# CS 4644/7643: Deep Learning <br> Spring 2024 <br> Problem Set 0 

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Due: Sunday, Jan 14, 11:59pm ET

## Instructions

1. We will be using Gradescope to collect your assignments. Please read the following instructions for submitting to Gradescope carefully! Failure to follow these instructions may result in parts of your assignment not being graded. We will not entertain regrading requests for failure to follow instructions.

- It is mandatory to use the $\mathrm{EAT}_{\mathrm{E}} \mathrm{X}$ template provided. For every question, there is only one correct answer. To mark the correct answer, change \choice to \CorrectChoice
- Remember to tag each question on GradeScope to the correct PDF page. Failure to do so will result in penalty.

2. Hard copies are not accepted.
3. We generally encourage you to collaborate with other students. You may talk to a friend, discuss the questions and potential directions for solving them. However, you need to write your own solutions and code separately, and not as a group activity. Please list the students you collaborated with.
Exception: PS0 is meant to serve as a background preparation test. You must NOT collaborate on PSO.
4. (1 point) Consider the tables below that display infection rates for a disease in two independent regions given vaccine status.

| Region | Pop. | Vaccination Rates | \% of Population Infected |
| :---: | :---: | :---: | :---: |
| Cityville | 874,961 | $77.0 \%$ | $0.36 \%$ |
| Townsland | 578,759 | $37.7 \%$ | $1 \%$ |


| Region | \% of Infected people that are Vaccinated | \% of Infected people that are Unvaccinated |
| :---: | :---: | :---: |
| Cityville | $27.8 \%$ | $72.2 \%$ |
| Townsland | $5.0 \%$ | $95.0 \%$ |

It appears that infected individuals in Cityville are much more likely to be vaccinated than in Townsland. Given these tables, would a vaccinated individual be less likely to be infected in Cityville or Townsland?
$\bigcirc$ Cityville $\bigcirc$ Townsland
2. (1 point)

Given a (possibly) biased coin with $P($ Heads $)=p$ and $P($ Tails $)=1-p$, first determine the method to generate a fair outcome (50:50) in the fewest amount of flips using this coin.

What is the expected number of coin flips required (in terms of $p$ ) to produce a fair outcome using this method?
$\bigcirc \frac{1}{p(1-p)} \bigcirc \frac{1}{1+p^{2}} \bigcirc \frac{2 p}{1-p} \bigcirc$ A fair outcome cannot be generated with a biased coin
3. (1 point) $X$ is a continuous random variable with probability density function:

$$
p(x)=\left\{\begin{array}{c}
2 x^{3} / 81 \quad 0 \leq x \leq 3  \tag{1}\\
2(x-3) / 8 \quad 3 \leq x \leq 5
\end{array}\right.
$$

Which of the following statements are true about the equation for the corresponding cumulative density function (CDF) $C(x)$ ?
[Hint: Recall that CDF is defined as $C(x)=\operatorname{Pr}(X \leq x)$.]
$\bigcirc C(x)=x^{4} / 162$ for $0 \leq x \leq 3$
$C(x)=x^{2} / 8-3 x / 4+13 / 8$ for $3 \leq x \leq 5$
$\bigcirc$ All of the above
$\bigcirc$ None of the above
4. (2 point) A random variable $x$ in standard normal distribution has the following probability density:

$$
\begin{equation*}
p(x)=\frac{1}{\sqrt{2 \pi}} e^{-\frac{x^{2}}{2}} \tag{2}
\end{equation*}
$$

Evaluate the following integral:

$$
\begin{equation*}
\int_{-\infty}^{\infty} p(x)\left(a x^{2}+b x-c\right) d x \tag{3}
\end{equation*}
$$

[Hint: We are not sadistic (okay, we're a little sadistic, but not for this question). This is not a calculus question.]
$a+b+c$- ca - c $\square$ $b+c$
5. (2 points) Consider the following function of $\mathbf{x}=\left(x_{1}, x_{2}, x_{3}, x_{4}, x_{5}, x_{6}\right)$ :

$$
\begin{equation*}
f(\mathbf{x})=\sigma\left(\log \left(5\left(\max \left\{x_{1}, x_{2}\right\} \cdot \frac{x_{3}}{x_{4}}-\left(x_{5}+x_{6}\right)\right)\right)+\frac{1}{2}\right) \tag{4}
\end{equation*}
$$

where $\sigma$ is the sigmoid function

$$
\begin{equation*}
\sigma(x)=\frac{1}{1+e^{-x}} \tag{5}
\end{equation*}
$$

Compute the gradient $\nabla_{\mathbf{x}} f(\cdot)$ and evaluate it at at $\hat{\mathbf{x}}=(-1,3,4,5,-5,7)$.

$$
\bigcirc\left[\begin{array}{c}
0 \\
0.031 \\
0.026 \\
-0.013 \\
-0.062 \\
-0.062
\end{array}\right] \bigcirc\left[\begin{array}{c}
0 \\
0.157 \\
0.131 \\
-0.065 \\
-0.314 \\
-0.314
\end{array}\right] \quad\left[\begin{array}{c}
0 \\
0.357 \\
0.268 \\
-0.214 \\
-0.894 \\
-0.894
\end{array}\right] \quad \bigcirc\left[\begin{array}{c}
0 \\
0.357 \\
0.268 \\
-0.214 \\
-0.447 \\
-0.447
\end{array}\right]
$$

6. (2 points) Which of the following functions are convex?$\|\mathbf{x}\|_{\frac{1}{2}}$$\min _{i=1}^{k} \mathbf{a}_{i}^{T} \mathbf{x}$ for $\mathbf{x} \in \mathbb{R}^{n}$, and a finite set of arbitrary vectors: $\left\{\mathbf{a}_{1}, \ldots, \mathbf{a}_{k}\right\}$$\log \left(1+\exp \left(\mathbf{w}^{T} \mathbf{x}\right)\right)$ for $\mathbf{w} \in \mathbb{R}^{d}$All of the above
7. (2 points) Suppose you want to predict an unknown value $Y \in \mathbb{R}$, but you are only given a sequence of noisy observations $x_{1}, \ldots, x_{n}$ of $Y$ with i.i.d. noise $\left(x_{i}=Y+\epsilon_{i}\right)$. If we assume the noise is I.I.D. Gaussian $\left(\epsilon_{i} \sim N\left(0, \sigma^{2}\right)\right)$, the maximum likelihood estimate $(\hat{y})$ for $Y$ can be given by:A: $\hat{y}=\operatorname{argmin}_{y} \sum_{i=1}^{n}\left(y-x_{i}\right)^{2}$B: $\hat{y}=\operatorname{argmin}_{y} \sum_{i=1}^{n}\left|y-x_{i}\right|$C: $\hat{y}=\frac{1}{n} \sum_{i=1}^{n} x_{i}$
$\bigcirc$ Both A \& CBoth B \& C
