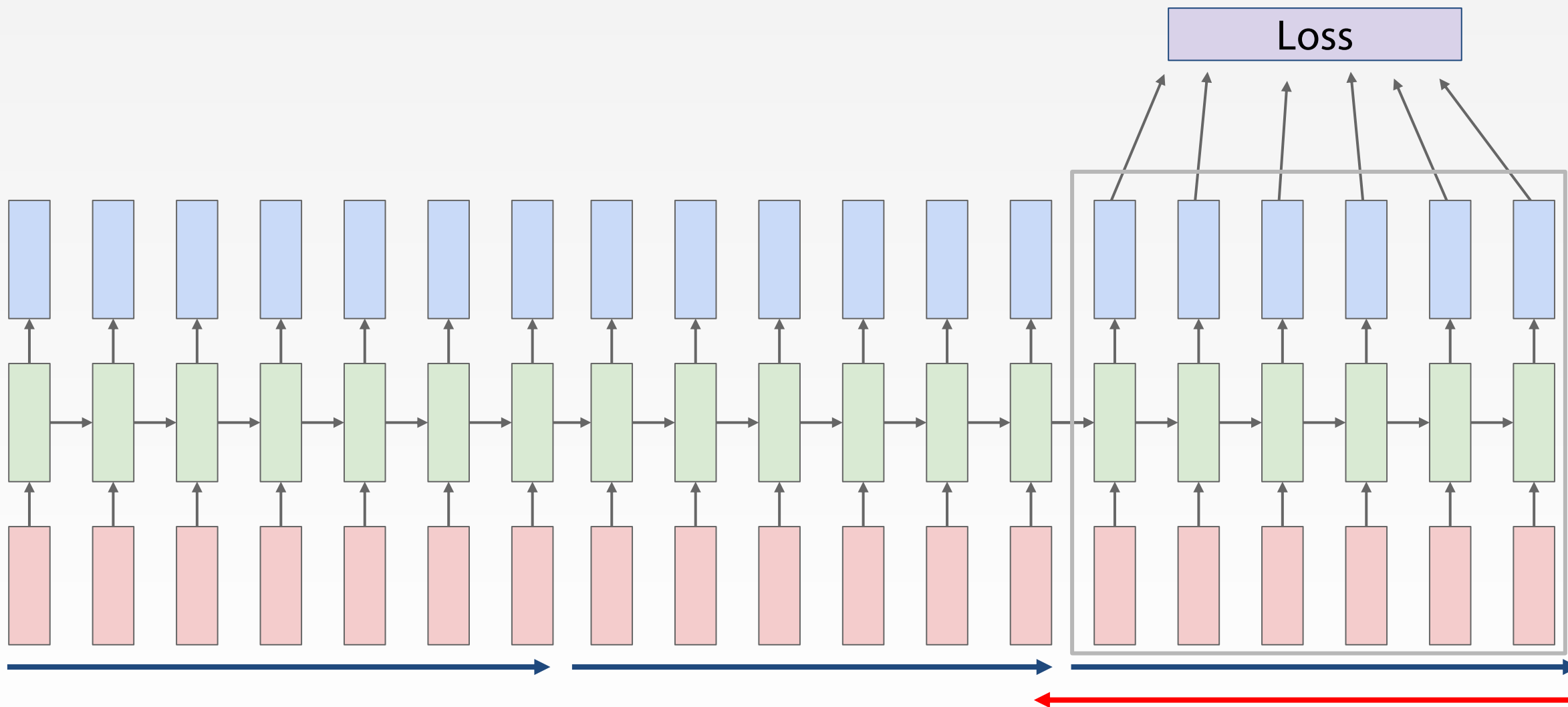
Run forward and backward through chunks of the sequence instead of whole sequence

TRUNCATED BACKPROPAGATION THROUGH TIME



Carry hidden states forward in time forever, but only backpropagate for some smaller number of steps

TRUNCATED BACKPROPAGATION THROUGH TIME



min-char-rnn.py gist: 112 lines of Python

```
1 """
2 Minimal character-level Vanilla RNN model. Written by Andrej Karpathy (@karpathy)
3 BSD License
4 """
5 import numpy as np
6
7 # data I/O
8 data = open('input.txt', 'r').read() # should be simple plain text file
9 chars = list(set(data))
10 data_size, vocab_size = len(data), len(chars)
11 print 'data has %d characters, %d unique.' % (data_size, vocab_size)
12 char_to_ix = { ch:i for i,ch in enumerate(chars) }
13 ix_to_char = { i:ch for i,ch in enumerate(chars) }
14
15 # hyperparameters
16 hidden_size = 100 # size of hidden layer of neurons
17 seq_length = 25 # number of steps to unroll the RNN for
18 learning_rate = 1e-1
19
20 # model parameters
21 wxh = np.random.randn(hidden_size, vocab_size)*0.01 # input to hidden
22 whh = np.random.randn(hidden_size, hidden_size)*0.01 # hidden to hidden
23 why = np.random.randn(vocab_size, hidden_size)*0.01 # hidden to output
24 bh = np.zeros((hidden_size, 1)) # hidden bias
25 by = np.zeros((vocab_size, 1)) # output bias
26
27 def lossFun(inputs, targets, hprev):
28     """
29     inputs, targets are both list of integers.
30     hprev is Hx1 array of initial hidden state
31     returns the loss, gradients on model parameters, and last hidden state
32     """
33     xs, hs, ys, ps = {}, {}, {}, {}
34     hs[-1] = np.copy(hprev)
35     loss = 0
36     # forward pass
37     for t in xrange(len(inputs)):
38         xs[t] = np.zeros((vocab_size,1)) # encode in 1-of-k representation
39         xs[t][inputs[t]] = 1
40         hs[t] = np.tanh(np.dot(wxh, xs[t]) + np.dot(whh, hs[t-1]) + bh) # hidden state
41         ys[t] = np.dot(why, hs[t]) + by # unnormalized log probabilities for next chars
42         ps[t] = np.exp(ys[t]) / np.sum(np.exp(ys[t])) # probabilities for next chars
43         loss += -np.log(ps[t][targets[t],0]) # softmax (cross-entropy loss)
44     # backward pass: compute gradients going backwards
45     dwdx, dwhh, dwhy = np.zeros_like(wxh), np.zeros_like(whh), np.zeros_like(why)
46     dbh, dby = np.zeros_like(bh), np.zeros_like(by)
47     dhnext = np.zeros_like(hs[0])
48     for t in reversed(xrange(len(inputs))):
49         dy = np.copy(ps[t])
50         dy[targets[t]] -= 1 # backprop into y
51         dwhy += np.dot(dy, hs[t].T)
52         dby += dy
53         dh = np.dot(why.T, dy) + dhnext # backprop into h
54         dhrw = (1 - hs[t] * hs[t]) * dh # backprop through tanh nonlinearity
55         dbh += dhrw
56         dwdx += np.dot(dhrw, xs[t].T)
57         dwhh += np.dot(dhrw, hs[t-1].T)
58         dhnext = np.dot(whh.T, dhrw)
59     for dparam in [dwdx, dwhh, dwhy, dbh, dby]:
60         np.clip(dparam, -5, 5, out=dparam) # clip to mitigate exploding gradients
61     return loss, dwdx, dwhh, dwhy, dbh, dby, hs[len(inputs)-1]
```

```
63 def sample(h, seed_ix, n):
64     """
65     sample a sequence of integers from the model
66     h is memory state, seed_ix is seed letter for first time step
67     """
68     x = np.zeros((vocab_size, 1))
69     x[seed_ix] = 1
70     ixes = []
71     for t in xrange(n):
72         h = np.tanh(np.dot(wxh, x) + np.dot(whh, h) + bh)
73         y = np.dot(why, h) + by
74         p = np.exp(y) / np.sum(np.exp(y))
75         ix = np.random.choice(range(vocab_size), p=p.ravel())
76         x = np.zeros((vocab_size, 1))
77         x[ix] = 1
78         ixes.append(ix)
79     return ixes
80
81 n, p = 0, 0
82 mwxh, mwhh, mwhy = np.zeros_like(wxh), np.zeros_like(whh), np.zeros_like(why)
83 mbh, mby = np.zeros_like(bh), np.zeros_like(by) # memory variables for Adagrad
84 smooth_loss = -np.log(1.0/vocab_size)*seq_length # loss at iteration 0
85 while True:
86     # prepare inputs (we're sweeping from left to right in steps seq_length long)
87     if p+seq_length+1 >= len(data) or n == 0:
88         hprev = np.zeros((hidden_size,1)) # reset RNN memory
89         p = 0 # go from start of data
90     inputs = [char_to_ix[ch] for ch in data[p:p+seq_length]]
91     targets = [char_to_ix[ch] for ch in data[p+1:p+seq_length+1]]
92
93     # sample from the model now and then
94     if n % 100 == 0:
95         sample_ix = sample(hprev, inputs[0], 200)
96         txt = ''.join(ix_to_char[ix] for ix in sample_ix)
97         print '----\n %s \n----' % (txt, )
98
99     # forward seq_length characters through the net and fetch gradient
100     loss, dwdx, dwhh, dwhy, dbh, dby, hprev = lossFun(inputs, targets, hprev)
101     smooth_loss = smooth_loss * 0.999 + loss * 0.001
102     if n % 100 == 0: print 'iter %d, loss: %f' % (n, smooth_loss) # print progress
103
104     # perform parameter update with Adagrad
105     for param, dparam, mem in zip([wxh, whh, why, bh, by],
106                                 [dwdx, dwhh, dwhy, dbh, dby],
107                                 [mwxh, mwhh, mwhy, mbh, mby]):
108         mem += dparam * dparam
109         param += -learning_rate * dparam / np.sqrt(mem + 1e-8) # adagrad update
110
111     p += seq_length # move data pointer
112     n += 1 # iteration counter
```

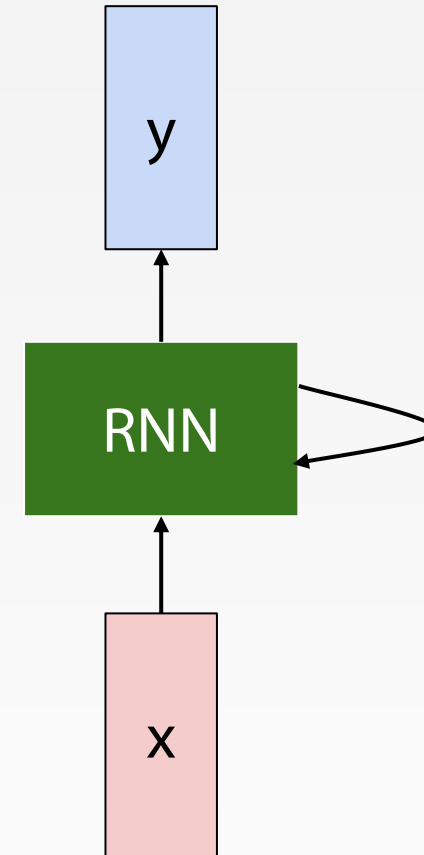
(<https://gist.github.com/karpathy/d4dee566867f8291f086>)

THE SONNETS

by William Shakespeare

From fairest creatures we desire increase,
That thereby beauty's rose might never die,
But as the ripener should by time decease,
His tender heir might bear his memory:
But thou, contracted to thine own bright eyes,
Feed'st thy light's flame with self-substantial fuel,
Making a famine where abundance lies,
Thyself thy foe, to thy sweet self too cruel:
Thou that art now the world's fresh ornament,
And only herald to the gaudy spring,
Within thine own bud buriest thy content,
And tender churl mak'st waste in niggarding:
 Pity the world, or else this glutton be,
 To eat the world's due, by the grave and thee.

When forty winters shall besiege thy brow,
And dig deep trenches in thy beauty's field,
Thy youth's proud livery so gazed on now,
Will be a tatter'd weed of small worth held:
Then being asked, where all thy beauty lies,
Where all the treasure of thy lusty days;
To say, within thine own deep sunken eyes,
Were an all-eating shame, and thriftless praise.
How much more praise deserv'd thy beauty's use,
If thou couldst answer 'This fair child of mine
Shall sum my count, and make my old excuse,'
Proving his beauty by succession thine!
 This were to be new made when thou art old,
 And see thy blood warm when thou feel'st it cold.



at first:

tyntd-iafhatawiaoihrdemot lytdws e ,tfti, astai f ogoh eoase rrranbyne 'nhthnee e
plia tklrqd t o idoe ns,smtt h ne etie h,hregtrs nigtike,aoaenns lng

train more

"Tmont thithey" fomesscerliund
Keushey. Thom here
sheulke, anmerenith ol sivh I lalterthend Bleipile shuwv fil on aseterlome
coaniogennc Phe lism thond hon at. MeiDimorotion in ther thize."

train more

Aftair fall unsuch that the hall for Prince Velzonski's that me of
her hearly, and behs to so arwage fiving were to it beloge, pavu say falling misfort
how, and Gogition is so overelical and offer.

train more

"Why do what that day," replied Natasha, and wishing to himself the fact the
princess, Princess Mary was easier, fed in had oftened him.
Pierre aking his soul came to the packs and drove up his father-in-law women.

PANDARUS:

Alas, I think he shall be come approached and the day
When little strain would be attain'd into being never fed,
And who is but a chain and subjects of his death,
I should not sleep.

Second Senator:

They are away this miseries, produced upon my soul,
Breaking and strongly should be buried, when I perish
The earth and thoughts of many states.

DUKE VINCENTIO:

Well, your wit is in the care of side and that.

Second Lord:

They would be ruled after this chamber, and
my fair nudes begun out of the fact, to be conveyed,
Whose noble souls I'll have the heart of the wars.

Clown:

Come, sir, I will make did behold your worship.

VIOLA:

I'll drink it.

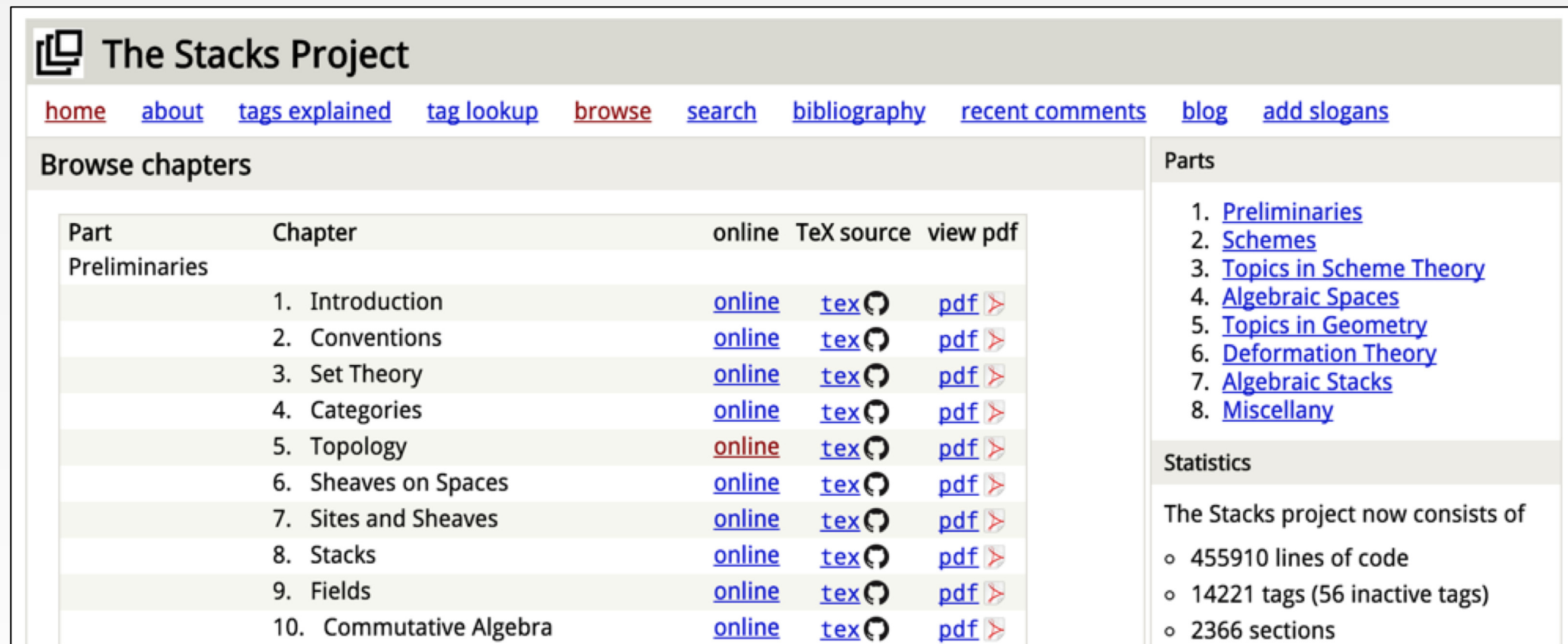
VIOLA:

Why, Salisbury must find his flesh and thought
That which I am not apt, not a man and in fire,
To show the reining of the raven and the wars
To grace my hand reproach within, and not a fair are hand,
That Caesar and my goodly father's world;
When I was heaven of presence and our fleets,
We spare with hours, but cut thy council I am great,
Murdered and by thy master's ready there
My power to give thee but so much as hell:
Some service in the noble bondman here,
Would show him to her wine.

KING LEAR:

O, if you were a feeble sight, the courtesy of your law,
Your sight and several breath, will wear the gods
With his heads, and my hands are wonder'd at the deeds,
So drop upon your lordship's head, and your opinion
Shall be against your honour.

