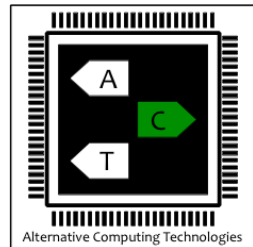


# Expectation-Oriented Framework for Automating Approximate Programming

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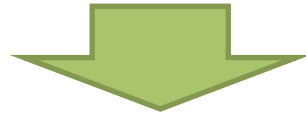


# Approximate Programming

Programmer's

**manual/explicit** specification

[EnerJ PLDI'11, Rely OOPSLA'13]



**AUTOMATE**

approximate programming

**Where? How much?**

# ExpAX Overview

Source Code



Source Code  
Expectation

Approximation  
Safety  
Analysis

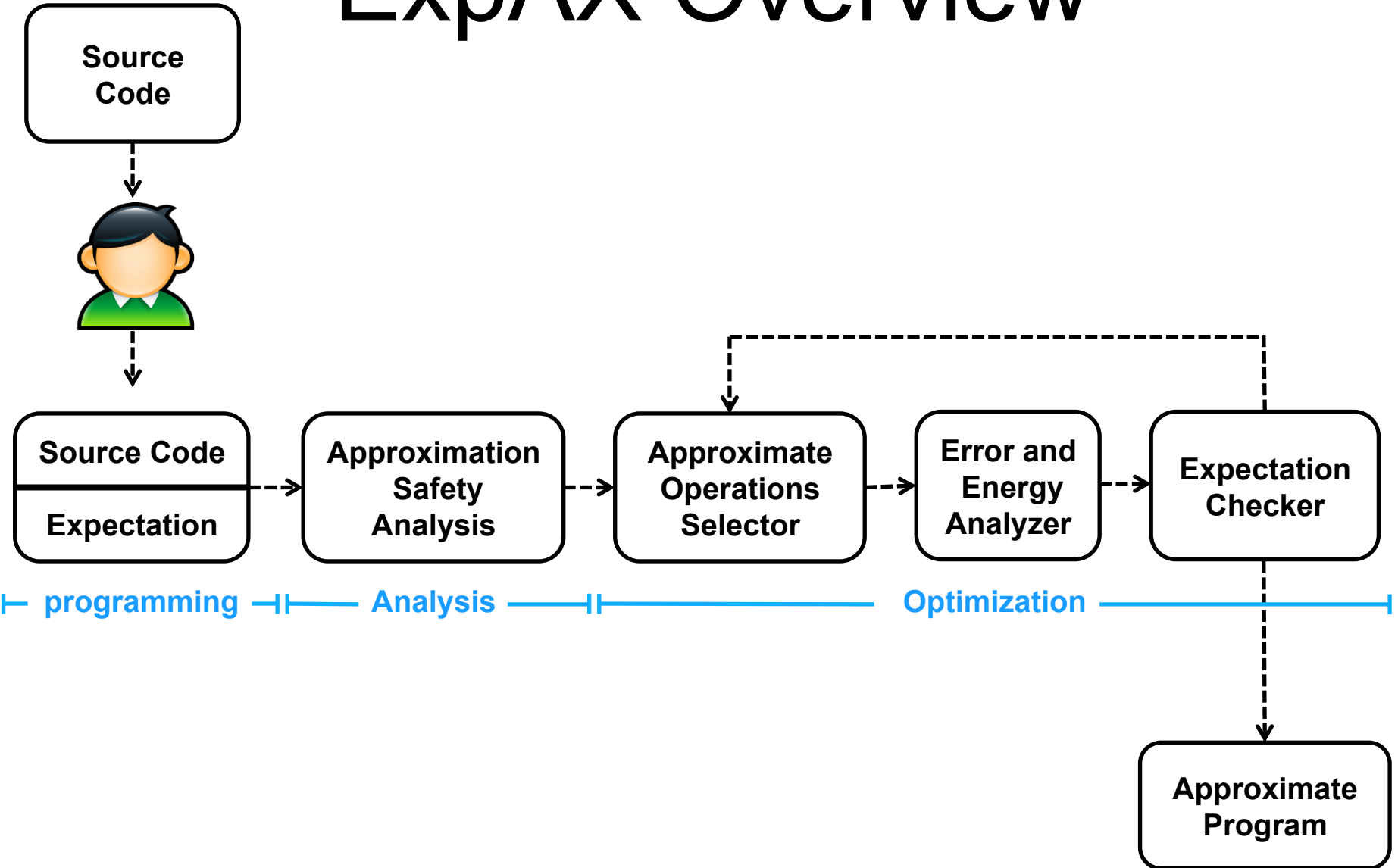
Approximate  
Operations  
Selector

Error and  
Energy  
Analyzer

Expectation  
Checker

Approximate  
Program

programming | Analysis | Optimization



# Programming Model

## Programmer's Annotations with **Expectation**

1. **accept**  $\text{rate}(v) < c$

e.g.  $\text{rate}(v) < 0.2$

2. **accept**  $\text{magnitude}(v) < c$  using  $f$

e.g.  $\text{magnitude}(v) < 0.1$

3. **accept**  $\text{magnitude}(v) > c$  using  $f$  with  $\text{rate} < c'$

e.g.  $\text{magnitude}(v) > 0.9$  with  $\text{rate} < 0.3$

# Approximation Safety Analysis

Find possible **safe-to-approximate variables**

**Unsafe**-to-approximate variables

1. Variables violating memory safety