THE STACKS PROJECT: OPEN SOURCE ALGEBRAIC GEOMETRY TEXTBOOK



The Stacks Project

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Statistics

The Stacks project now consists of

- 455910 lines of code
- 14221 tags (56 inactive tags)
- 2366 sections

Latex source



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For $\bigoplus_{n=1, \dots, m}$ where $\mathcal{L}_{m, \bullet} = 0$, hence we can find a closed subset \mathcal{H} in \mathcal{H} and any sets \mathcal{F} on X , U is a closed immersion of S , then $U \rightarrow T$ is a separated algebraic space.

Proof. Proof of (1). It also start we get

$$S = \text{Spec}(R) = U \times_X U \times_X U$$

and the comparicoly in the fibre product covering we have to prove the lemma generated by $\coprod Z \times_U U \rightarrow V$. Consider the maps M along the set of points Sch_{fppf} and $U \rightarrow U$ is the fibre category of S in U in Section, ?? and the fact that any U affine, see Morphisms, Lemma ?? . Hence we obtain a scheme S and any open subset $W \subset U$ in $Sh(G)$ such that $\text{Spec}(R') \rightarrow S$ is smooth or an

$$U = \bigcup U_i \times_{S_i} U_i$$

which has a nonzero morphism we may assume that f_i is of finite presentation over S . We claim that $\mathcal{O}_{X, x}$ is a scheme where $x, x', s'' \in S'$ such that $\mathcal{O}_{X, x'} \rightarrow \mathcal{O}'_{X', x'}$ is separated. By Algebra, Lemma ?? we can define a map of complexes $GL_{S'}(x'/S'')$ and we win. \square

To prove study we see that $\mathcal{F}|_U$ is a covering of \mathcal{X}' , and \mathcal{T}_i is an object of $\mathcal{F}_{X/S}$ for $i > 0$ and \mathcal{F}_p exists and let \mathcal{F}_i be a presheaf of \mathcal{O}_X -modules on \mathcal{C} as a \mathcal{F} -module. In particular $\mathcal{F} = U/\mathcal{F}$ we have to show that

$$\widetilde{M}^\bullet = \mathcal{I}^\bullet \otimes_{\text{Spec}(k)} \mathcal{O}_{S, s} - i_X^{-1} \mathcal{F}$$

is a unique morphism of algebraic stacks. Note that

$$\text{Arrows} = (Sch/S)_{fppf}^{opp}, (Sch/S)_{fppf}$$

and

$$V = \Gamma(S, \mathcal{O}) \mapsto (U, \text{Spec}(A))$$

is an open subset of X . Thus U is affine. This is a continuous map of X is the inverse, the groupoid scheme S .

Proof. See discussion of sheaves of sets. \square

The result for prove any open covering follows from the less of Example ?? . It may replace S by $X_{spaces, \acute{e}tale}$ which gives an open subspace of X and T equal to S_{Zar} , see Descent, Lemma ?? . Namely, by Lemma ?? we see that R is geometrically regular over S .

Lemma 0.1. Assume (3) and (3) by the construction in the description.

Suppose $X = \lim |X|$ (by the formal open covering X and a single map $\underline{\text{Proj}}_X(\mathcal{A}) = \text{Spec}(B)$ over U compatible with the complex

$$\text{Set}(\mathcal{A}) = \Gamma(X, \mathcal{O}_{X, \mathcal{O}_X}).$$

When in this case of to show that $\mathcal{Q} \rightarrow \mathcal{C}_{Z/X}$ is stable under the following result in the second conditions of (1), and (3). This finishes the proof. By Definition ?? (without element is when the closed subschemes are catenary. If T is surjective we may assume that T is connected with residue fields of S . Moreover there exists a closed subspace $Z \subset X$ of X where U in X' is proper (some defining as a closed subset of the uniqueness it suffices to check the fact that the following theorem

(1) f is locally of finite type. Since $S = \text{Spec}(R)$ and $Y = \text{Spec}(R)$.

Proof. This is form all sheaves of sheaves on X . But given a scheme U and a surjective étale morphism $U \rightarrow X$. Let $U \cap U = \coprod_{i=1, \dots, n} U_i$ be the scheme X over S at the schemes $X_i \rightarrow X$ and $U = \lim_i X_i$. \square

The following lemma surjective restrocomposes of this implies that $\mathcal{F}_{x_0} = \mathcal{F}_{x_0} = \mathcal{F}_{\mathcal{X}, \dots, 0}$.

Lemma 0.2. Let X be a locally Noetherian scheme over S , $E = \mathcal{F}_{X/S}$. Set $\mathcal{I} = \mathcal{J}_1 \subset \mathcal{I}'_n$. Since $\mathcal{I}^n \subset \mathcal{I}^n$ are nonzero over $i_0 \leq \mathfrak{p}$ is a subset of $\mathcal{J}_{n, 0} \circ \bar{A}_2$ works.

Lemma 0.3. In Situation ?? . Hence we may assume $\mathfrak{q}' = 0$.

Proof. We will use the property we see that \mathfrak{p} is the next functor (??). On the other hand, by Lemma ?? we see that

$$D(\mathcal{O}_{X'}) = \mathcal{O}_X(D)$$

where K is an F -algebra where δ_{n+1} is a scheme over S . \square

Proof. Omitted. □

Lemma 0.1. Let \mathcal{C} be a set of the construction.

Let \mathcal{C} be a gerber covering. Let \mathcal{F} be a quasi-coherent sheaves of \mathcal{O} -modules. We have to show that

$$\mathcal{O}_{\mathcal{O}_X} = \mathcal{O}_X(\mathcal{L})$$

Proof. This is an algebraic space with the composition of sheaves \mathcal{F} on $X_{\acute{e}tale}$ we have

$$\mathcal{O}_X(\mathcal{F}) = \{morph_1 \times_{\mathcal{O}_X} (\mathcal{G}, \mathcal{F})\}$$

where \mathcal{G} defines an isomorphism $\mathcal{F} \rightarrow \mathcal{F}$ of \mathcal{O} -modules. □

Lemma 0.2. This is an integer \mathcal{Z} is injective.

Proof. See Spaces, Lemma ??.

Lemma 0.3. Let S be a scheme. Let X be a scheme and X is an affine open covering. Let $\mathcal{U} \subset \mathcal{X}$ be a canonical and locally of finite type. Let X be a scheme. Let X be a scheme which is equal to the formal complex.

The following to the construction of the lemma follows.

Let X be a scheme. Let X be a scheme covering. Let

$$b : X \rightarrow Y' \rightarrow Y \rightarrow Y \rightarrow Y' \times_X Y \rightarrow X.$$

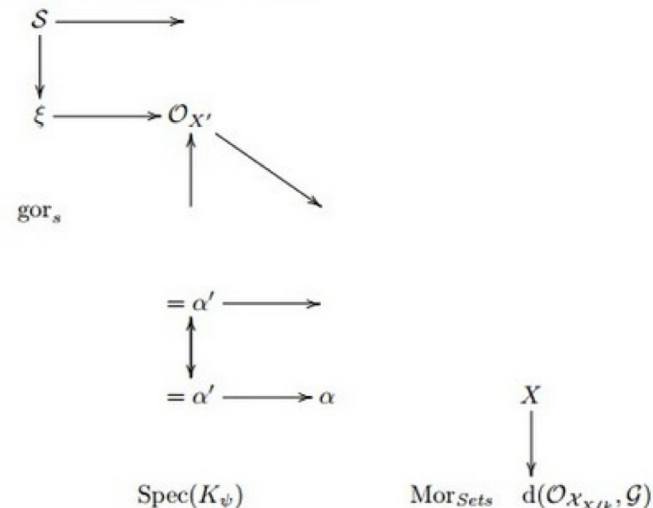
be a morphism of algebraic spaces over S and Y .

Proof. Let X be a nonzero scheme of X . Let X be an algebraic space. Let \mathcal{F} be a quasi-coherent sheaf of \mathcal{O}_X -modules. The following are equivalent

- (1) \mathcal{F} is an algebraic space over S .
- (2) If X is an affine open covering.

Consider a common structure on X and X the functor $\mathcal{O}_X(U)$ which is locally of finite type. □

This since $\mathcal{F} \in \mathcal{F}$ and $x \in \mathcal{G}$ the diagram



is a limit. Then \mathcal{G} is a finite type and assume S is a flat and \mathcal{F} and \mathcal{G} is a finite type f_* . This is of finite type diagrams, and

- the composition of \mathcal{G} is a regular sequence,
- $\mathcal{O}_{X'}$ is a sheaf of rings.

□

Proof. We have see that $X = \text{Spec}(R)$ and \mathcal{F} is a finite type representable by algebraic space. The property \mathcal{F} is a finite morphism of algebraic stacks. Then the cohomology of X is an open neighbourhood of U . □

Proof. This is clear that \mathcal{G} is a finite presentation, see Lemmas ??.

A reduced above we conclude that U is an open covering of \mathcal{C} . The functor \mathcal{F} is a “field

$$\mathcal{O}_{X,x} \rightarrow \mathcal{F}_{\bar{x}} \rightarrow -1(\mathcal{O}_{X_{\acute{e}tale}}) \rightarrow \mathcal{O}_{X_t}^{-1} \mathcal{O}_{X_\lambda}(\mathcal{O}_{X_\eta}^{\bar{v}})$$

is an isomorphism of covering of \mathcal{O}_{X_t} . If \mathcal{F} is the unique element of \mathcal{F} such that X is an isomorphism.

The property \mathcal{F} is a disjoint union of Proposition ?? and we can filtered set of presentations of a scheme \mathcal{O}_X -algebra with \mathcal{F} are opens of finite type over S .

If \mathcal{F} is a scheme theoretic image points. □

If \mathcal{F} is a finite direct sum \mathcal{O}_{X_λ} is a closed immersion, see Lemma ??.

This is a sequence of \mathcal{F} is a similar morphism.



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branch: master -

linux / +



Merge branch 'drm-fixes' of git://people.freedesktop.org/~airlied/linux



torvalds authored 9 hours ago

latest commit 4b1786927d

Documentation	Merge git://git.kernel.org/pub/scm/linux/kernel/git/nab/target-pending	6 days ago
arch	Merge branch 'x86-urgent-for-linus' of git://git.kernel.org/pub/scm/...	a day ago
block	block: discard bdi_unregister() in favour of bdi_destroy()	9 days ago
crypto	Merge git://git.kernel.org/pub/scm/linux/kernel/git/herbert/crypto-2.6	10 days ago
drivers	Merge branch 'drm-fixes' of git://people.freedesktop.org/~airlied/linux	9 hours ago
firmware	firmware/ihex2fw.c: restore missing default in switch statement	2 months ago
fs	vfs: read file_handle only once in handle_to_path	4 days ago
include	Merge branch 'perf-urgent-for-linus' of git://git.kernel.org/pub/scm/...	a day ago
init	init: fix regression by supporting devices with major:minor:offset fo...	a month ago
ipc	Merge branch 'for-linus' of git://git.kernel.org/pub/scm/linux/kernel...	a month ago

Code

Pull requests 74

Pulse

Graphs

HTTPS clone URL

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```

static void do_command(struct seq_file *m, void *v)
{
    int column = 32 << (cmd[2] & 0x80);
    if (state)
        cmd = (int)(int_state ^ (in_8(&ch->ch_flags) & Cmd) ? 2 : 1);
    else
        seq = 1;
    for (i = 0; i < 16; i++) {
        if (k & (1 << i))
            pipe = (in_use & UMXTHREAD_UNCCA) +
                ((count & 0x00000000ffffffff) & 0x0000000f) << 8;
        if (count == 0)
            sub(pid, ppc_md.kexec_handle, 0x20000000);
        pipe_set_bytes(i, 0);
    }
    /* Free our user pages pointer to place camera if all dash */
    subsystem_info = &of_changes[PAGE_SIZE];
    rek_controls(offset, idx, &soffset);
    /* Now we want to deliberately put it to device */
    control_check_polarity(&context, val, 0);
    for (i = 0; i < COUNTER; i++)
        seq_puts(s, "policy ");
}

```

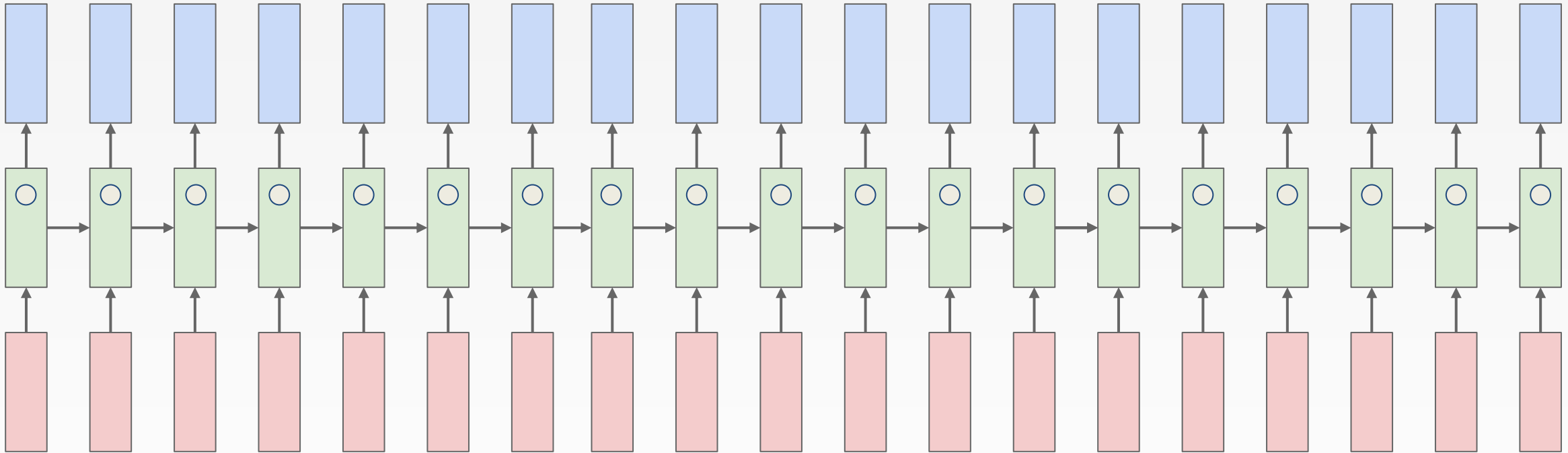
Generated C code

```
/*
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 * Inc., 675 Mass Ave, Cambridge, MA 02139, USA.
 */
```

```
#include <linux/kexec.h>
#include <linux/errno.h>
#include <linux/io.h>
#include <linux/platform_device.h>
#include <linux/multi.h>
#include <linux/ckevent.h>
```

```
#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system_info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>
```

SEARCHING FOR INTERPRETABLE CELLS



Karpathy, Johnson, and Fei-Fei: Visualizing and Understanding Recurrent Networks, ICLR Workshop 2016

SEARCHING FOR INTERPRETABLE CELLS

```
/* Unpack a filter field's string representation from user-space
 * buffer. */
char *audit_unpack_string(void **bufp, size_t *remain, size_t len)
{
    char *str;
    if (!*bufp || (len == 0) || (len > *remain))
        return ERR_PTR(-EINVAL);
    /* Of the currently implemented string fields, PATH_MAX
     * defines the longest valid length.
     */
}
```

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SEARCHING FOR INTERPRETABLE CELLS

```
/* Unpack a filter field's string representation from user-space
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    /* Of the currently implemented string fields, PATH_MAX
     * defines the longest valid length.
     */
}
```

quote detection cell

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SEARCHING FOR INTERPRETABLE CELLS

Cell sensitive to position in line:

The sole importance of the crossing of the Berezina lies in the fact that it plainly and indubitably proved the fallacy of all the plans for cutting off the enemy's retreat and the soundness of the only possible line of action--the one Kutuzov and the general mass of the army demanded--namely, simply to follow the enemy up. The French crowd fled at a continually increasing speed and all its energy was directed to reaching its goal. It fled like a wounded animal and it was impossible to block its path. This was shown not so much by the arrangements it made for crossing as by what took place at the bridges. When the bridges broke down, unarmed soldiers, people from Moscow and women with children who were with the French transport, all--carried on by vis inertiae--pressed forward into boats and into the ice-covered water and did not, surrender.

line length tracking cell

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SEARCHING FOR INTERPRETABLE CELLS

```
static int __dequeue_signal(struct sigpending *pending, sigset_t *mask,
                           siginfo_t *info)
{
    int sig = next_signal(pending, mask);
    if (sig) {
        if (current->notifier) {
            if (sigismember(current->notifier_mask, sig)) {
                if (!(current->notifier)(current->notifier_data)) {
                    clear_thread_flag(TIF_SIGPENDING);
                    return 0;
                }
            }
        }
        collect_signal(sig, pending, info);
    }
    return sig;
}
```

if statement cell

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SEARCHING FOR INTERPRETABLE CELLS

Cell that turns on inside comments and quotes:

```
/* Duplicate LSM field information. The lsm_rule is opaque, so
 * re-initialized. */
static inline int audit_dupe_lsm_field(struct audit_field *df,
                                     struct audit_field *sf)
{
    int ret = 0;
    char *lsm_str;
    /* our own copy of lsm_str */
    lsm_str = kstrdup(sf->lsm_str, GFP_KERNEL);
    if (unlikely(!lsm_str))
        return -ENOMEM;
    df->lsm_str = lsm_str;
    /* our own (refreshed) copy of lsm_rule */
    ret = security_audit_rule_init(df->type, df->op, df->lsm_str,
                                  (void *)&df->lsm_rule);
    /* Keep currently invalid fields around in case they
     * become valid after a policy reload. */
    if (ret == -EINVAL) {
        pr_warn("audit rule for LSM '%s' is invalid\n",
              df->lsm_str);
        ret = 0;
    }
    return ret;
}
```

quote/comment cell

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SEARCHING FOR INTERPRETABLE CELLS

```
#ifdef CONFIG_AUDITSYSCALL
static inline int audit_match_class_bits(int class, u32 *mask)
{
    int i;
    if (classes[class]) {
        for (i = 0; i < AUDIT_BITMASK_SIZE; i++)
            if (mask[i] & classes[class][i])
                return 0;
    }
    return 1;
}
```

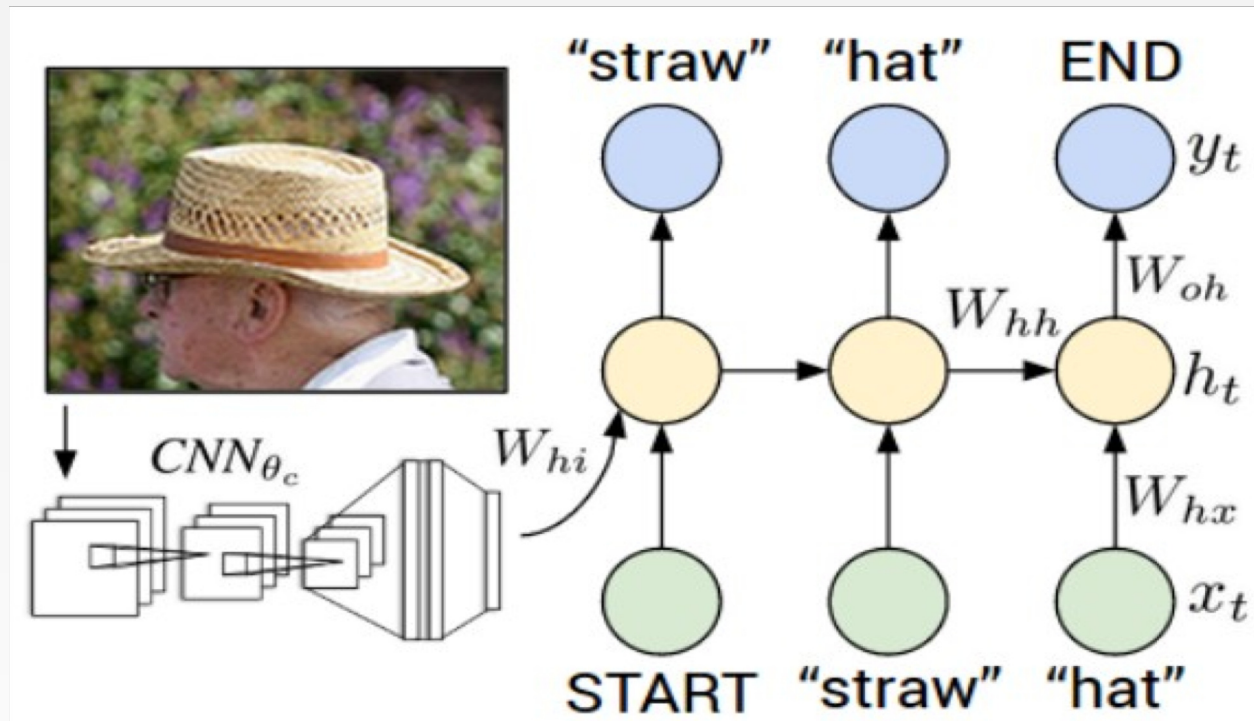
code depth cell

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IMAGE CAPTIONING

IMAGE CAPTIONING



Explain Images with Multimodal Recurrent Neural Networks, Mao et al.

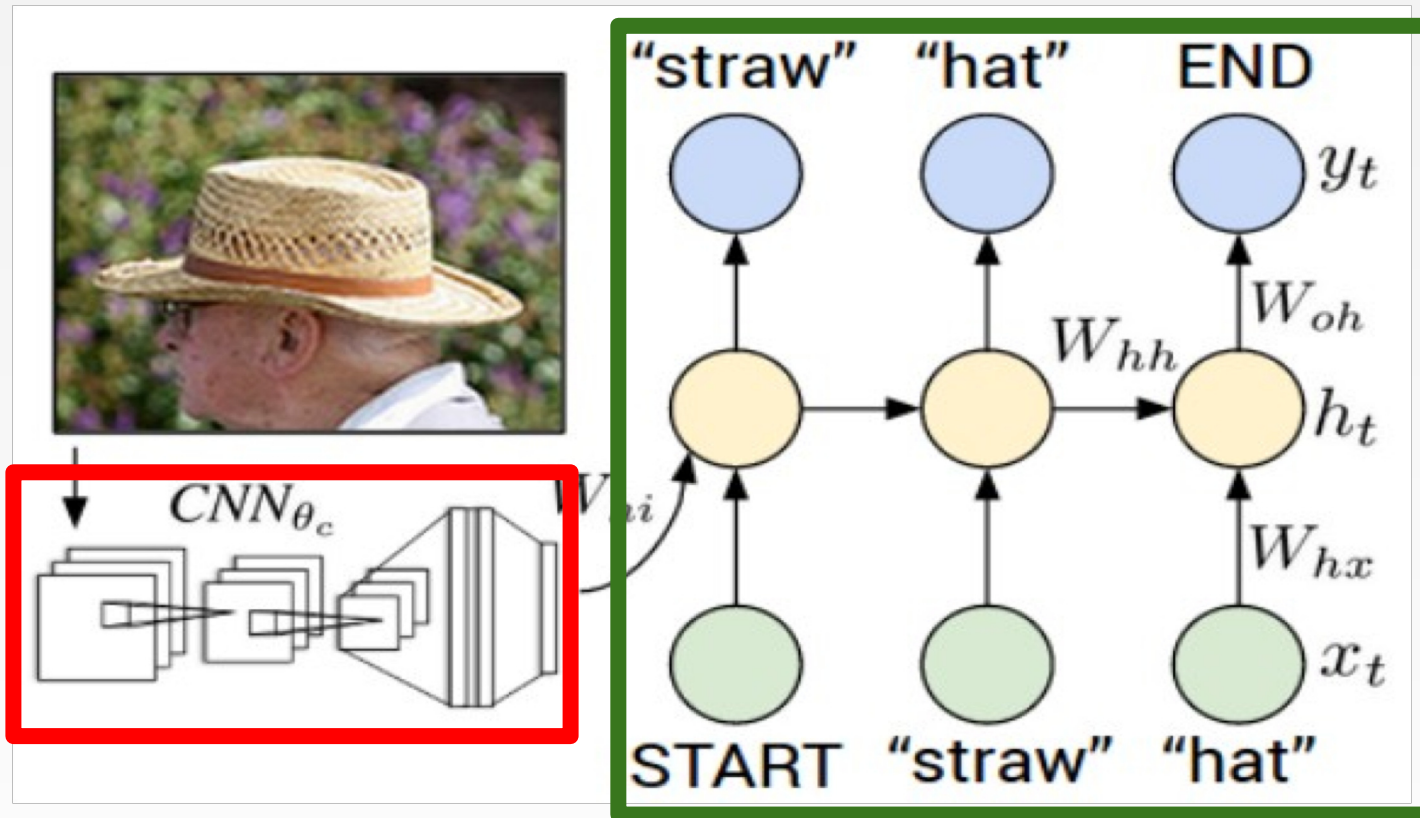
Deep Visual-Semantic Alignments for Generating Image Descriptions, Karpathy and Fei-Fei

Show and Tell: A Neural Image Caption Generator, Vinyals et al.

Long-term Recurrent Convolutional Networks for Visual Recognition and Description, Donahue et al.

Learning a Recurrent Visual Representation for Image Caption Generation, Chen and Zitnick

Recurrent Neural Network



Convolutional Neural Network



test image



test image

image

conv-64

conv-64

maxpool

conv-128

conv-128

maxpool

conv-256

conv-256

maxpool

conv-512

conv-512

maxpool

conv-512

conv-512

maxpool

FC-4096

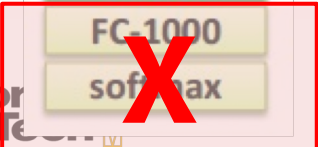
FC-4096

FC-1000

softmax

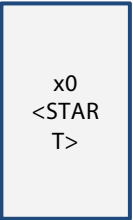


test image





test image



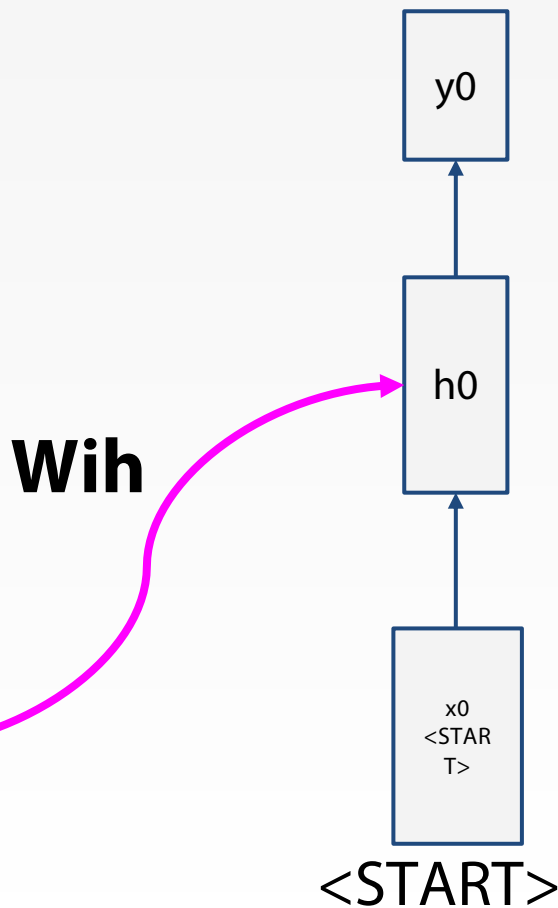
<START>



V



test image

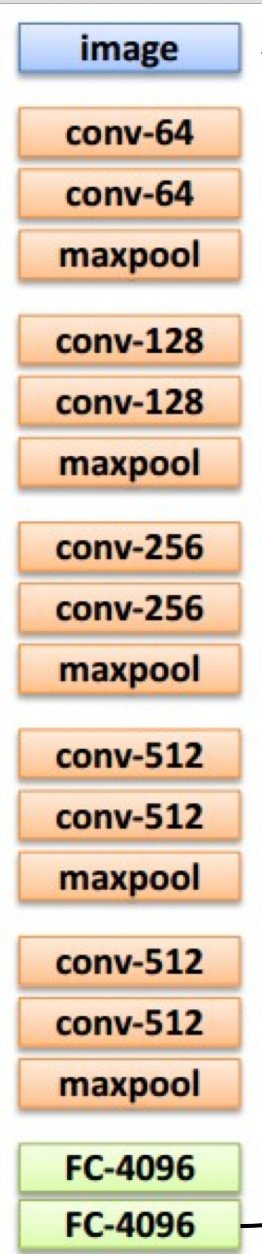


before:

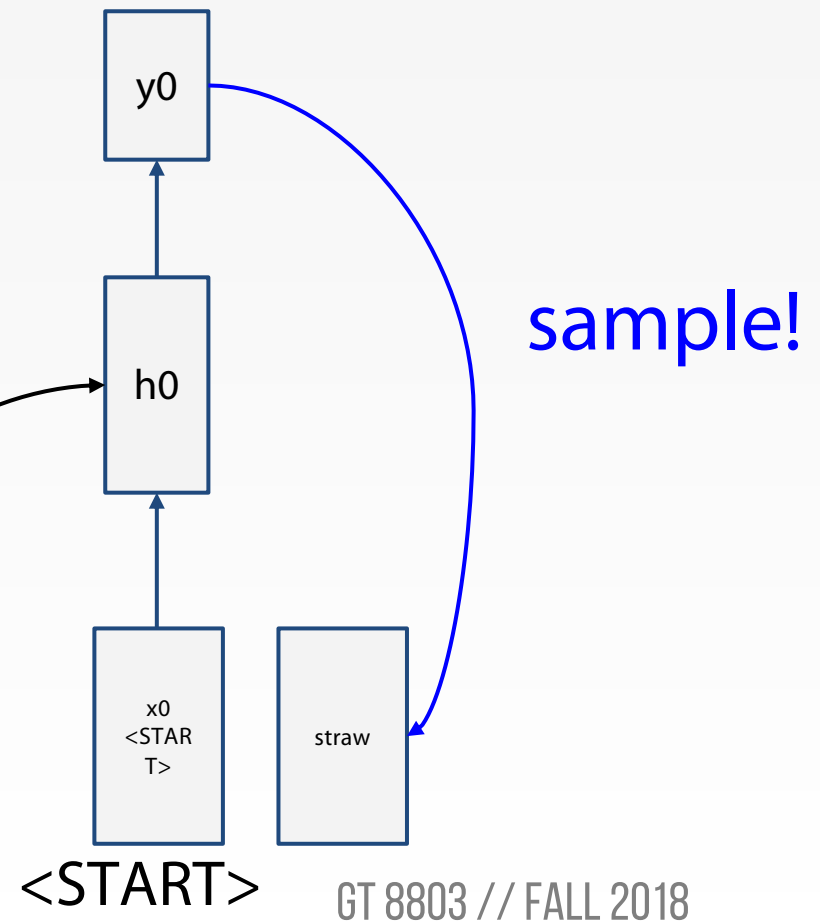
$$h = \tanh(W_{xh} * x + W_{hh} * h)$$

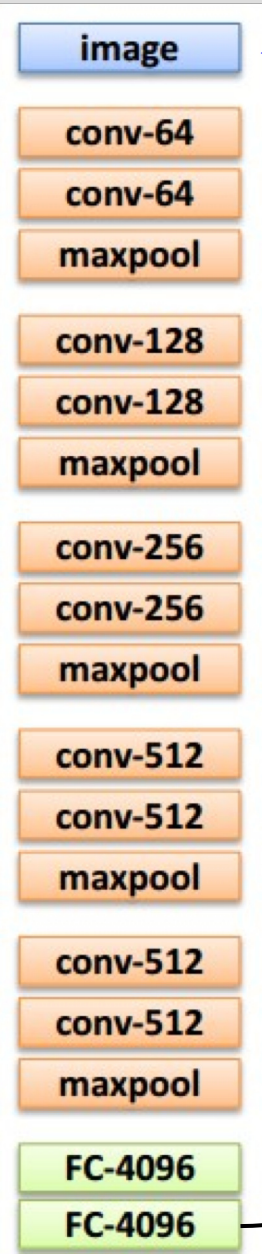
now:

$$h = \tanh(W_{xh} * x + W_{hh} * h + W_{ih} * v)$$

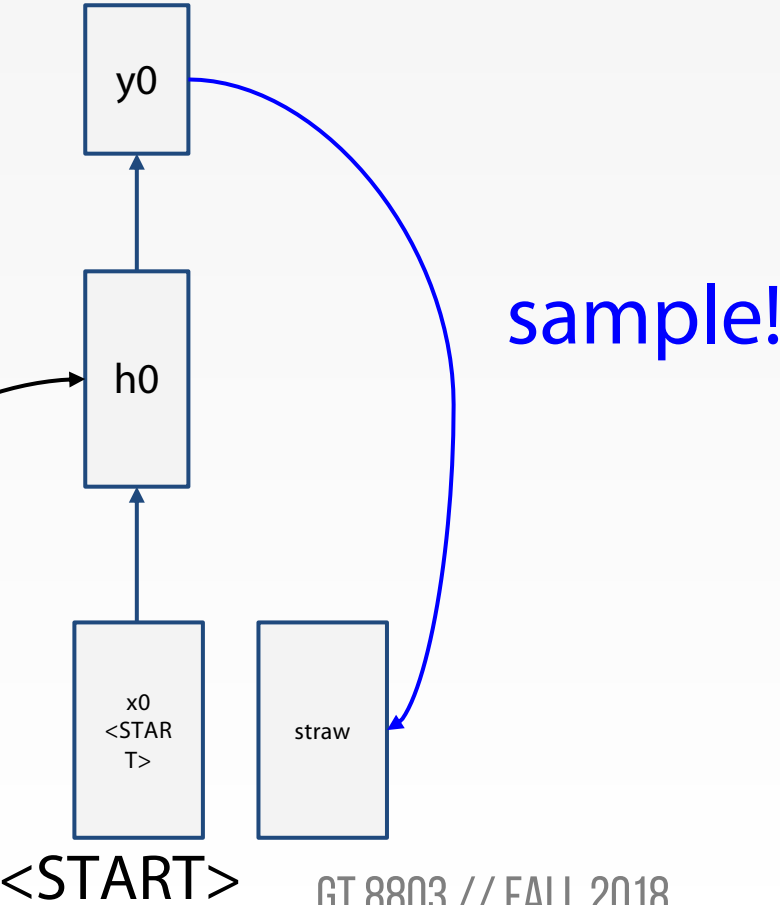


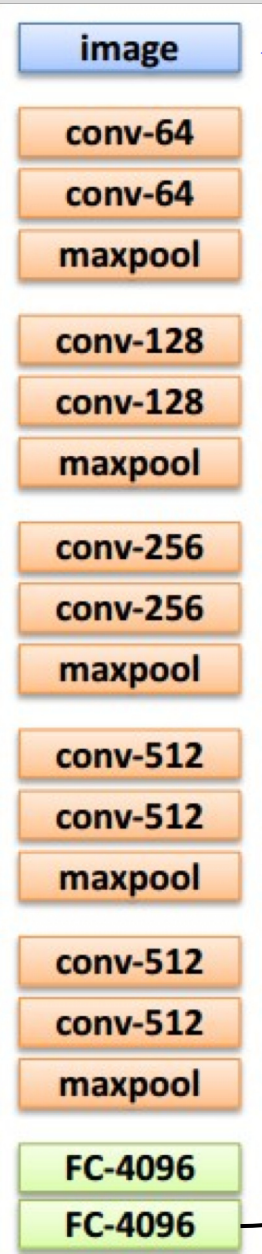
test image



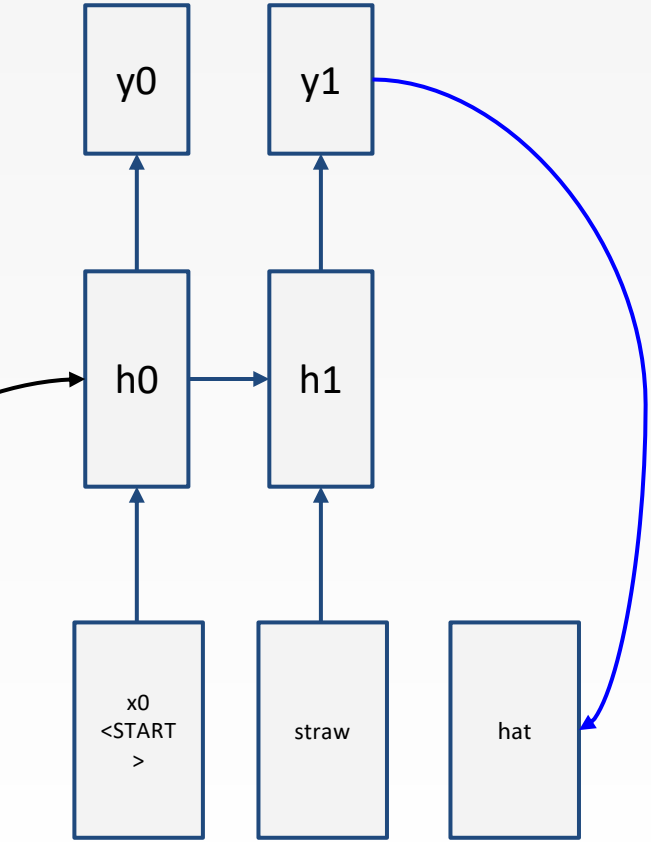