2. Variables violating functional correctness

# Approximation Safety Analysis

## Backslicing Analysis

For each variable **v** in program,  
find all variables **contributing** to the variable **v**

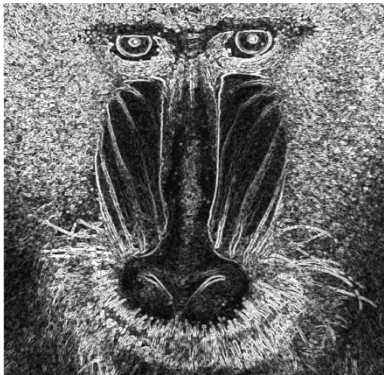
**unsafe**-to-approximate variables  
should be **precise**

**Everything else** should be **precise** variables

# Example



edgeDetection



```
Float sobel (float[3][3] p) {  
    float x, y, gradient;  
    x = (p[0][0] + 2 * p[0][1] + p[0][2]);  
    x += (p[2][0] + 2 * p[0][1] + p[2][2]);  
    y = (p[0][2] + 2 * p[1][2] + p[2][2]);  
    y += (p[0][0] + 2 * p[1][1] + p[2][0]);  
    gradient = sqrt(x * x + y * y);  
    ...  
    return gradient;  
}
```

```
void edgeDetection(Image &src, Image &dst) {  
    grayscale(src);  
  
    for (int y = ...)  
        for (int x = ...)  
            dst[x][y] = sobel(window(src, x, y));  
  
    accept rate(dst) < 0.1;  
}
```

# Optimization

Find a **subset** of safe-to-approximate operations

- Minimize error
- Maximize energy saving

Objective function

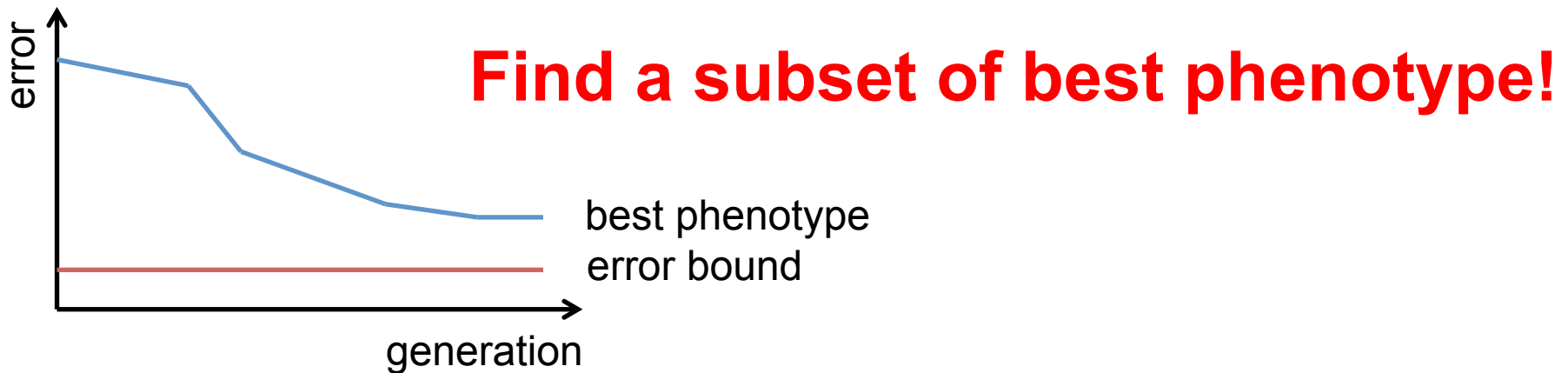
$$f(\textit{subset}) = (\alpha \times \textit{error} + \beta \times \textit{energy})^{-1}$$