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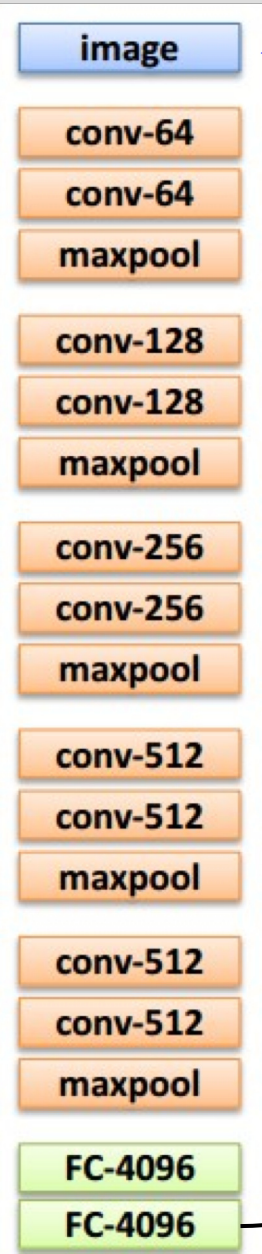




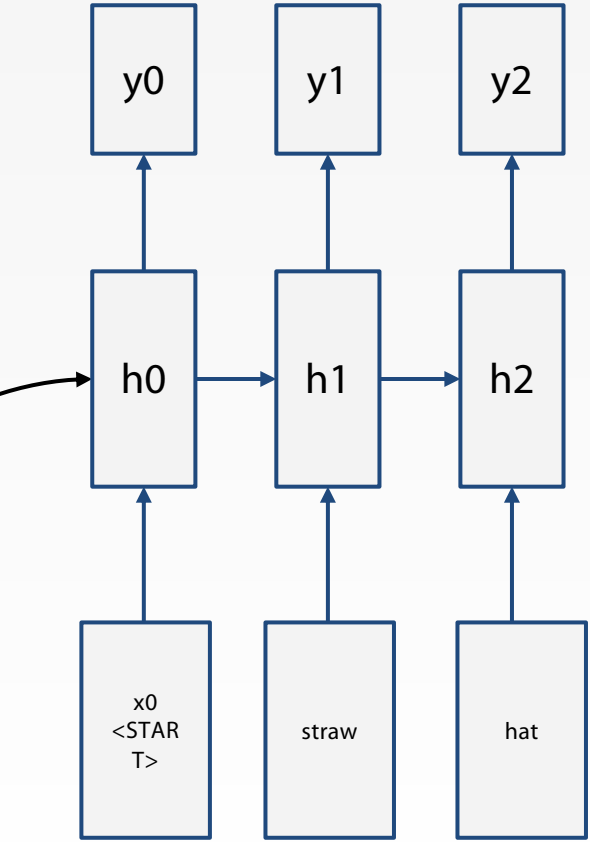
test image



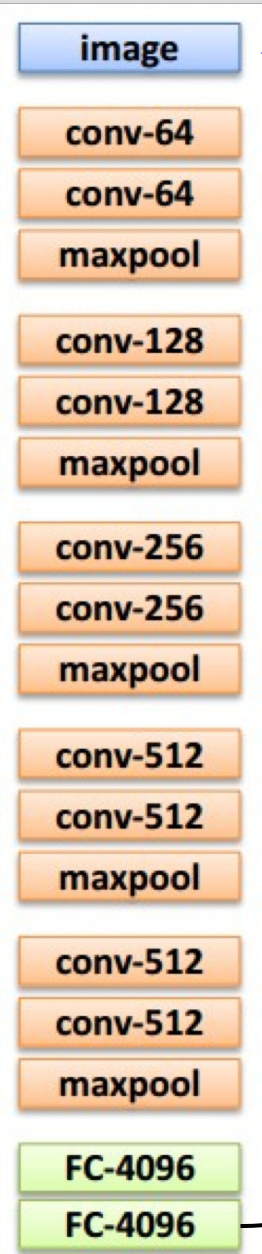
sample!



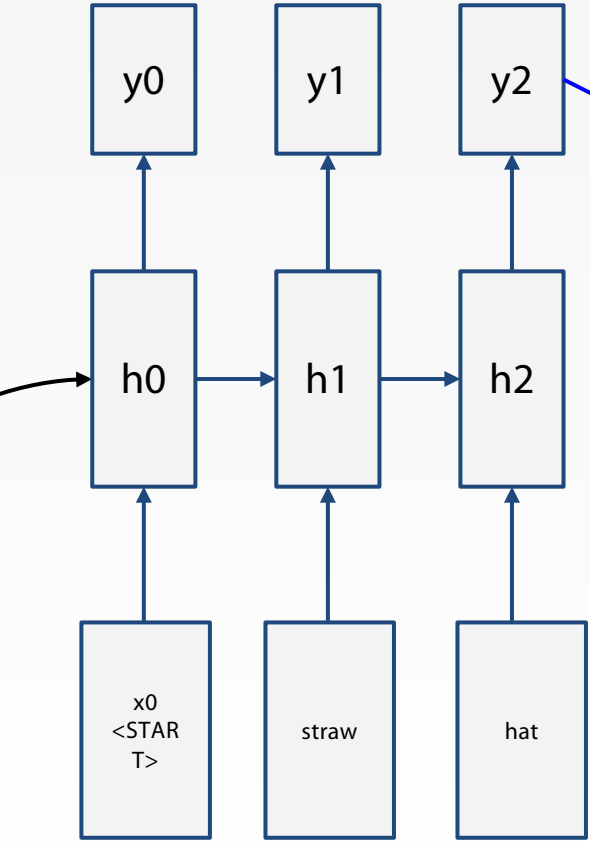
test image



<START>



test image



sample
<END> token
=> finish.

IMAGE CAPTIONING: EXAMPLE RESULTS



A cat sitting on a suitcase on the floor



A cat is sitting on a tree branch



A dog is running in the grass with a frisbee



A white teddy bear sitting in the grass



Two people walking on the beach with surfboards



A tennis player in action on the court



Two giraffes standing in a grassy field

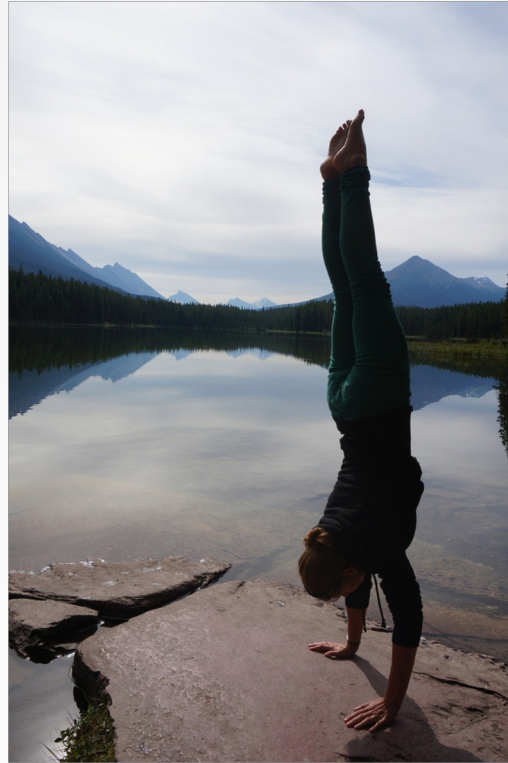


A man riding a dirt bike on a dirt track

IMAGE CAPTIONING: FAILURE CASES



A woman is holding a cat in her hand



A woman standing on a beach holding a surfboard



A bird is perched on a tree branch



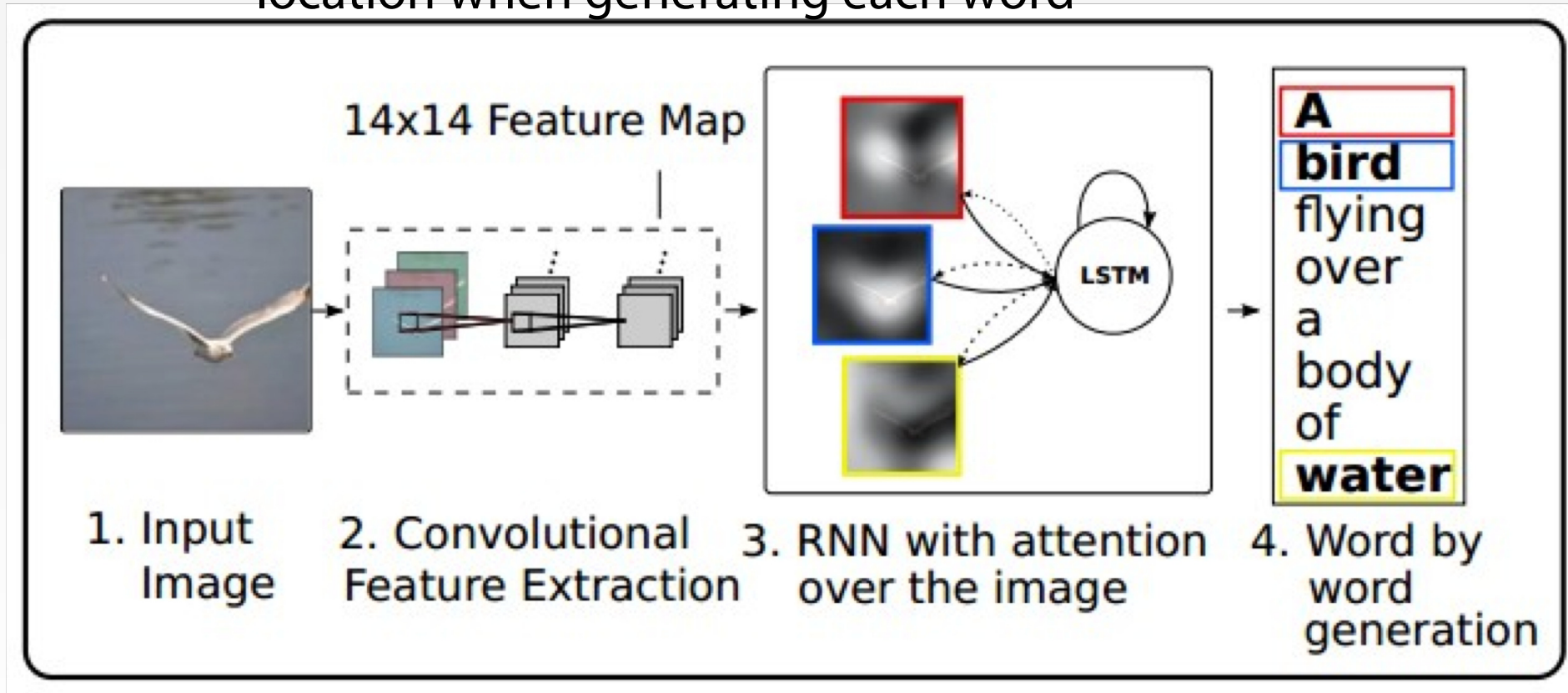
A person holding a computer mouse on a desk



A man in a baseball uniform throwing a ball

IMAGE CAPTIONING WITH ATTENTION

RNN focuses its attention at a different spatial location when generating each word



Xu et al, "Show, Attend, and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015
Figure copyright Kelvin Xu, Jimmy Lei Ba, Jamie Kiros, Kyunghyun Cho, Aaron Courville, Ruslan Salakhutdinov, Richard S. Zemel, and Yoshua Bengio, 2015. Reproduced with permission.

IMAGE CAPTIONING WITH ATTENTION

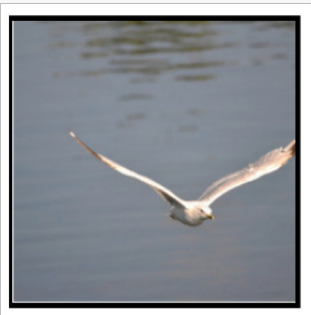
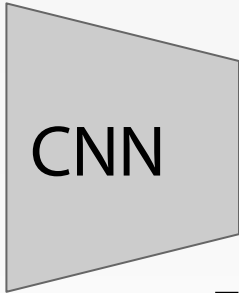
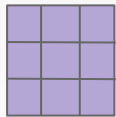


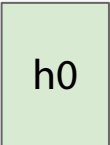
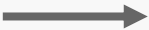
Image:
 $H \times W \times 3$



CNN

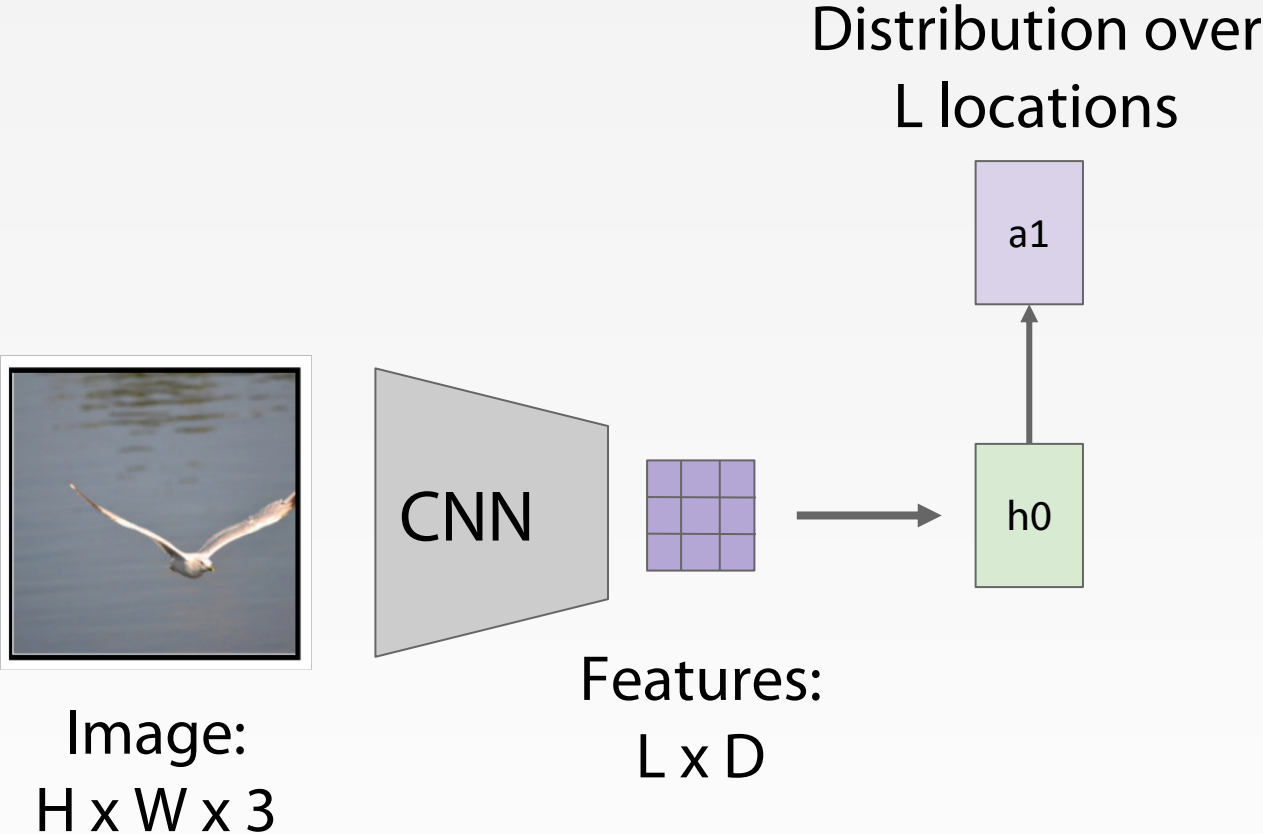


Features:
 $L \times D$



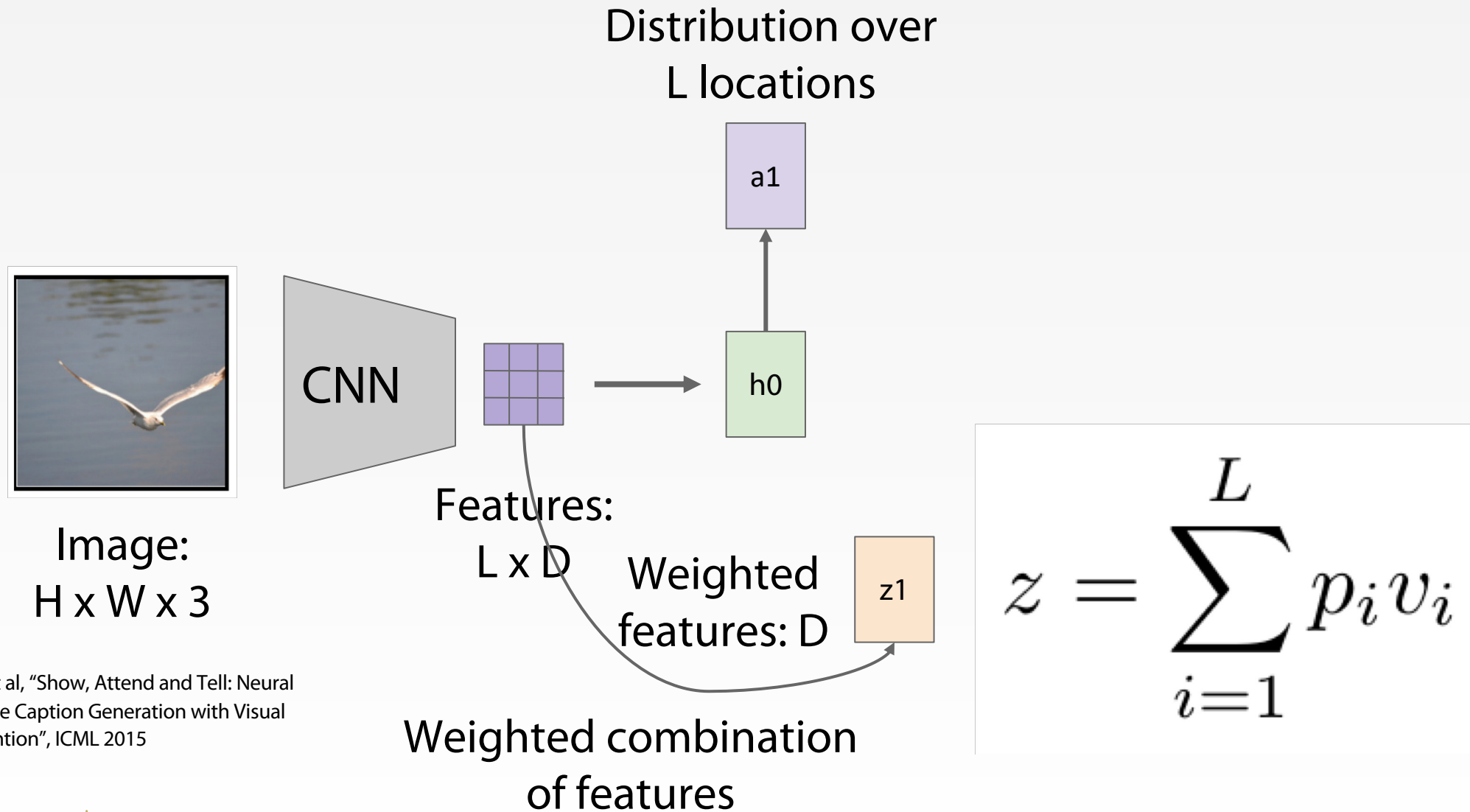
Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

IMAGE CAPTIONING WITH ATTENTION



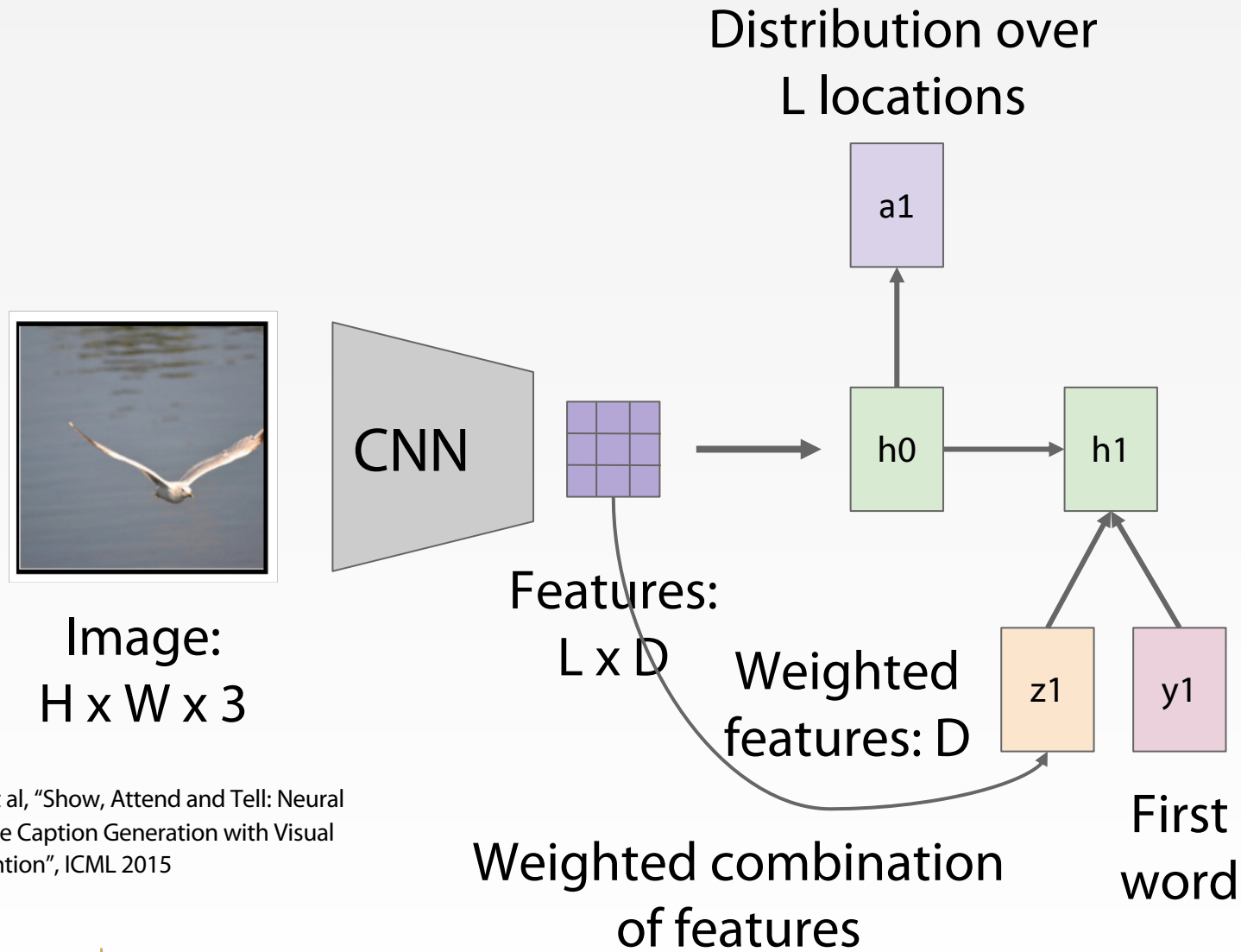
Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

IMAGE CAPTIONING WITH ATTENTION



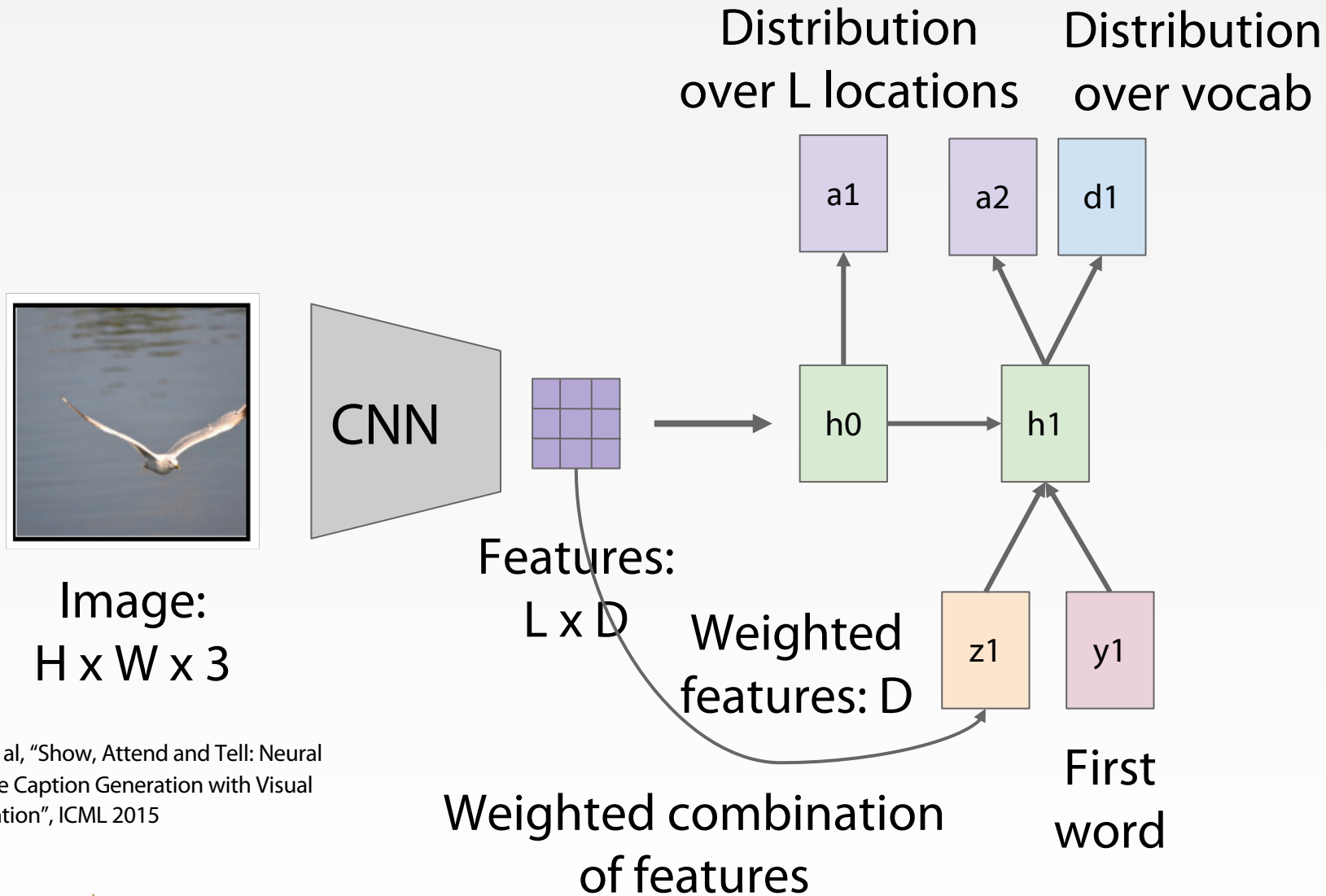
Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

IMAGE CAPTIONING WITH ATTENTION



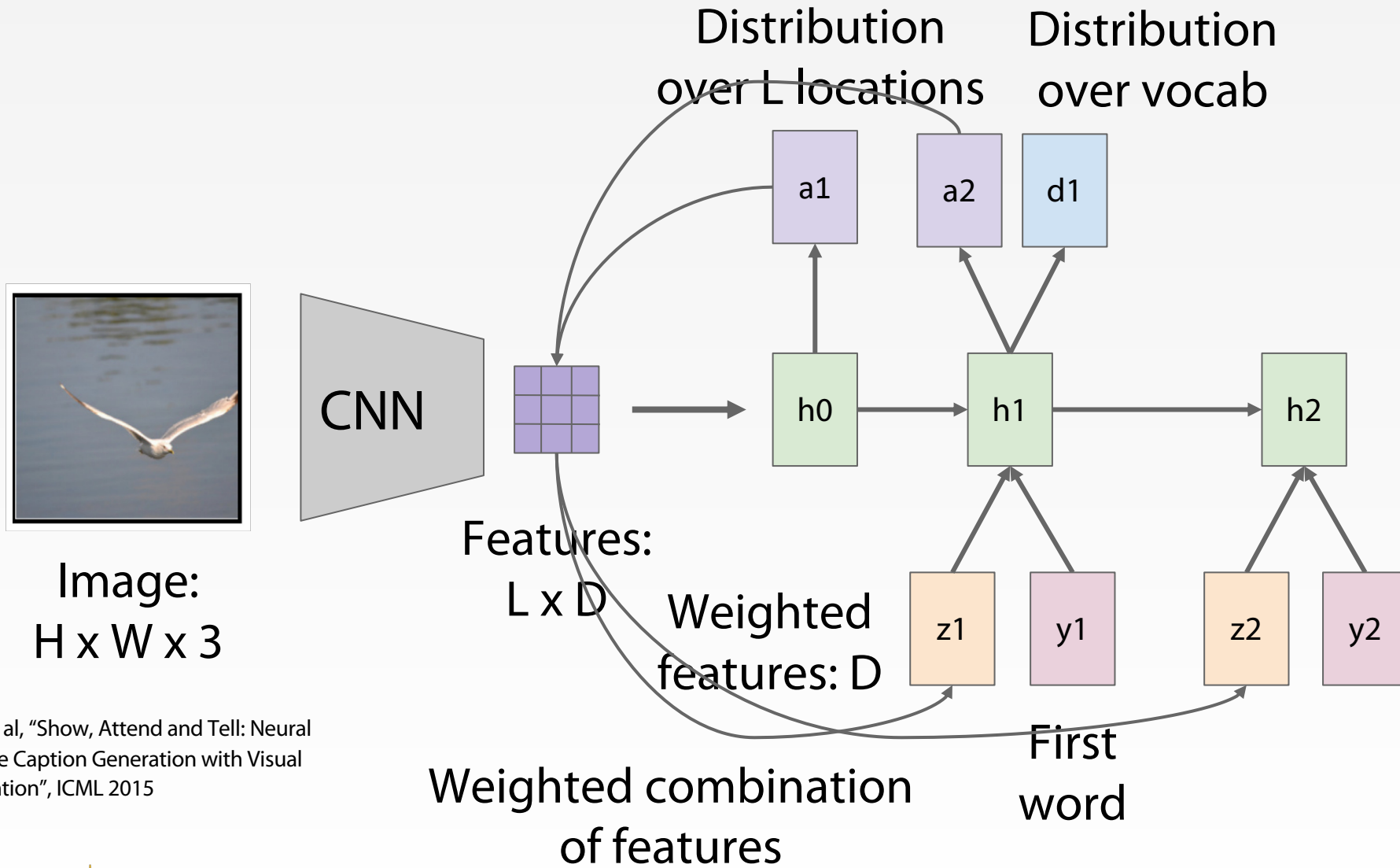
Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

IMAGE CAPTIONING WITH ATTENTION



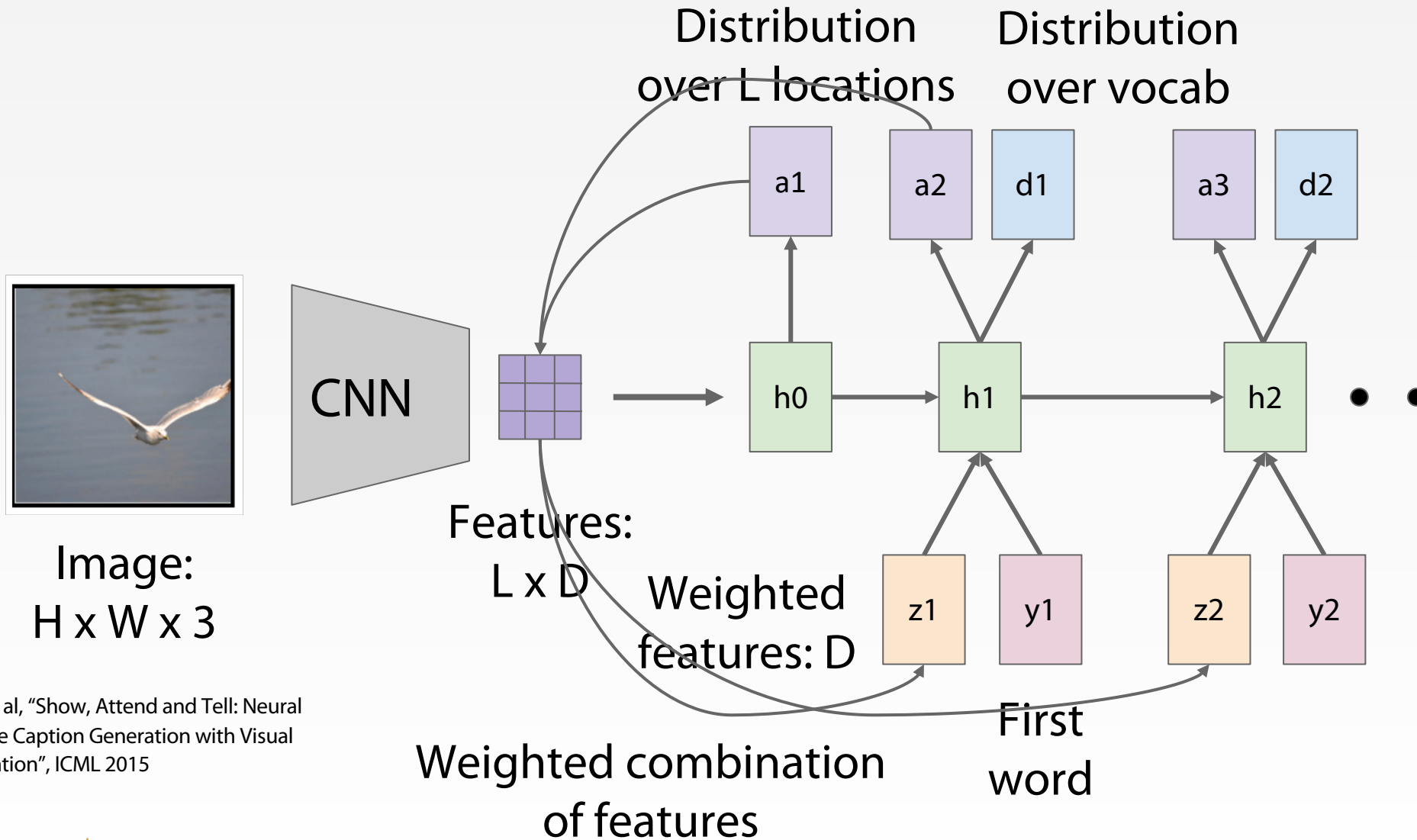
Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

IMAGE CAPTIONING WITH ATTENTION



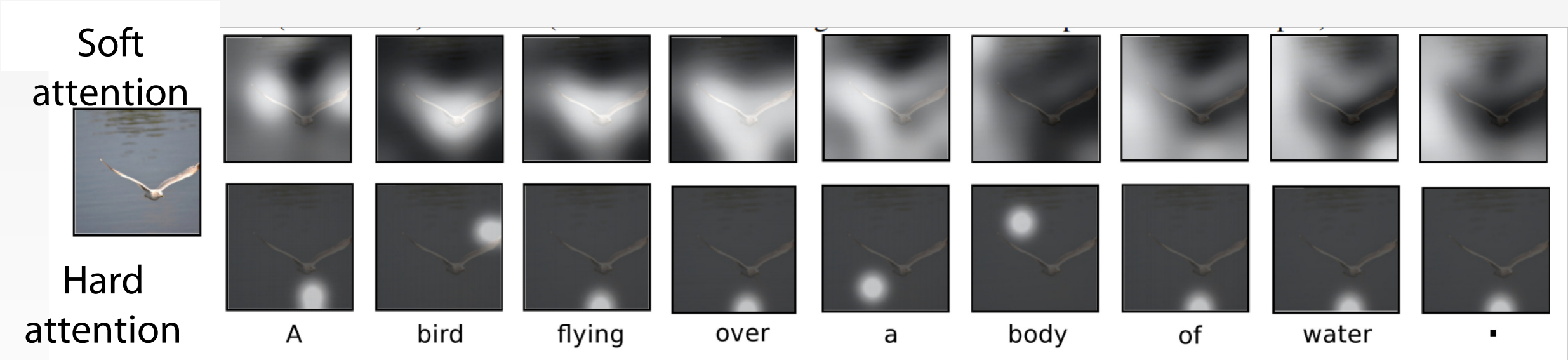
Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

IMAGE CAPTIONING WITH ATTENTION



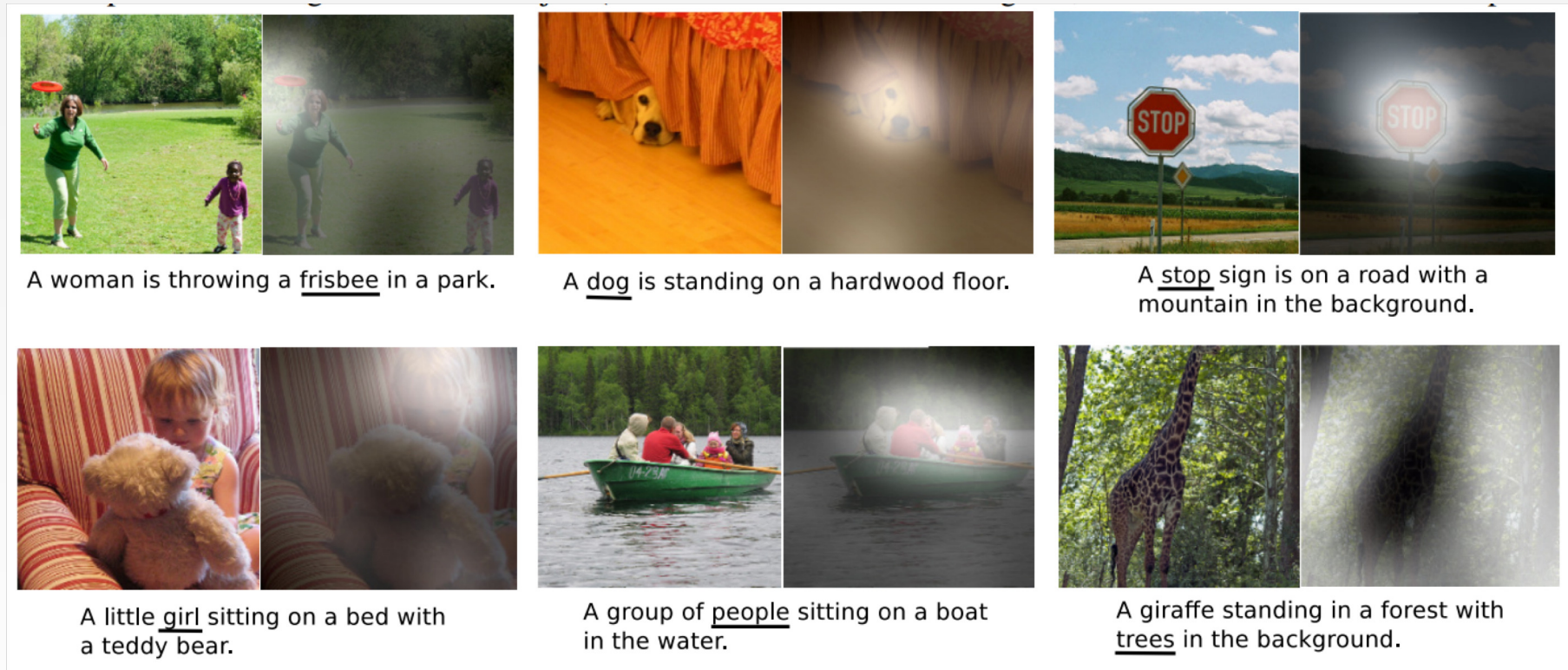
Xu et al, "Show, Attend and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015

IMAGE CAPTIONING WITH ATTENTION



Xu et al, "Show, Attend, and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015
Figure copyright Kelvin Xu, Jimmy Lei Ba, Jamie Kiros, Kyunghyun Cho, Aaron Courville, Ruslan Salakhutdinov, Richard S. Zemel, and Yoshua Benchio, 2015. Reproduced with permission.

IMAGE CAPTIONING WITH ATTENTION



A woman is throwing a frisbee in a park.

A dog is standing on a hardwood floor.

A stop sign is on a road with a mountain in the background.

A little girl sitting on a bed with a teddy bear.

A group of people sitting on a boat in the water.

A giraffe standing in a forest with trees in the background.

Xu et al, "Show, Attend, and Tell: Neural Image Caption Generation with Visual Attention", ICML 2015