Genetic algorithm

**phenotype**: a bitvector representing a subset  
(approximate('0') or precise('1'))



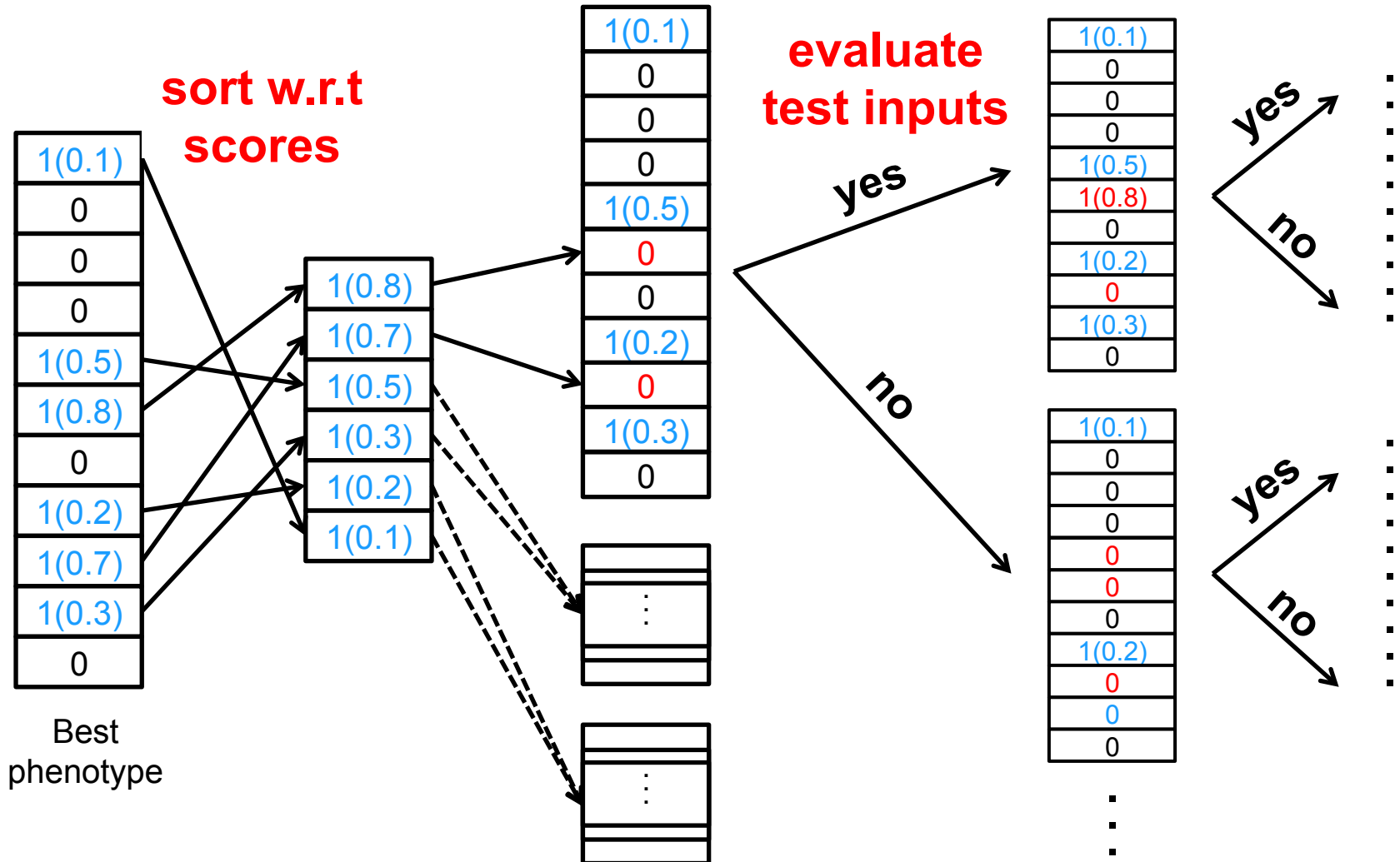
# Statistical Guarantee



For each **eval** in genetic algorithm:  
calculate a **score** for each **operation**

$$f(\text{operation}) = \sum_{\text{eval} \in \text{Eval}} \left( \frac{\alpha \times \text{error} + \beta \times \text{energy}}{n(\text{approx})} \right) / n(\text{Eval})$$