Figure copyright Kelvin Xu, Jimmy Lei Ba, Jamie Kiros, Kyunghyun Cho, Aaron Courville, Ruslan Salakhutdinov, Richard S. Zemel, and Yoshua Bengio, 2015. Reproduced with permission.

VISUAL QUESTION ANSWERING



Q: What endangered animal is featured on the truck?

- A: A bald eagle.**
- A: A sparrow.
- A: A humming bird.
- A: A raven.



Q: Where will the driver go if turning right?

- A: Onto 24 3/4 Rd.**
- A: Onto 25 3/4 Rd.
- A: Onto 23 3/4 Rd.
- A: Onto Main Street.



Q: When was the picture taken?

- A: During a wedding.**
- A: During a bar mitzvah.
- A: During a funeral.
- A: During a Sunday church service.

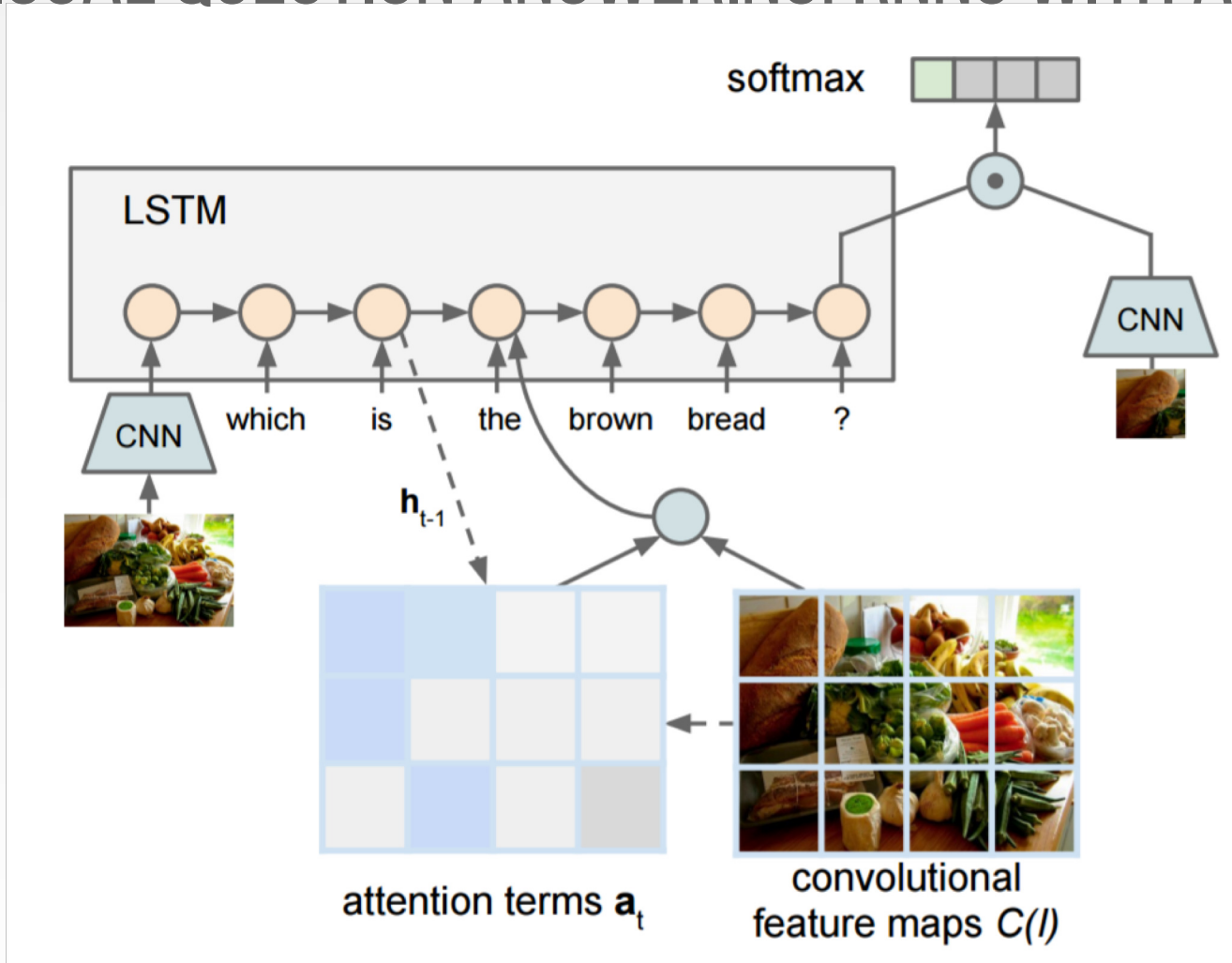


Q: Who is under the umbrella?

- A: Two women.**
- A: A child.
- A: An old man.
- A: A husband and a wife.

Agrawal et al, "VQA: Visual Question Answering", ICCV 2015
Zhu et al, "Visual 7W: Grounded Question Answering in Images", CVPR 2016
Figure from Zhu et al, copyright IEEE 2016. Reproduced for educational purposes.

VISUAL QUESTION ANSWERING: RNNs WITH ATTENTION



A

cat

What kind of animal is in the photo?
A **cat**.

B

cake

Why is the person holding a knife?
To cut the **cake** with.

Zhu et al, "Visual 7W: Grounded Question Answering in Images", CVPR 2016
Figures from Zhu et al, copyright IEEE 2016. Reproduced for educational purposes.

Multilayer RNNs

$$h_t^l = \tanh W^l \begin{pmatrix} h_t^{l-1} \\ h_{t-1}^l \end{pmatrix}$$

$h \in \mathbb{R}^n$ $W^l [n \times 2n]$

LSTM:

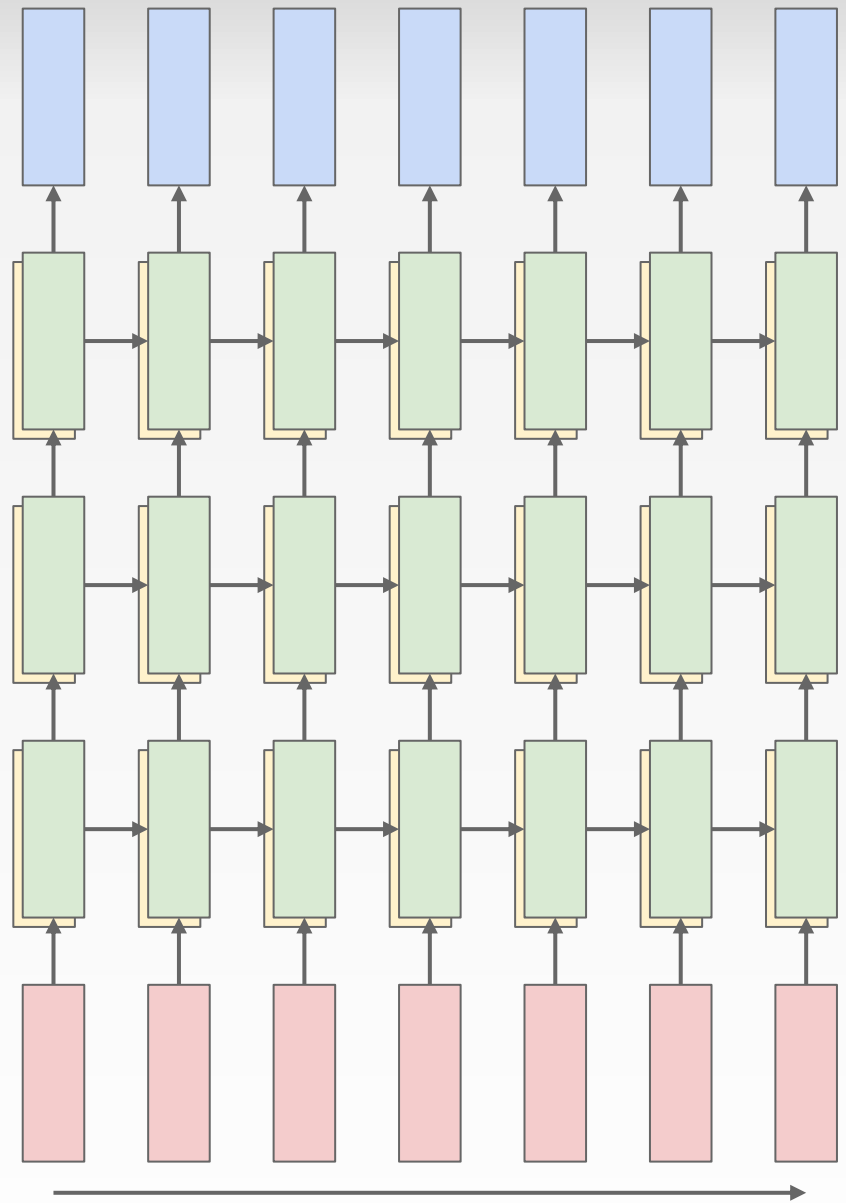
$$W^l [4n \times 2n]$$

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \text{sigm} \\ \text{sigm} \\ \text{sigm} \\ \text{tanh} \end{pmatrix} W^l \begin{pmatrix} h_t^{l-1} \\ h_{t-1}^l \end{pmatrix}$$

$$c_t^l = f \odot c_{t-1}^l + i \odot g$$

$$h_t^l = o \odot \tanh(c_t^l)$$

depth



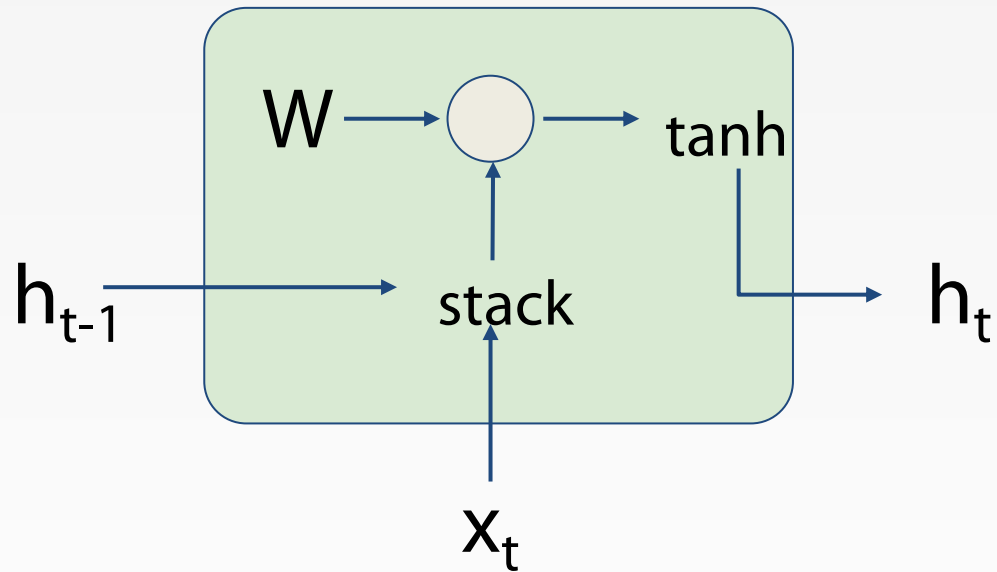
time



LSTM

VANILLA RNN GRADIENT FLOW

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

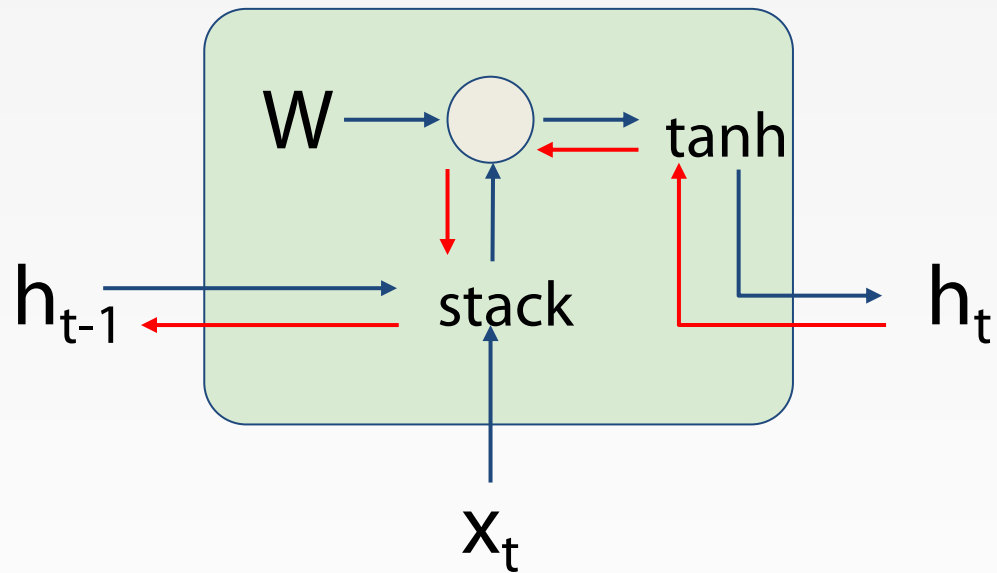


$$\begin{aligned}h_t &= \tanh(W_{hh}h_{t-1} + W_{hx}x_t) \\ &= \tanh\left(\begin{pmatrix} W_{hh} & W_{hx} \end{pmatrix} \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right) \\ &= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right)\end{aligned}$$

VANILLA RNN GRADIENT FLOW

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

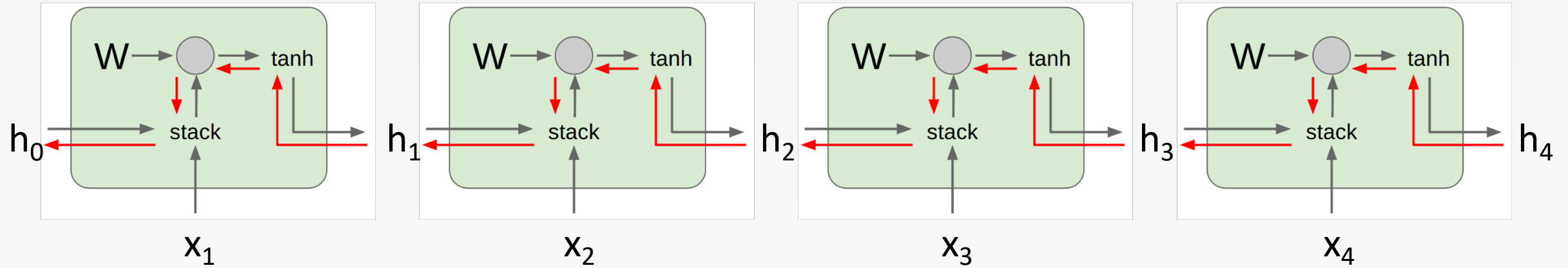
Backpropagation from h_t to h_{t-1}
multiplies by W (actually W_{hh}^T)



$$\begin{aligned}h_t &= \tanh(W_{hh}h_{t-1} + W_{hx}x_t) \\ &= \tanh\left((W_{hh} \quad W_{hx}) \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right) \\ &= \tanh\left(W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}\right)\end{aligned}$$

VANILLA RNN GRADIENT FLOW

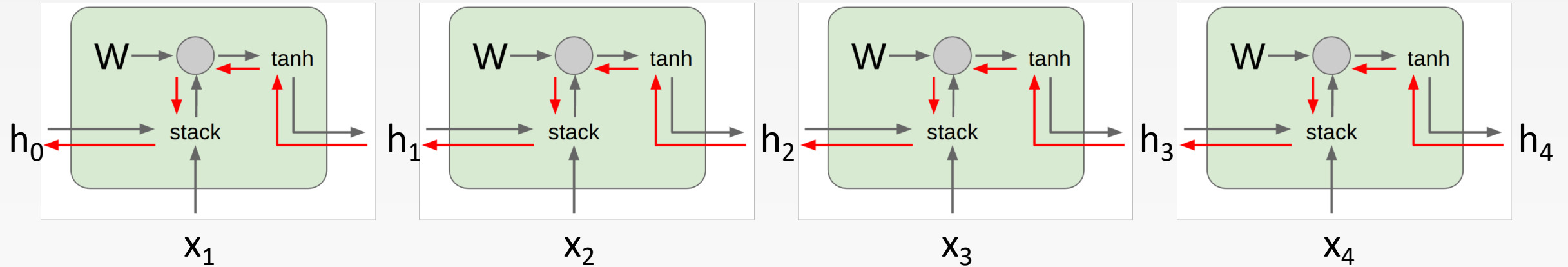
Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



Computing gradient of h_0 involves many factors of W (and repeated \tanh)

VANILLA RNN GRADIENT FLOW

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



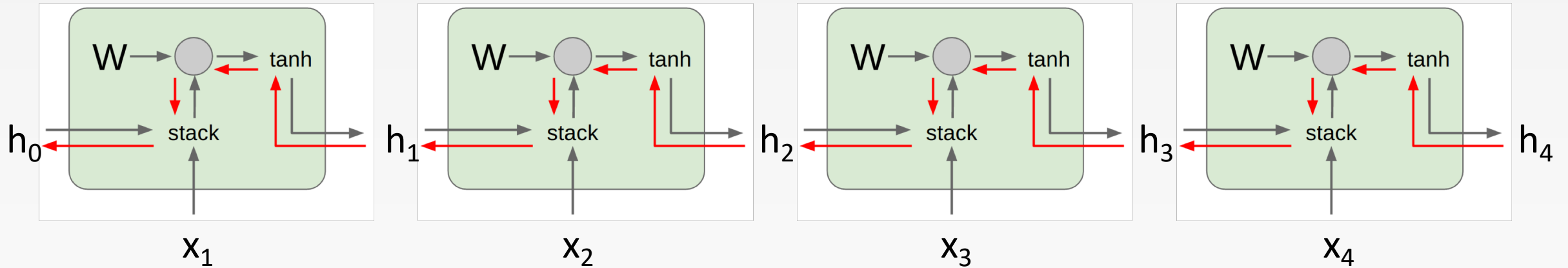
Computing gradient of h_0 involves many factors of W (and repeated \tanh)

Largest singular value > 1 :
Exploding gradients

Largest singular value < 1 :
Vanishing gradients

VANILLA RNN GRADIENT FLOW

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



Computing gradient of h_0 involves many factors of W (and repeated tanh)

Largest singular value > 1 :
Exploding gradients

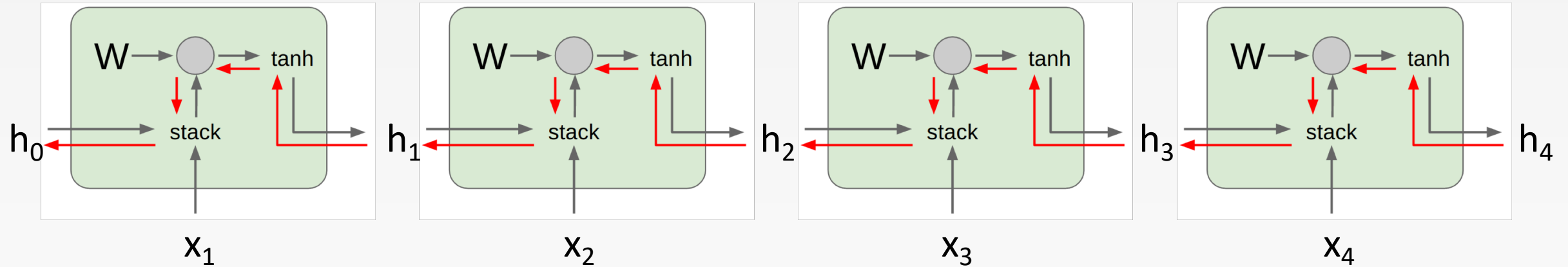
Largest singular value < 1 :
Vanishing gradients

Gradient clipping: Scale gradient if its norm is too big