# Space Exploration with Transformed Best Phenotype



# Evaluation

## **Benchmarks:**

scimark2 – FFT, LU, SOR, MonteCarlo, SMM  
Imagefill, raytracer, jmeint, zxing

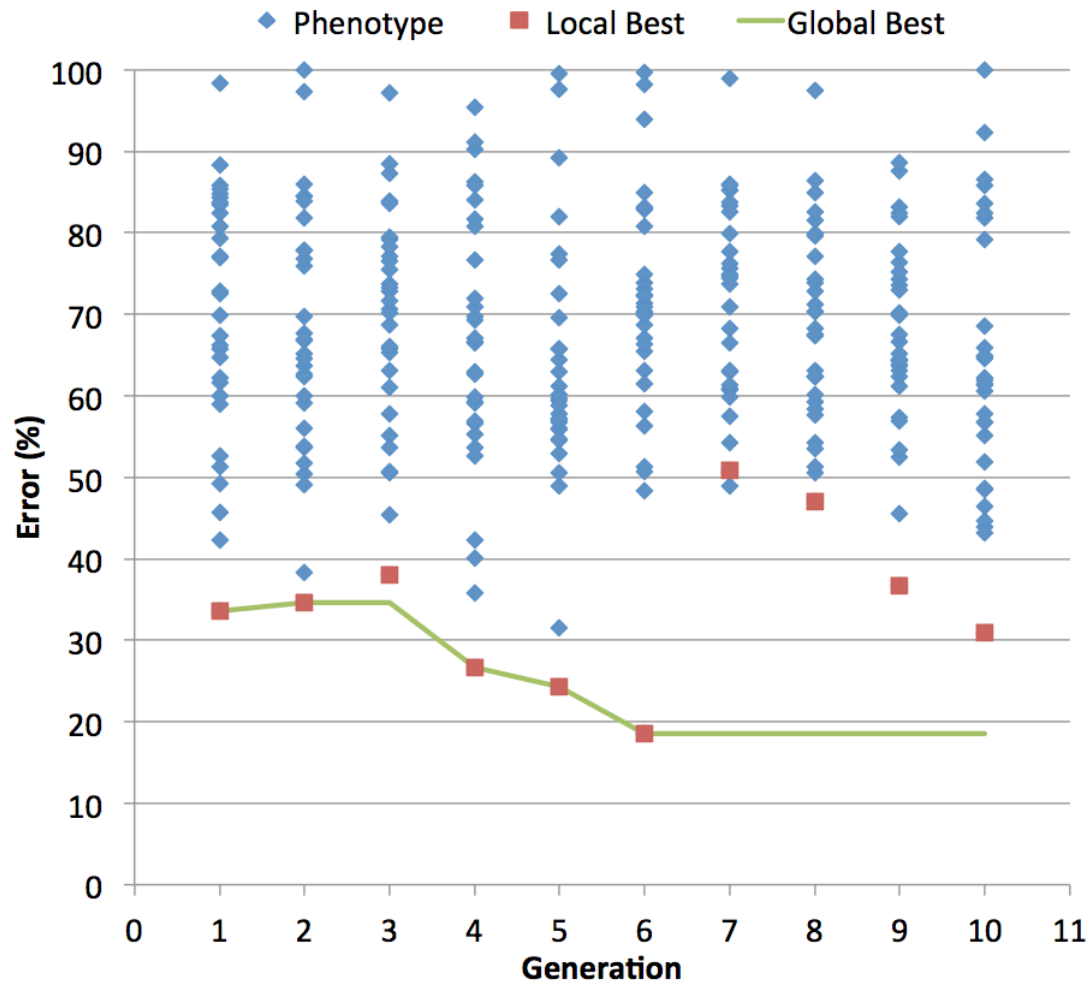
## **Simulator:**

Open-source simulator provided by EnerJ

# Analysis Result

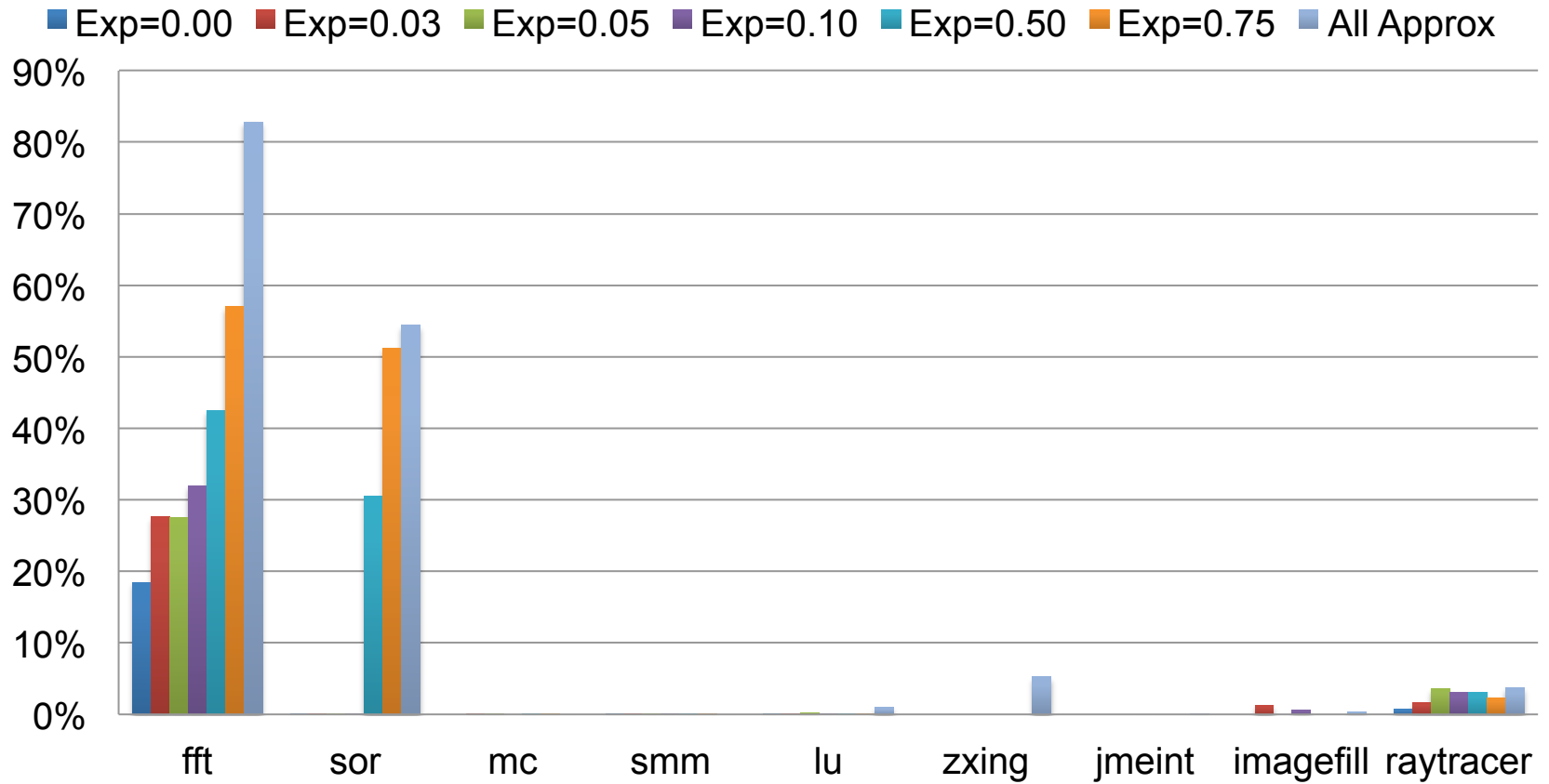
BenchName	Enerj: # of Annotations	ExpAX: # of Expectations
FFT	27	1
LU	20	1
SOR	9	1
MonteCarlo	3	1
SMM	8	1
imagefill	28	7
RayTracer	27	2
jmeint	113	1
zxing	172	15

# Genetic Algorithm Results



**LU on aggressive system specification**

# Error



# Conclusion

## **Expax:**

an expectation-oriented framework for **automating** approximate programming

1. Programming model with a new program specification
2. Approximation safety analysis
3. Optimization framework  
with heuristics for statistical guarantee