```
grad_norm = np.sum(grad * grad)
if grad_norm > threshold:
    grad *= (threshold / grad_norm)
```

VANILLA RNN GRADIENT FLOW

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994
Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



Computing gradient of h_0 involves many factors of W (and repeated \tanh)

Largest singular value > 1 :
Exploding gradients

Largest singular value < 1 :
Vanishing gradients

→ Change RNN architecture

LONG SHORT TERM MEMORY (LSTM)

Vanilla RNN

$$h_t = \tanh \left(W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix} \right)$$

LSTM

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

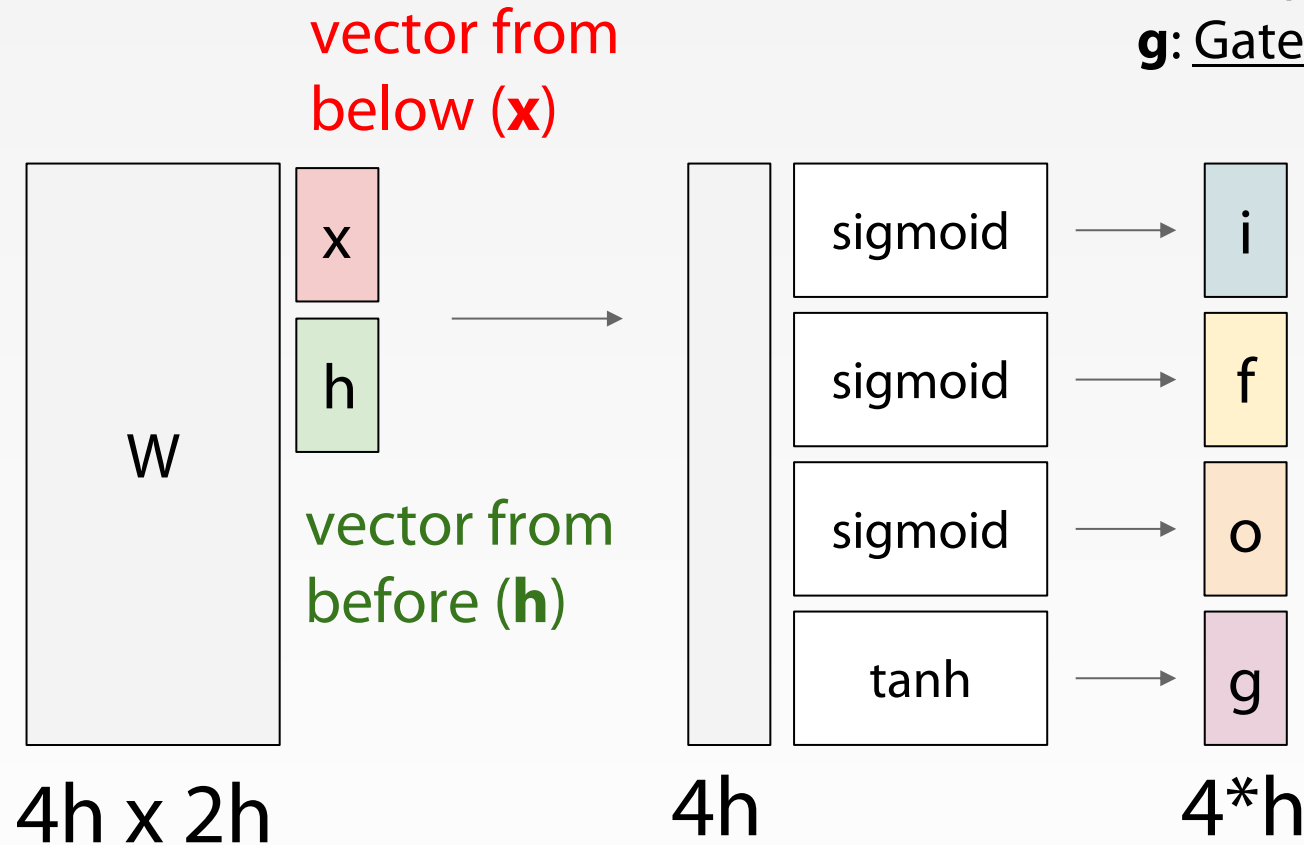
$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

Hochreiter and Schmidhuber, "Long Short Term Memory", Neural Computation 1997

LONG SHORT TERM MEMORY (LSTM)

[Hochreiter et al., 1997]

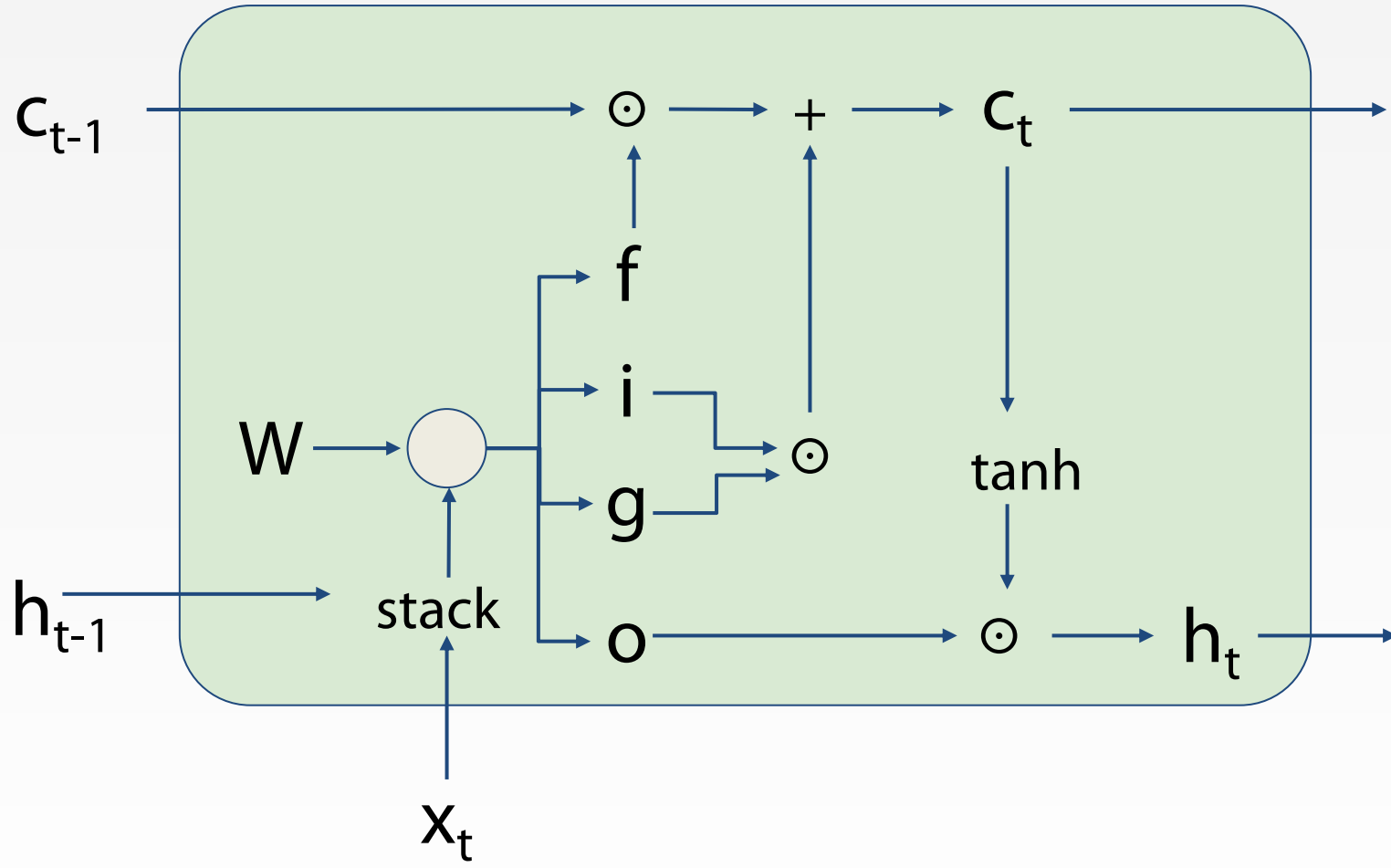


- i**: Input gate, whether to write to cell
- f**: Forget gate, whether to erase cell
- o**: Output gate, how much to reveal cell
- g**: Gate gate (?), how much to write to cell

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$
$$c_t = f \odot c_{t-1} + i \odot g$$
$$h_t = o \odot \tanh(c_t)$$

LONG SHORT TERM MEMORY (LSTM)

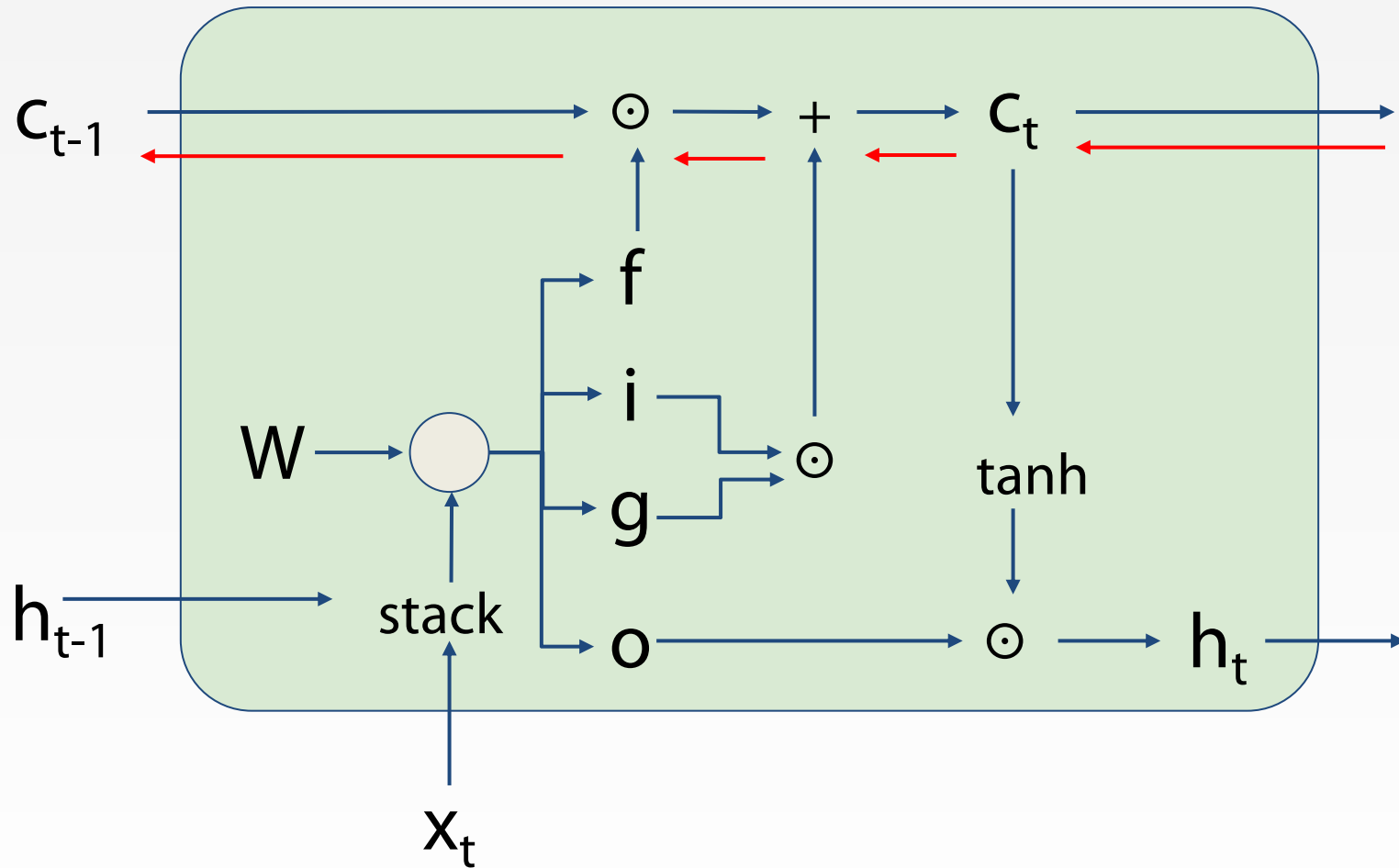
[Hochreiter et al., 1997]



$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$
$$c_t = f \odot c_{t-1} + i \odot g$$
$$h_t = o \odot \tanh(c_t)$$

LONG SHORT TERM MEMORY (LSTM): GRADIENT FLOW

[Hochreiter et al., 1997]



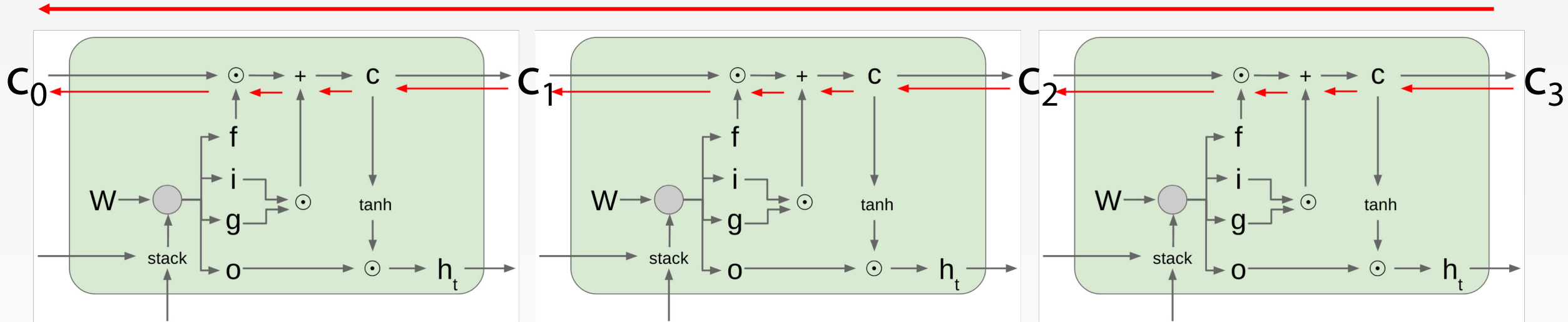
Backpropagation from c_t to c_{t-1} only elementwise multiplication by f , no matrix multiply by W

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$
$$c_t = f \odot c_{t-1} + i \odot g$$
$$h_t = o \odot \tanh(c_t)$$

LONG SHORT TERM MEMORY (LSTM): GRADIENT FLOW

[Hochreiter et al., 1997]

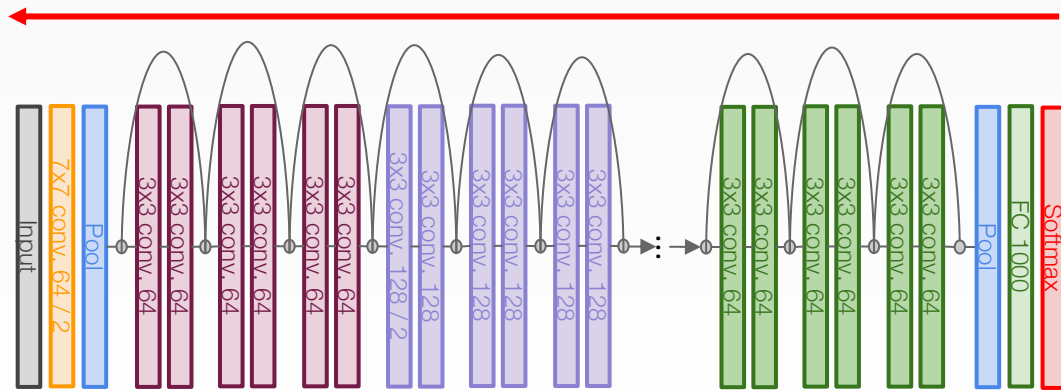
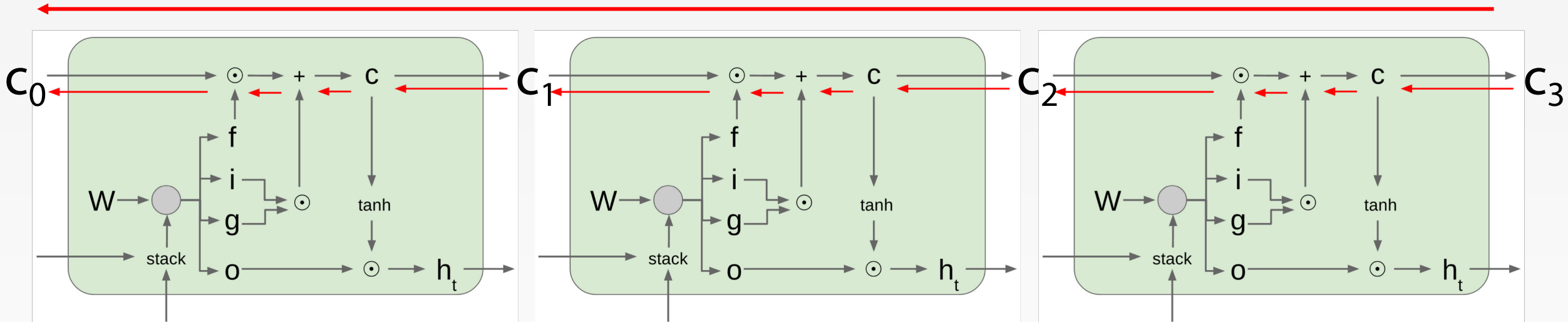
Uninterrupted gradient flow!



LONG SHORT TERM MEMORY (LSTM): GRADIENT FLOW

[Hochreiter et al., 1997]

Uninterrupted gradient flow!

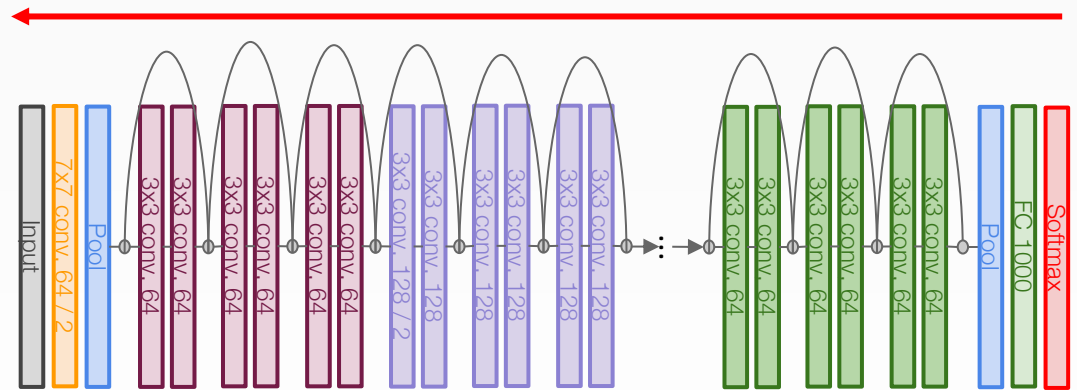
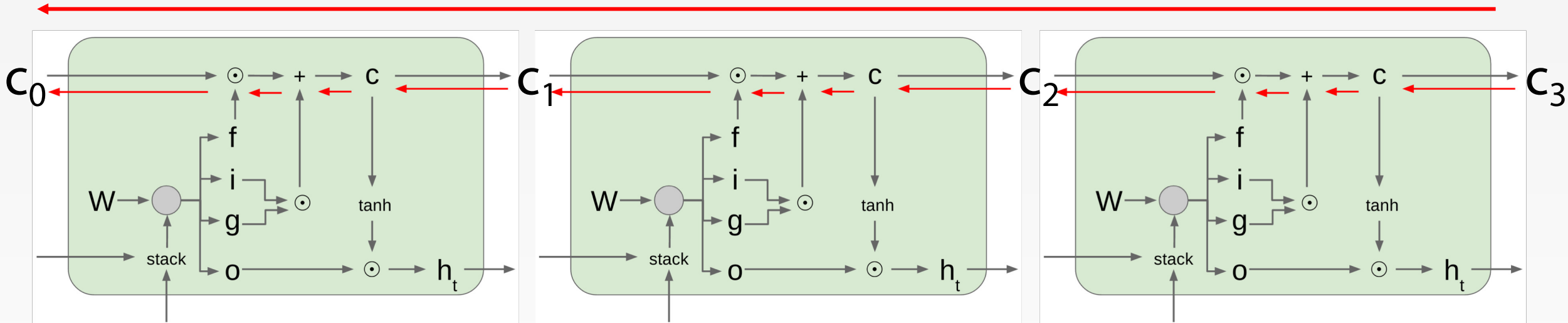


Similar to ResNet!

LONG SHORT TERM MEMORY (LSTM): GRADIENT FLOW

[Hochreiter et al., 1997]

Uninterrupted gradient flow!



Similar to ResNet!

In between:

Highway Networks

$$g = T(x, W_T)$$

$$y = g \odot H(x, W_H) + (1 - g) \odot x$$

Srivastava et al, "Highway Networks", ICML DL Workshop 2015

OTHER RNN VARIANTS

GRU [*Learning phrase representations using rnn encoder-decoder for statistical machine translation, Cho et al. 2014*]

$$\begin{aligned}r_t &= \sigma(W_{xr}x_t + W_{hr}h_{t-1} + b_r) \\z_t &= \sigma(W_{xz}x_t + W_{hz}h_{t-1} + b_z) \\ \tilde{h}_t &= \tanh(W_{xh}x_t + W_{hh}(r_t \odot h_{t-1}) + b_h) \\h_t &= z_t \odot h_{t-1} + (1 - z_t) \odot \tilde{h}_t\end{aligned}$$

[*LSTM: A Search Space Odyssey, Greff et al., 2015*]

[*An Empirical Exploration of Recurrent Network Architectures,*

MUT1:

$$\begin{aligned}z &= \text{sigm}(W_{xz}x_t + b_z) \\r &= \text{sigm}(W_{xr}x_t + W_{hr}h_t + b_r) \\h_{t+1} &= \tanh(W_{hh}(r \odot h_t) + \tanh(x_t) + b_h) \odot z \\ &+ h_t \odot (1 - z)\end{aligned}$$

MUT2:

$$\begin{aligned}z &= \text{sigm}(W_{xz}x_t + W_{hz}h_t + b_z) \\r &= \text{sigm}(x_t + W_{hr}h_t + b_r) \\h_{t+1} &= \tanh(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z \\ &+ h_t \odot (1 - z)\end{aligned}$$

MUT3:

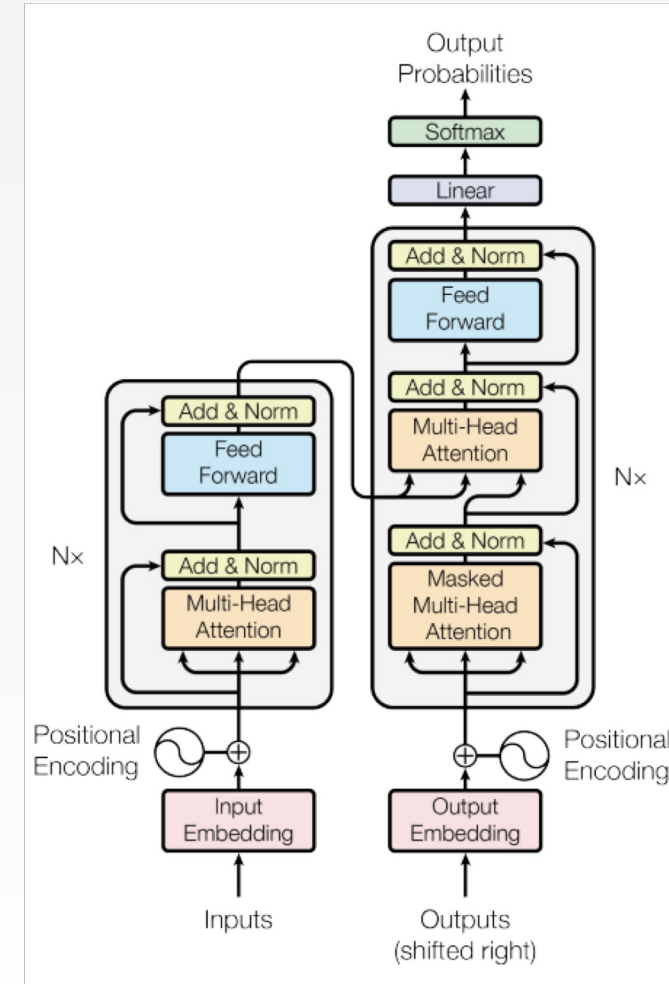
$$\begin{aligned}z &= \text{sigm}(W_{xz}x_t + W_{hz} \tanh(h_t) + b_z) \\r &= \text{sigm}(W_{xr}x_t + W_{hr}h_t + b_r) \\h_{t+1} &= \tanh(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z \\ &+ h_t \odot (1 - z)\end{aligned}$$

RECENTLY IN NATURAL LANGUAGE PROCESSING...

NEW PARADIGMS FOR REASONING OVER SEQUENCES

[*“Attention is all you need”, Vaswani et al., 2018*]

- New “Transformer” architecture no longer processes inputs sequentially; instead it can operate over inputs in a sequence in parallel through an attention mechanism
- Has led to many state-of-the-art results and pre-training in NLP, for more results see e.g.
 - “BERT: Pre-training of Deep Bidirectional Transformers for Language Understanding”, Devlin et al., 2018
 - OpenAI GPT-2, Radford et al., 2018



SUMMARY: RNNs

- RNNs allow a lot of flexibility in architecture design
 - Vanilla RNNs are simple but don't work very well
 - Common to use LSTM or GRU: their additive interactions improve gradient flow
- Backward flow of gradients in RNN can explode or vanish.
 - Exploding is controlled with gradient clipping.
 - Vanishing is controlled with additive interactions (LSTM)
- Better/simpler architectures are a hot topic of current research, as well as new paradigms for reasoning over sequences
- Better understanding (both theoretical and empirical) is needed.